## DISSERTATION

## GAS LIFT OPTIMIZATION OF BAYAN WELLS USING PROSPER

BY

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## **CERTIFICATION OF APPROVAL**

### Gas Lift Optimization Of Bayan Wells Using PROSPER

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A project dissertation submitted to the Petroleum Engineering Programme Universiti Teknologi PETRONAS in partial fulfilment of the requirement for the BACHELOR OF ENGINEERING (Hons) (PETROLEUM ENGINEERING)

Approved by,

(Dr. Mohd Nur Fitri Ismail)

UNIVERSITI TEKNOLOGI PETRONAS TRONOH, PERAK September 2012

## **CERTIFICATION OF ORIGINALITY**

This is to certify that I am responsible for the work submitted in this project, that the original work is my own except as specified in the references and acknowledgements, and that the original work contained herein have not been undertaken or done by unspecified sources or persons.

MUHAMMAD AIZUDDIN B. MOHAMMAD ROSLAN

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### ABSTRACT

This project aims to study the complete mechanism of gas lift optimization and application to help increase the oil and gas production in BAYAN wells. The BAYAN wells have been producing for several years now and the production rate have been declining over time and in need of well stimulation and gas lift optimization is the best option. Gas lift optimization is the most common artificial lift method widely used in oil production. It will help to increase the production by increasing the effective density of the oil and increasing the pressure inside the reservoir. The total gas used for oil production is constrained by daily availability limits and limits on maximum injection volume into each well. The oil produced from each well is known to be a nonlinear function of the gas injected into it and varies between wells. The problem is to identify and inject the optimal amount of gas into each well to maximize the total amount of oil production from the reservoir on a daily basis. The problem has long been of practical interest to all major oil exploration companies as it has a potential of deriving large financial benefits. Thus, it is hoped that this project will increase the production rate of BAYAN wells.

### **INTRODUCTION**

#### Background

As a reservoir produces, it naturally encounters pressure drop, solution gas reduction and water cut increase which can stop or reduce its production flow rate. Artificial lift methods including gas lift can resume or increase the production rate by adding some additional energy to the fluid in well. Gas lift is one of the most common artificial lift methods which are used widely in oil production process. The objective of installing gas lift in a completion is to increase the drawdown on the producing formation by injecting gas into the lower part of the oil column and consequently reducing the flowing gradient in the oil column. This cab increase flow rate or bring a dead well on production. Gas lift optimization is crucial to ensure maximum oil production within facility constraints. During the lift process, gas is injected into the tubing. Gas injection will lighten the fluid column along the tubing, so it will increase oil production. Normally oil production increases as gas injection increases. However, the gas injection has an optimum limit because too much gas injection will cause slippage, where gas phase moves faster than liquid, so that it reduces oil production.

Gas lift becomes critical to sustain production as oil fields mature. Increasing watercut and decreasing reservoir pressure eventually cause wells to cease natural flow. Subsequently, gas lift is required to kick off and sustain flow from these wells. Gas lift optimization requires a lot of effort, and faces many challenges in the process of implementation. However, the gain is significant, and always perceived as the most cost effective restoration method. Many parameters are involved in a successful gas lift operation. Gas lift optimization means specifying these parameters in such a way that the production and the operation's net present value are maximized. If the parameters are not specified properly, the operations become impossible or at least uneconomical.

For this project, the field used is BAYAN field located offshore of Sarawak.

#### **Problem Statement**

Problem Identification:

• As the oil field mature, the productions from the field have been declining over the years. This is due to the fact that the pressure inside the reservoir is decreasing as the oil and gas produced from the well increases, thus reducing the flow of oil and gas from the well.

Significant of the Project:

• This project will help to investigate the best methods and process of gas lift to optimize BAYAN Field production. The optimization will have a return value acceptable with the cost needed to perform the gas lift.

#### **Objectives and Scope of Study**

I. To optimize the production of BAYAN field well by using gas lift optimization.

### LITERATURE REVIEW

#### **Gas Lift**

In an oil producing-well, reservoir fluid consisting of oil and water and sometimes together with gas flows from reservoir through a tubing toward surface facilities. In case where the reservoir pressure is high enough, the reservoir fluid can flows up to the surface naturally. However as time increases, the reservoir depletes and the pressure decreases. If this happened, oil production decreases so that artificial lift methods, such as gas lift method need to apply.

Gas lift is the method of artificial lift that uses external source of high-pressure an gas for supplementing formation gas to lift the well fluids. The primary consideration in the selection of a gas-lift system to lift a well, a group of wells, or an entire field is the availability and compression cost of gas. Continuous-flow gas lift is the only method of artificial lift that fully utilizes the energy in the formation gas production. Most wells are gas lifted by continuous flow, which can be considered an extension of natural flow by supplementing the formation gas with additional high pressure gas from an outside source. Gas is injected continuously into the production conduit at a maximum depth on the basis of the available injection gas pressure. The injection gas mixes with the produced well fluids and decreases the flowing pressure gradient of the mixture from the point of gas injection to the surface. The lower bowing pressure gradient reduces the flowing bottomhole pressure (BHFP) to



Figure 1 – Continues Gas Lift

establish the drawdown required for attaining a design production rate from the well. In a typical gas lift system, compressed gas is injected through gas lift mandrels and valves into the production string. The injected gas lowers the hydrostatic pressure in the production string to re-establish the required pressure differential between the reservoir and well bore, thus causing the formation fluids to flow to the surface.

Produce fluid and gas along with injected gas is then flown into separator. Produced oil is pumped to storage while injected gas and produced gas is returned to the suction side of the compressor. After the gas is recompressed, the rotation cycle is completed. Make up gas from another gas producing well is used for compressor startup. The typical general gas lift system is shown on following figure.



