

**Study on CO<sub>2</sub> Removal by Benfield Solution Using FEMLAB**

By

ANA FARALIZA BT MOHAMED PUAD

Dissertation submitted in partial fulfillment of  
the requirement for the  
Bachelor of Engineering (Hons)  
(Chemical Engineering)

JANUARY 2005

**Universiti Teknologi PETRONAS**  
**Bandar Seri Iskandar**  
**31750 Tronoh**  
**Perak Darul Ridzuan**

PUSAT SUMBER MAKLUMAT  
UNIVERSITI TEKNOLOGI PETRONAS

UNIVERSITI TEKNOLOGI PETRONAS  
Information Resource Center



IPB184365

6

TP

245

. 04

A532

2005

10 Carbon, Activated  
20 Adsorption

## **CERTIFICATE OF APPROVAL**

**Study on CO<sub>2</sub> Removal by Benfield Solution Using FEMLAB**

by

**ANA FARALIZA BT MOHAMED PUAD**

A project dissertation submitted to the

Chemical Engineering Programme

Universiti Teknologi PETRONAS

In partial fulfillment of the requirement for the

BACHELOR OF ENGINEERING (Hons)

(CHEMICAL ENGINEERING)

Approved by,



(Dr. Suzana Yusup)

Supervisor

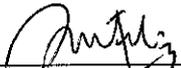
UNIVERSITI TEKNOLOGI PETRONAS

TRONOH, PERAK

JANUARY 2005

## **CERTIFICATION OF ORIGINALITY**

This is to certify that I am responsible for the work submitted in this project, that the original work is my own except as specified in the references and acknowledgements, and that the original work contained herein have not been undertaken or done by unspecified source or persons.

  
\_\_\_\_\_  
ANA FARALIZA MOHAMED PUAD

## TABLE OF CONTENTS

<b>CERTIFICATE OF APPROVAL.....</b>	<b>I</b>
<b>CERTIFICATE OF ORIGINALITY.....</b>	<b>II</b>
<b>ABSTRACT.....</b>	<b>III</b>
<b>ACKNOWLEDGEMENT.....</b>	<b>IV</b>
<b>NOMENCLATURE.....</b>	<b>V</b>
<b>LIST OF FIGURES.....</b>	<b>VI</b>
<b>LIST OF TABLES.....</b>	<b>VII</b>
<b>CHAPTER 1: INTRODUCTION</b>	
1.1 Background of Study.....	1
1.2 Problem Statement.....	2
1.3 Objectives.....	2
1.4 Scope of Work.....	3
1.4.1 Relevancy of the project	3
<b>CHAPTER 2: LITERATURE REVIEW AND THEORY</b>	
2.1 Gas Treating Process.....	4
2.2 Fundamentals of Chemical Solvent.....	5
2.3 Fundamental of Chemical Reaction.....	5
2.4 Reaction Kinetics.....	6
2.5 Mass Transfer.....	9

<b>CHAPTER 3: METHODOLOGY</b>	
3.1 Simulation Strategy and Model Development.....	11
3.1.1 Transport Phenomena Equations.....	11
3.1.2 Chemical Reaction Equations.....	13
3.1.3 FEMLAB Modelling.....	15
<b>CHAPTER 4: RESULTS AND DISCUSSION</b>	
4.1 FEMLAB Program.....	16
4.2 Discussion.....	18
4.2.1 Effect of Liquid Temperature.....	18
4.2.2 Effect of Potassium Carbonate Concentration.....	20
4.2.3 Effect of Promoter Concentration.....	22
4.2.4 Effect of Gas Mass Transfer Coefficient.....	24
<b>CHAPTER 5: CONCLUSION AND RECOMMENDATIONS.....</b>	
5.1 Conclusion.....	26
5.2 Recommendations.....	27
<b>REFERENCES.....</b>	28
<b>APPENDICES.....</b>	30

## ABSTRACT

The main objective of this project is to study CO<sub>2</sub> removal by Benfield solution at various process conditions ie: at various temperature and concentration of lean Benfield solution, at different concentration of diethanolamine (DEA) and at different value of gas mass transfer coefficient,  $K_{gCO_2}$ .