If sufficient drawdown in the bottomhole pressure (BHP) is not possible by continuous flow, intermittent gas lift operation may be used. Intermittent gas lift requires high instantaneous gas volumes to displace liquid slugs to the surface. The disadvantage of intermittent lift is an "on-off" need for high pressure gas, which presents a gas handling problem at the surface and surging in the BHFP that cannot be tolerated in many wells producing sand. Most high-pressure gas lift systems are designed to recirculate the lift gas. The lowpressure gas from the production separator is compressed and reinjected into the well to lift the fluids from the well. This closed loop is referred to as a closed rotative gas-lift system. Continuous-flow gas lift operations are preferable with a closed rotative system.



Figure 3 – Intermittent Gas Lift

Intermittent gas lift operations are particularly difficult to regulate and to operate efficiently in smaller closed rotative systems with limited gas storage capacities in the low- and high-pressure lines.



According to completion procedure, general gas lift classification has been shown in the figure below.

Gas lift optimization is key factor to enhance the production performance in a maturing environment, where natural production depletes rapidly. During initial stage of gas lift operation, the focus is to kick off dead wells; less attention is put in optimization effort. The initial oil production buildup is substantial as dead wells resumed production. With the increasing numbers of gas lift wells online, gas lift optimization efforts become critical to maximize oil production within system constraints. Pressure of a production system is carefully preset to meet specific delivery requirement. In certain circumstances, production system pressure may be reduced, which translates to less surface backpressure to wells. With lower backpressure, a well can produce at higher drawdown, hence higher flow rate.

 $q = Productivity Index \times drawdown$ 

The gas allocation optimization problem is a complicated long time problem of interest. Liquid production rate for each well is nonlinear function of gas injection rate, but unfortunately it is not known explicitly. In existing approaches, the optimization problem has been solved in three steps of procedure. In first step, a set of data relating gas injection to oil production from each well are collected. The data may be obtained from field data or numerical simulation data. In second step, a regression or interpolation method is applied to estimate the nonlinear function which relates gas injection to liquid production.

However, a thorough evaluation is necessary before commitment is made as they are certain setbacks, e.g. lower compressor discharge pressure, lower sales gas volume etc. Also, not all wells will respond to the lower backpressure. A low Gas-Oil ratio (GOR) well is more likely to respond to the lower system pressure whereas for a high GOR well, choke is normally installed to control drawdown. In this case, the backpressure exerted on the well is the high tubing head pressure upstream to the choke due to restricted flow across the choke. Reduction in production system pressure downstream to the choke has no impact to the well

In most cases, oil is produced using gas lift system from an oil field which consists of a group of gas lift wells such as BAYAN Field. The most common optimization problem faced in multi gas lift wells system is maximization of total oil production. Let the total gas available for injection N gas lift wells are given by  $Q_{gav}$ . How much gas should be injected to each well to maximize total oil production? Since

$$q_0 = (1 - WC)q_l$$

Then the problem can be written as a constrained maximization

$$maxQ_0 = \sum_{k=1}^{N} (1 - WC_k)\varphi_k(qg_k)$$

Subject to

$$\sum_{k=1}^{N} qg_k \le Qg_{av}$$

In case where the gas available for injection Qgav is large enough, then for each k = 1, 2, ..., N, gas injection qgk is chosen such that maximizing liquid production 'k(qgk ). Gas available for injection Qgav is usually very limited and should be shared in optimal form for each well.

#### Advantages and Limitations of Gas Lift

The flexibility of gas lift in terms of production rates and depth of lift cannot be matched by other methods of artificial lift if adequate injection-gas pressure and volume are available. Gas lift is one of the most forgiving forms of artificial lift, since a poorly designed installation will normally gas lift some fluid. Many efficient gas lift installations with wireline-retrievable gas lift valve mandrels are designed with minimal well information for locating the mandrel depths on initial well completion. Highly deviated wells that produce sand and have a high formation gas/liquid ratio are excellent candidates for gas lift when artificial lift is needed. Many gas lift installations are designed to increase the daily production from flowing wells. No other method is as ideally suited for through-flowline (TFL) ocean floor completions as a gas lift system.

Maximum production is possible by gas lift from a well with small casing and high deliverability. Wireline-retrievable gas lift valves can be replaced without killing a well or pulling the tubing. The gas lift valve is a simple device with few moving parts and sand-laden well fluids do not have to pass through the valve to be lifted. The individual well in-hole equipment is relatively inexpensive. The surface equipment for injection gas control is simple and requires little maintenance and practically no space for installation. The reported overall reliability and operating costs for a gas lift system are lower than for other methods of lift. Maximum liquid production is achieved by availing gas lift system. The performance comparison of different artificial lift method has been shown in figure below.



Figure 6 – Hydraulic Pump, PCP Pump, Rod Pump and Plunger lift Performance Curve.

The primary limitations for gas lift operations are the lack of formation gas or of an outside source of gas, wide well spacing, and available space for compressors on offshore platforms. Generally, gas lift is not applicable to single-well installations and widely spaced wells that are not suited for a centrally located power system. Gas lift can intensify the problems associated with production of a viscous crude, a super-saturated brine, or an emulsion. Old casing, sour gas, and long, small-ID flowlines can rule out pas lift operations. Wet gas without dehydration will reduce the reliability of gas lift operations.

#### **Inflow Performance**

The Inflow Performance Relationship (IPR) describes pressure drawdown as a function of production rate, where drawdown is defined as the difference between static and flowing bottom hole pressure (FBHP). The simplest approach to describe the inflow performance of oil wells is the use of the productivity index (PI) concept. It was developed using the following assumptions:

- Flow is radial around the well
- A single-phase liquid is flowing
- Permeability distribution in the formation is homogeneous
- The formation is fully saturated with the given liquid.

The flow through a porous media is given by the Darcy equation:

$$\frac{q}{A} = \frac{k}{\mu} \frac{dp}{dl}$$

Using the assumptions above it can be written as

$$q = \frac{0.00708kh}{\mu\beta ln\left(\frac{r_e}{r_w}\right)} \left(p_r - p_{wf}\right)$$

Where:

q = liquid rate, STB/d

k = effective permeability, mD

h = pay thickness, ft

 $\mu$  = liquid viscosity, cP

B = liquid volume factor, bbl/STB

re = drainage radius of well, ft

rw = radius of wellbore, ft

pR = average reservoir pressure

pwf = flowing bottomhole pressure

Most parameters on the right hand side are constant, which permits collecting them into a single coefficient called PI:

$$q = PI(p_r - p_{wf})$$

This gives us:

$$PI = \frac{q}{\left(p_r - p_{wf}\right)}$$

This equation states that liquid inflow into a well is directly proportional to the pressure drawdown. It will plot as a straight line on a pressure vs. rate diagram. The use of the PI concept is quite straightforward. If the average reservoir pressure and the PI are known, use of equation above gives the flow rate for any FBHP. The well's PI can either be calculated from reservoir parameters, or measured by taking flow rates at various FBHPs.

This works well for a single phase flow, but when producing a multiphase reservoir the curve will not plot as a straight line. As the oil approaches the well bore and the pressure drops below bubble point, gas comes out of solution. Thus, the free gas saturation in the vicinity of the oil steadily increases, which implies that the relative permeability to gas steadily increases at the expense of the relative permeability of oil. The greater the drawdown, the bigger this effect would be. Since the PI depends on the effective oil permeability, it is expected that it will decrease. Figure below shows the IPR curve for this condition.





Vogel used a numerical reservoir simulator to study the inflow of wells depleting solution gas drive reservoirs. He considered cases below bubble point and varied parameters like draw downs, fluid and rock properties. Vogel found that the calculated IPR curves exhibited the same general shape, which is given by the dimensionless equation:

$$\frac{q}{q_{max}} = 1 - 0.2 \frac{p_{wf}}{2} - 0.8 \left(\frac{p_{wf}}{p_r}\right)^2$$

The equation is generally accepted for other drive mechanisms as well, and is found to give reliable results for almost any well with a bottom hole pressure below bubble point of the oil. There are a number of other models designed for special cases e.g. horizontal wells, transient flow, fractured wells, non-Darcy pressure loss, high rates etc.

#### **Outflow Performance**

The well's outflow performance, or Vertical Lift Performance (VLP), describes the bottomhole pressure as a function of flow rates. According to Golan and Whitson the outflow performance is dependent on different factors; liquid rate, fluid type (gasto- liquid ratio, water cut), fluid properties and tubing size. Gabor divides the total pressure drop in a well into a hydrostatic component, friction component and an acceleration component:

<u>Hydrostatic component</u> represents the change in potential energy due to gravitational force acting on the mixture:

$$\left(\frac{dp}{dl}\right)_h = \rho g \sin \beta$$

Where:  $\rho = \text{density of fluid}$ 

 $\beta$  = pipe inclination angle, measured from horizontal g = gravity constant <u>Friction component</u> stands for the irreversible pressure losses occurring in the pipe due to fluid friction on the pipe inner wall:

$$\left(\frac{dp}{dl}\right)_f = \frac{1}{d}f\frac{1}{2}\rho v^2$$

Where: f = friction factord = pipe inside diameterv = fluid velocity

The type of flow is determined from the Reynolds number:

$$Re = \frac{\rho v d}{\mu}$$

Where:  $\mu =$ fluid viscosity

The boundary between flows regimes are:

$\operatorname{Re} \leq 2000$ :	Laminar flow
$2000 < \text{Re} \le 4000$ :	Transition between laminar and turbulent flow
4000 < Re:	Turbulent flow

<u>Acceleration component</u> represents the kinetic energy changes of the flowing mixture and is proportional to the changes in flow velocity. The term is often negligible:

$$\left(\frac{dp}{dl}\right)_a = -\rho v \frac{dv}{dl}$$

#### **Multiphase Flow**

Oil wells normally produce a mixture of fluids and gases to the surface while phase conditions usually change along the path. At higher pressures, especially at the well bottom, flow may be single phase. But going up in the well the continuous decrease of pressure causes dissolved gas to gradually escape from the flowing liquid, resulting in multiphase flow. Gas injection into a well is also an example of multiphase flow. In single phase flow we discriminate between laminar and turbulent flow. In two phase flow we discriminate in addition between flow regimes that are characteristic for the time and space distribution of gas and liquid flow. In horizontal flow we discriminate between the flow regimes:

- Stratified flow
- Slug flow
- Dispersed bubble flow
- Annular flow

These are shown in figure below. At low velocities the gas and liquid are separated as in stratified flow. At high velocities gas and liquid become mixed. Slug flow is an example of a flow regime in between, representing both separation and mixing. Slug flow is consequently referred to as an intermittent flow regime.



In vertical flow we discriminate between the flow regimes

- Slug flow
- Churn flow
- Dispersed bubble flow
- Annular flow

Figure below illustrates the flow regimes in vertical flow. The same comments that apply to horizontal flow are valid in vertical flow. The big difference is that in vertical (concurrent upward) flow it is not possible to obtain stratified flow. The equivalent flow regime at identical flow rates of gas and liquid is slug flow with very slow bullet shaped Taylor bubbles.



### **BAYAN Oil Field**

Bayan oil field is located offshore of Sarawak. It is one of Malaysia's longest serving oil field. It consists of 3 parts name 'West Bayan', 'North West Bayan' and 'North Bayan'.

## **METHODOLOGY**

#### PROSPER

PROSPER is a PROduction and System PERformance analysis software. It assists the production or reservoir engineer to predict tubing and pipeline hydraulics and temperature with accuracy and speed. Prosper's powerful sensitivity calculation features enable existing design to be optimized. It helps petroleum producers to maximize their production earnings by providing the means of critically analyzing the performance of each producing well.

#### **Preparation of Well Model in Prosper**

The well models in this work had been prepared by Prosper program. Prosper makes model for each component of the producing well system separately which contributes to overall performance, and then allows to verify each model subsystem by performance matching. In this way, the program ensures that the calculation is as accurate as possible. Once the system model has been tuned to real data, Prosper is confidently used to model the well in different scenarios and to make forward predictions of reservoir pressure based on surface production data.

#### **Prosper's Approach and Systems Analysis**

Prosper's approach is to first construct a robust PVT model for the reservoir fluid. The PVT model is constructed by entering laboratory PVT data and adjusting the correlation model until it fits the measured data for improving the accuracy of forward prediction. Well potential and producing pressure losses are both dependent on fluid (PVT) properties. The accuracy of system analysis calculation is therefore dependent on the accuracy of the fluid properties model.

In the VLP matching phase, Prosper divides the total pressure loss into friction and gravity components and uses a non-linear regression technique to separately optimize the value of each component. Not only does the matching process result in a more accurate model, it also highlights the inconsistencies in the PVT model or in equipment description.

When sufficient accurate field data is available, robust PVT, IPR and VLP models are prepared by performance matching. Each model component is separately validated; therefore dependency on the components of the model can be eliminated. The following flow chart gives an outline of the calculation steps required to carry out a system analysis using Prosper and the thesis work had been performed according to this procedure.



Week	eek Objectives					
	FYP I					
5	Completion of preliminary research work					
6	Submission of extended proposal					
9	Completion of proposal defence					
12	Confirmation on lab material and equipment for conducting					
	experiment					
13	Submission of Interim draft report					
14 Submission of Interim report						
FYP II						
5	Finalized the experiment procedure					
6	Conducting experiment					
7	Result analysis and discussion					
8	Submission of progress report					
9	Preparation for Pre-SEDEX					
11	Pre-SEDEX					
12	Submission of draft report					
13	Submission of technical paper and dissertation					
14	Oral presentation					
15	Submission of project dissertation					

Table 1 – Gantt chart

## **Result, Calculation & Discussion**

Well model set up of this FYP work had been approached systematically by working from left to right through the main screen of Prosper. The main screen is divided into following order:

- Options Summery
- PVT Data
- Equipment Data
- Gas Lift Data (for gas lift well)
- IPR Data
- Calculation Summary

This order reflects the recommended workflow to follow to set up the well model. The first five sections are input data screen and the last section mentions all the calculation and design features. Calculation menus are activated only when the necessary input data has been entered.



Fluid Description       Calculation Type         Fluid Oil and Water       Predict         Method Black Oil       Model Rough Approximation         Separator       Single-Stage Separator         Separator       Output         Hydrates       Disable Warning         Water Viscosity       Use Default Correlation         Viscosity Model       Newtonian Fluid         Well       Well Completion         Flow Type       Tubing Flow         Well Type       Tubing Flow         Well Type       Tubing Flow         Well Type       Producer         Artificial Lift       Reservoir         Method Gas Lift       Inflow Type Single Branch         Type       No Friction Loss In Annulus         User information       Comments (Cntl-Enter for new line)         Comments       Comments (Cntl-Enter for new line)	p Comments	Datestamp D	port <u>H</u> elp	Cancel <u>R</u> eport <u>Expo</u>	D <u>o</u> ne (
Fluid       Oil and Water <ul> <li>Predict</li> <li>Pressure and Temperature (offshore)</li> <li>Model</li> <li>Rough Approximation</li> <li>Range</li> <li>Full System</li> <li>Output</li> <li>Show calculating data</li> <li>Water Viscosity</li> <li>Use Default Correlation</li> <li>Viscosity Model</li> <li>Newtonian Fluid</li> <li>Well</li> <li>Well</li> <li>Well Type</li> <li>Tubing Flow</li> <li>Well Type</li> <li>Producer</li> <li>Well Type</li> <li>Producer</li> <li>Method</li> <li>Gas Lift</li> <li>Type</li> <li>No Friction Loss In Annulus</li> <li>Water Information</li> <li>Comments (Cntl-Enter for new line)</li> <li>Comments (Cntl-Enter for new line)</li></ul>		Calculation Type			Fluid Description
Method       Black Oil       Image Separator       Model       Rough Approximation         Separator       Single-Stage Separator       Output       Show calculating data         Emulsions       No       Image       Output       Show calculating data         Water Viscosity       Use Default Correlation       Image       Output       Show calculating data         Well       Viscosity       Use Default Correlation       Image       Well Completion         Flow Type       Tubing Flow       Image       Type       Cased Hole         Well       Type       Producer       Image       Beservoir         Artificial Lift       Image       Image       Single Branch         Type       No       Field       Sas Coning       No	re and Temperature (offshore)	Predict	-	Oil and Water	Fluid
Separator       Single-Stage Separator         Emulsions       No         Hydrates       Disable Warning         Water Viscosity       Use Default Correlation         Viscosity Model       Newtonian Fluid         Well       Image: Full System         Flow Type       Tubing Flow         Well       Image: Full System         Image: Full System	Approximation	Model	-	Black Oil	Method
Separator       Single-Stage Separator         Emulsions       No         Hydrates       Disable Warning         Water Viscosity       Use Default Correlation         Viscosity Model       Newtonian Fluid         Well       Well Completion         Flow Type       Tubing Flow         Well Type       Type Cased Hole         Gravel Pack       No         Artificial Lift       Inflow Type         Method       Gas Lift       Inflow Type         Type       No Friction Loss In Annulus       Gas Coning         User information       Comments (Cntl-Enter for new line)         Company       Taisman Energy Norge AS         Field       Varg	stem 💌	Range			
Emulsions       No         Hydrates       Disable Warning         Water Viscosity       Use Default Correlation         Viscosity Model       Newtonian Fluid         Well       Image: Strategy	alculating data 📃	Output	-	Single-Stage Separator	Separator
Hydrates       Disable Warning         Water Viscosity       Use Default Correlation         Viscosity Model       Newtonian Fluid         Well       Image: Completion         Flow Type       Tubing Flow         Well Type       Type Cased Hole         Gravel Pack       No         Artificial Lift       Image: Single Branch         Type       No Friction Loss In Annulus       Gas Coning         User information       Comments (Cntl-Enter for new line)         Company       Taisman Energy Norge AS         Field       Varg			-	No	Emulsions
Water Viscosity       Use Default Correlation         Viscosity Model       Newtonian Fluid         Well       Well Completion         Flow Type       Tubing Flow         Well Type       Producer         Artificial Lift       Gas Lift         Type       No Friction Loss In Annulus         User information       Comments (Cntl-Enter for new line)         Company       Talisman Energy Norge AS         Field       Varg			-	Disable Warning	Hydrates
Viscosity Model       Newtonian Fluid         Well       Well Completion         Flow Type       Type Cased Hole         Well Type       Producer         Artificial Lift       Reservoir         Method       Gas Lift         Type       No Friction Loss In Annulus         User information       Comments (Cntl-Enter for new line)         Company       Talisman Energy Norge AS         Field       Varg			•	Use Default Correlation	Water Viscosity
Well       Image: Second			•	Newtonian Fluid	Viscosity Model
Well       Well Completion         Flow Type       Tubing Flow         Well Type       Producer         Artificial Lift       Gravel Pack         Method       Gas Lift         Type       No Friction Loss In Annulus         User information       Comments (Cntl-Enter for new line)         Company       Taisman Energy Norge AS         Field       Varg					
How Type       Tubing How         Well Type       Producer         Artificial Lift       Image: Company Produce Pack         Method       Gas Lift         Type       No Friction Loss In Annulus         User information       Comments (Cntl-Enter for new line)         Company       Taisman Energy Norge AS         Field       Varg		Well Completion		The second s	Well
Well Type       Producer       Gravel Pack No         Artificial Lift       Reservoir         Method       Gas Lift       Inflow Type         Type       No Friction Loss In Annulus       Gas Coning         User information       Company       Talisman Energy Norge AS         Field       Varg       Inflow Type		I ype	<u> </u>	Tubing Flow	Flow Type
Artificial Lift Method Gas Lift Type No Friction Loss In Annulus User information Company Talisman Energy Norge AS Field Varg		Gravel Pack		Producer	Well Type
Method     Gas Lift     Inflow Type     Single Branch       Type     No Friction Loss In Annulus     Gas Coning     No       User information     Comments (Cntl-Enter for new line)     Comments (Cntl-Enter for new line)       Field     Varg		Reservoir			Artificial Lift
Type     No Friction Loss In Annulus     Gas Coning     No       User information     Comments (Cntl-Enter for new line)       Company     Talisman Energy Norge AS       Field     Varg	Branch 🗾	Inflow Type	•	Gas Lift	Method
User information Company Talisman Energy Norge AS Field Varg	•	Gas Coning	•	No Friction Loss In Annulus	Туре
User information Company Talisman Energy Norge AS Field Varg					
Field Varg	new line)	Comments (Cntl-Er			User information
Field Varg	<u> </u>			Talisman Energy Norge AS	Company
				Varg	Field
Location Varg W				Varg W	Location
Well A-03				A-03	Well
Platform					Platform
Analyst					Analyst
Date	-				Date

Figure 11 – System Summary

To predict pressure and temperature changes from the reservoir along the well bore and flow line tubular, it is necessary to accurately predict fluid properties as a function of pressure and temperature. Full set of PVT data had been entered to describe the fluid properties properly and enable the program to calculate them. Necessary PVT data had been adopted from the report.

	141.0	0-010-0	Correlations
Solution GOR	943.7	5m3/5m3	Pb, Rs, Bo   Standing
Gao Gravity	0.937		
uas uravių	200000	op. gravity	
Mole Percent H2S	0	percent	
npurities			
Mole Percent CO2 Mole Percent N2	2.468	percent	
			<u></u>

D <u>one M</u> air 128 Free Tempo Bubbl	Free Free Free Free Free Free Free Free	<u>}eset</u> Copy ee Free deg ( BARa	Clip J	nport PVIP Import Tr <u>a</u> nsfer <u>P</u> lot <u>H</u> elp ≤< ≥>
Pressure BARa 203	Gas Oil Ratio Sm3/Sm3 141.9	Oil FVF m3/Sm3 1.545	Oil Viscosity mPa.s 0.292	

Figure 13 – PVT Input Data

Done Main Match Match All Parameters Plot Help									
Match On	Match On Correlations								
All/ <u>N</u> one	Standard Deviation	Parameter 1	Parameter 2	Pb,Rs,Bo					
Bubble Point	0	0.9921	-23.5173						
🔄 Gas Oil Ratio	1.2449e-5	1.02897	-7.62092	Oil Viscosity					
🔄 Oil FVF	0	0.96506	0.034404	Beal et al					
(Above Bubble Point)		1	1e-8						
🔲 Oil Viscosity	0	1.06519	0.016844						

Figure 14 - Regression Screen

D <u>o</u> ne <u>C</u> ancel <u>M</u> ain <u>R</u> eset all <u>H</u> elp							
Bubble Point							
	Glaso	Standing	Lasater	Vazquez-Beggs	Petrosky et al		
Parameter 1	0.9741	0.9921	1.07561	0.91525	0.96564		
Parameter 2	-80.0365	-23.5173	192.26	-299.209	-108.123		
Std deviation							
	Reset	Reset	Reset	Reset	Reset		
Solution GOR							
	Glaso	Standing	Lasater	Vazquez-Beggs	Petrosky et al		
Parameter 1	1.08626	1.02897	0.82579	1.24987	1.37621		
Parameter 2	-13.7636	-7.62092	-0.16847	-2.43204	-211.82		
Std deviation	0.070873	1.2449e-5			0.70986		
	Reset	Reset	Reset	Reset	Reset		
-Oil FVF	Dil EVE						
	Glaso	Standing	Lasater	Vazquez-Beggs	Petrosky et al		
Parameter 1	1.06122	0.96506	0.96508	1.13397	0.96379		
Parameter 2	-0.066466	0.034404	0.034364	-0.13397	0.022157		
Parameter 3	1	1	1	1	1		
Parameter 4	1e-8	1e-8	1e-8	1e-8	1e-8		
Std deviation							
	Reset	Reset	Reset	Reset	Reset		
-Oil Viscosity							
	Beal et al	Beggs et al	Petrosky et al				
Parameter 1	1.06519	0.94676	0.88495				
Parameter 2	0.016844	-0.017394	-0.043624				
Std deviation							
	Reset	Reset	Reset				

Figure 15 – Correlation Parameters Screen

Done	<u>C</u> ancel	<u>A</u> ll	<u>E</u> dit	<u>Summary</u>				
<u>R</u> eport	E <u>x</u> port	Rese <u>t</u>	<u>H</u> elp					
Input Data	iation Survey ace Equipment inhole Equipme thermal Gradier rage Heat Capa	nt It acities						
Disable Surface Equipment No								
	Figure 16 – Equipment Input Data							

	one <u>C</u> ancel	<u>M</u> ain	Help Impo	rt <u>Plot</u>	Eilter
	t Data				
mpe	Measured Depth	True Vertical Depth	Cumulative Displacement	Angle	
	(m)	(m)	(m)	(degrees)	
1	0	0	0	0	
2	167.7	167.7	0	0	
3	394.5	394.18	12.044	3.04407	
4	494.57	492.21	32.1468	11.5888	
5	639.9	627.43	85.4043	21.4974	
6	872.8	829.92	200.47	29.6076	
7	1076.5	1006.01	302.872	30.1792	
8	1396.9	1284.91	460.577	29.4862	
9	1592.27	1457.25	552.601	28.1007	
10	1883.87	1711.31	695.723	29.3943	
11	2174.96	1962.12	843.465	30.5006	
12	2493.1	2234.9	1007.18	30.9717	
13	2786.16	2485.16	1159.68	31.3556	
14	2990.12	2 2652.8 1275.85		34.7219	
15	3194.67	2820.62	1392.8	34.8716	
16	3345.22	2942.82	1480.74	35.7386	
17	3462.35	3036.88	1550.54	36.5788	
18	3500	3066.87	1573.3	37.1981	
Γ <sup>MD</sup>	<-> IVD	-			1
		I	Caj	culate	

Figure 17 – Deviation survey data

ut Data									_
Label	Туре	Measured Depth	Tubing Inside Diameter	Tubing Inside Roughness	Tubing Outside Diameter	Tubing Outside Roughness	Casing Inside Diameter	Casing Inside Roughness	Rate Multiplier
		(m)	(inches)	(inches)	(inches)	(inches)	(inches)	(inches)	
	Xmas Tree	23.8							
	Tubing	448.29	4.778	0.0006					1
TRSV	SSSV		4.562						1
	Tubing	3132.05	4.778	0.0006					1
	Tubing	3155.84	4.67	0.0006					1
	Tubing	3160.24	4.778	0.0006					1
Liner	Tubing	3385	4.811	0.0006					1

Figure 18 – Downhole Equipment data

Done Cancel Main Help Default						
Input Parameters						
Cp Oil	2.219	KJ/Kg/K				
Cp Gas	2.13527	KJ/Kg/K				
Cp Water	4.1868	KJ/Kg/K				
Cp Water	4.1868	KJ/Kg/K				

Figure 19 – Average Heat Capacities

Done         Validate         Calculate         Be           Cancel         Reset         Elot         Ex           Help         Model and Global Variable Selection         Selection	port Transfer Data Select Model Input Data
Reservoir Model PI Entry Vogel Composite Darcy Felkovich MultiPade Felkovich Jones Transent Horizontal Well - No Flow Boundaries Horizontal Well - Constant Fressure Upper Boundary MultiLayer Reservoir External Entry Horizontal Well - OF Friction Loss In WellBore SkriAde (ELF) Dual Prozety Horizontal Well - Transverse Vertical Fractures	Mechanical / Geometrical Skin     Deviation and Partial Penetration Skin       ExcKe MacLeod Karekas+Tarig     300       BaRa     BARa       Reservoir Pressure Water Cut, 95     96       Water Cut, 95     percent.       Total GOR 141-9     Sm3/Sm3       Relative Permeability     No
Figure 20	0 – IPR Model Selection

For matching Bubble point pressure, Solution GOR and Oil FVF; Prosper uses following traditional Black oil correlations: Glaso, Standing, Lesater, Vazquez-Beggs and Petrosky.

For matching Oil Viscosity; Prosper uses Beal at el, Beggs at el and Petroskey at el. Carefully inspecting the correlation parameters in Prosper, the following correlations had been identified for the best overall fit for the matched PVT:

- Pb, Rs and Bo -----Standing
- Oil viscosity -----Beal at el

After selecting the best fit correlations, PVT input data had been matched with measured data and Prosper was showing PVT is MATCHED in input screen.

ut Parameters	1.41.0		Correlations	[a	
Solution GOR	141.9	Sm3/Sm3	Pb, Rs, Bo	Standing	<u> </u>
Oil Gravity	843.7	Kg/m3	Oil Viscosity	Beal et al	<b>_</b>
Gas Gravity	0.937	sp. gravity			
Water Salinity	200000	ppm			
urities	10				
urities Mole Percent H2S	0	percent			
urities Mole Percent H2S Mole Percent CO2	0	percent			

Figure 21 – Matched PVT

## **PVT Plot**

A PVT plot with GOR versus Pressure had been drawn to check the consistency with the match data. From the plot diagram, it had been observed that the Black oil model had been properly matched with the PVT match data.







West Bayan PVT

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Based on the data obtained from the field, the summary STOIIP, EUR and recovery factor for each well have been tabulated.

**SUMMARY STOIP - MMSTB** 

	BLOCKS	S0	<b>S</b> 1	S2	S3	S4	S5	S6	<b>S</b> 7	TOTAL
W BAYAN	1	-	14.5	22.9	14.4	49.1	5.0	2.1	18.5	126.50
	2 A	-	1.2	1.0	1.2	7.1	0.7	-	1.2	12.20
	2 B	35.2	3.1	8.1	1.2	1.4	0.4	-	0.1	49.40
	4	1.9	5.3	9.3	15.2	22.3	1.4	-	7.3	62.61
	5 E	-	0.2	2.0	2.8	-	0.6	0.3	0.2	6.15
	SUB TOTAL	37.1	24.2	43.3	34.6	79.9	8.1	2.4	27.3	256.86
	3	11.3	3.9	6.5	23.1	-	-	-	-	44.76
	5 W12	18.7	-	10.5	39.0	-	-	-	-	68.19
	5 W34	4.0	1.3	2.4	3.6	-	-	-	-	11.30
INVV DATAN	5 W5	1.9	-	2.9	1.7	-	-	-	-	6.54
	NWB	2.6	5.5	1.8	4.9	-	-	-	-	14.83
	SUB TOTAL	38.4	10.7	24.2	72.3	-	-	-	-	145.62
	1	-	-	-	-	-	-	-	3.6	3.61
	2 A	-	-	-	-	-	-	-	0.1	0.10
	2 B/C	-	-	-	-	-	-	-	13.9	13.89
	2 D	-	-	-	-	-	-	-	1.8	1.80
N BAYAN	2 E/F	-	-	-	-	-	-	-	5.5	5.53
	3	-	-	-	-	-	-	-	1.3	1.31
	8 A	-	-	-	-	-	-	-	1.9	1.90
	NBA	-	-	-	1.4	2.4	-	-	-	3.87
	SUB TOTAL	-	-	-	1.44	2.43	-	-	28.14	32.01
	TOTAL	75.51	34.96	67.45	108.37	82.33	8.07	2.40	55.40	434.49

### SUMMARY EUR (MMSTB)

	BLOCKS	S0	S1	S2	S3	S4	S5	S6	S7	TOTAL
	1	-	0.0	7.1	8.9	24.0	1.2	-	9.0	50.19
W BAYAN	2 A	-	0.0	0.0	-	2.1	0.3	-	0.1	2.63
	2 B	10.5	0.0	0.3	0.0	-	-	-	-	10.79
	4	0.4	0.1	0.7	13.4	14.1	0.0	-	0.7	29.38
	5 E	-	-	-	-	-	-	-	-	-
	SUB TOTAL	10.9	0.1	8.1	22.2	40.3	1.6	-	9.8	92.99
	3	-	0.1	3.4	4.6	-	-	-	-	8.07
	5 W12	3.7	-	1.1	9.4	-	-	-	-	14.24
	5 W34	-	-	0.2	0.0	-	-	-	-	0.25
INW DATAN	5 W5	-	-	-	-	-	-	-	-	-
	NWB	-	1.2	-	0.0	-	-	-	-	1.22
	SUB TOTAL	3.7	1.3	4.6	14.1	-	-	-	-	23.78
	1	-	-	-	-	-	-	-	0.5	0.50
	2 A	-	-	-	-	-	-	-	-	-
	2 B/C	-	-	-	-	-	-	-	2.9	2.86
	2 D	-	-	-	-	-	-	-	0.5	0.49
N BAYAN	2 E/F	-	-	-	-	-	-	-	3.2	3.22
	3	-	-	-	-	-	-	-	-	-
	8 A	-	-	-	-	-	-	-	-	-
	NBA	-	-	-	-	-	-	-	-	-
	SUB TOTAL	-	-	-	-	-	-	-	7.07	7.07
	TOTAL	14.59	1.41	12.78	36.34	40.26	1.56	-	16.89	123.84

	BLOCKS	S0	S1	S2	S3	S4	S5	S6	S7	TOTAL
W BAYAN	1		0%	31%	62%	49%	24%	0%	49%	40%
	2 A		0%	3%	0%	30%	49%		12%	22%
	2 B	30%	0%	4%	0%	0%	0%		0%	22%
	4	20%	1%	8%	88%	63%	1%		9%	47%
	5 E		0%	0%	0%		0%	0%	0%	0%
	SUB TOTAL									
										0%
	3	0%	3%	52%	20%					18%
	5 W12	20%		10%	24%					21%
NW BAYAN	5 W34	0%	0%	8%	1%					2%
INV DATAN	5 W5	0%		0%	0%					0%
	NWB	0%	22%	0%	0%					8%
	SUB TOTAL									
	1								14%	14%
	2 A								0%	0%
	2 B/C								21%	21%
	2 D								27%	27%
N BAYAN	2 E/F								58%	58%
	3								0%	0%
	8 A								0%	0%
	NBA				0%	0%				0%
	SUB TOTAL	19.33%	4.05%	18.95%	33.54%	48.90%	19.35%	0.00%	30.48%	28.50%
>65%										
60%>RF>40%										
40%>RF>20%										
RF<20%										

#### **Recovery Factor**

After the simulation is completed, the results are tabulated in a table form based on the recovery factor table.

	BLOCKS	S0	S1	S2	S3	S4	S5	S6	S7	TOTAL
W BAYAN	1		0%	2%	6%	3%	1%	0%	4%	16%
	2 A		0%	0%	0%	2%	2%		1%	5%
	2 B	3%	0%	0%	0%	0%	0%		0%	3%
	4	3%	0%	0%	8%	5%	0%		0%	16%
	5 E		0%	0%	0%		0%	0%	0%	0%
	SUB TOTAL									
	3	0%	0%	5%	1%					6%
	5 W12	2%		1%	1%					4%
	5 W34	0%	0%	8%	0%					8%
NW DATAN	5 W5	0%		0%	0%					0%
	NWB	0%	1%	0%	0%					1%
	SUB TOTAL									
	1								1%	1%
	2 A								0%	0%
	2 B/C								2%	2%
	2 D								2%	2%
N BAYAN	2 E/F								3%	3%
	3								0%	0%
	8 A								0%	0%
	NBA				0%	0%				0%
	SUB TOTAL	8.00%	1.00%	16.00%	16.00%	10.00%	3.00%	0.00%	13.00%	
RF>10%										
10%>RF>0%										
RF<0%										

#### **Expected Recovery after Gas Lift Optimization**

### Discussion

This feature in Prosper enables to adjust the multiphase flow correlations to match the flowing bottomhole pressure. Prosper uses a non-linear regression to tune the VLP correlations to best match the measured data. This is done by calculating a pressure traverse using a correlation and determining the error between measured and calculated pressures. The gravity and friction terms of the pressure loss equations are then adjusted and the process is repeated until the measured and calculated results agree within 1 psi or 50 iterations have been completed.

**Parameter 1 (Gravity term):** This is the multiplier for the gravity term in the pressure drop correlation. Provided that the PVT has been correctly matched, the greatest source of uncertainty in the VLP calculation for oil wells is usually the holdup correlations. Prosper attempts to make a gravity component match by adjusting the holdup correlation. If a match is not obtained with a parameter 1 more than 5% away from the value 1, the density is adjusted. For single phase applications, no hold up correction is possible. So any significant deviation from 1.0 for parameter 1 indicates a PVT problem. If Prosper has to adjust parameter 1 by more than +10%, there is

probably an inconsistency between the fluid density predicted by the PVT model and the field data.

**Parameter 2 (Friction term):** This is the multiplier for the friction term in the pressure drop correlation. If parameter 2 requires a large correction, it is likely that there is an error in equipment description or the flow rates are incorrect. As the effect of a shift in the friction component on the overall pressure loss is less than for the gravity term, a larger range in the value of parameter 2 is expected. If Prosper has to adjust the parameter 2 by more than +-10%, there is probably an error in the value of roughness entered of the equipment.

In this work, once the matching process was completed, the match parameters had shown alongside each of the correlations that had been matched. Parameter 1 and 2 were found very much close to unity with PE-2 correlation for current well test data of all wells

#### **Correlations Comparison and Selecting the Best-fit Correlation**

Correlation comparison is the fundamental step in the quality check of the model. This option allows pressure gradient plots to be generated with different correlations to be compared with measured gradient survey data. The comparison enables to understand if the measurements make sense, i.e. violate or not the principle of physics and to select the flow correlation that best fits the experimental measurements.

Two most important correlations had been primarily considered for rough quality check. Those are Fancher Brown (FB) and Duns and Ros Modified (DRM) correlations.

**Fancher Brown:** The gradient correlation to the left is the Fancher Brown correlation which provides the minimum pressure losses. It is a no slip hold-up correlation that gives the lowest possible value of VLP. Since it neglects gas/liquid slips, it always predict a pressure which is less than the measured value. Thus, measured data falling to the left of Fancher Brown on the correlation comparison plot indicates that there is a problem with fluid density or with field pressure data.

**Duns and Ros Modified:** The gradient correlation to the extreme right is the Duns and Ros Modified correlation which provides the maximum pressure losses. This correlation usually performs better in mist flow cases and should be used in condensate wells. It tends to over predict VLP in oil wells. Thus, measured data falling to the right of Duns and Ros Modified on the correlation comparison plot indicates that the measured data points are not consistent.

Some other relevant correlations that had been compared are mentioned below:

**Hagedorn Brown:** This correlation performs well for slug flow at moderate to high production rates. It should not be used for condensate and whenever mist flow is the

main flow regime. Hagedorn Brown under predicts VLP at low rates and should not be used for predicting minimum stable rates.

**Petroleum Experts:** This correlation combines the best features of exiting correlations. It uses the Gould et al flow map and the Hagedorn Brown correlation in slug flow and Duns and Ros for mist flow. In the transition regime, a combination of slug and mist result is used.

**Petroleum Expert 2:** This correlation includes the features of Petroleum Experts correlation with original work on predicting low rate VLP and well stability.

**Petroleum Expert 3:** This correlation includes the features of Petroleum Experts 2 correlation with original work for viscous, volatile and foamy oils.

**Petroleum Experts 4:** The correlation is an advanced mechanistic model for any angled wells, suitable for any fluid (including retrograde condensate).

**Beggs and Brill:** This is primarily a pipe line correlation. It generally over predicts pressure drops in vertical and deviated wells.

**Hydro 3P (internal):** This correlation is a mechanistic model and considers three phase flow.

### CONCLUSION

The objective of the project is to study the best way to perform gas lift optimization in order to increase the production rate of BAYAN wells. From the research and simulation that will be done using PROSPER, it is hoped that a better understanding of the gas lift optimization will help to achieve the objective. Hence, it is expected that the result will be increase in production rate in BAYAN wells.

### NOMENCLATURE

q = Production rate, STB/day

- $q_o = Oil production rate, STB/day$
- $q_l = Liquid$  production rate, STB/day

WC = Water cut

 $G = Gravitational acceleration ft/s^2$ 

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