Scope of study includes identification of general process description of Benfield absorption system and chemical reactions involved, development of transport phenomena equation that describes Benfield absorption system in mathematical form. Then the required coefficient values are searched through literature review. Followed by modelling using FEMLAB and documentation of FEMLAB output. Finally the results were analyzed and justified with existing studies.

At different temperature of lean Benfield, the rate of CO<sub>2</sub> absorption is increased initially, but further increment of temperature caused less CO<sub>2</sub> to be absorbed. Thus for temperature 333K, 343K and 353K the optimum temperature for this system is found at 343K. The effect of gas mass transfer coefficient,  $K_{gCO_2}$  to amount of CO<sub>2</sub> absorption in Benfield solution is inversely proportional. At various concentration of potassium carbonate which are 0.0001 mol/m<sup>3</sup>, 0.02 mol/m<sup>3</sup> and 0.06 mol/m<sup>3</sup> the most efficient of CO<sub>2</sub> absorption occurred at 0.02 mol/m<sup>3</sup>. The different in concentration of Amine did not affect the system. From the results obtained it can be concluded that the absorption is limited by the resistance to diffusion and finite velocity of the reaction.

## **ACKNOWLEDGMENT**

I would like to express my greatest gratitude to my supervisor, Dr Suzana Yusup for her guidance and readiness to assist throughout the project. I would also like to thank to Dr.Shahidah Mohd Shariff, En. Ariffin Marzuki, En.Shahrul Azman Zainal Abidin and the Process Technology Group of PETRONAS Research & Scientific Services for giving me the opportunity to gain experience and knowledge which is a great assistance in this project throughout my Industrial Internship Programme. My gratitude goes to Final Year Research Project coordinators, Universiti Teknologi PETRONAS (UTP), lecturers and technicians involved in this project. Last but not least, to my beloved parents En.Mohamed Puad bin Yahya and Pn.Jamalia bt Harun and family for their endless support and motivation in any field that I am involved in. Thank you and may Allah bless all of you.

## NOMENCLATURE

<b><math>D_i</math></b>	Diffusivity of component $i$ in Potassium Carbonate solution ( $m^2/h$ )
<b><math>K</math></b>	pseudo first order rate constant ( $h^{-1}$ )
<b><math>k_{AM}</math></b>	second order rate constant of amine ( $m^3/kmol h$ )
<b><math>k_{OH}</math></b>	forward reaction rate constant of reaction ( $m^3/kmol s$ )
<b><math>k_{OH}</math></b>	backward reaction rate constant of reaction ( $s^{-1}$ )
<b><math>k_g</math></b>	gas side mass transfer coefficient ( $kmol/h m^2 atm$ )
<b><math>K_g</math></b>	overall mass transfer coefficient ( $kmol h^{-1} m^{-2} atm^{-1}$ )
<b><math>K_1</math></b>	first ionization constant for carbonic acid ( $kmol/m^3$ )
<b><math>K_2</math></b>	second ionization constant for carbonic acid ( $kmol/m^3$ )
<b><math>T</math></b>	gas temperature (K)
<b><math>t</math></b>	liquid temperature (K)
<b><math>N_i</math></b>	mass transfer flux of $i$ component ( $kmol/m^2 h$ )
<b><math>C_i</math></b>	Concentration of $i$ species ( $mol/m^3$ )

## LIST OF FIGURES

**Figure 3.1.3:** Step by Step of FEMLAB Modelling.

**Figure 4.1.1a:** Concentration profile of CO<sub>2</sub> absorbed at 343K.

**Figure 4.1.1b:** Concentration profile of CO<sub>2</sub> absorbed at 333K.

**Figure 4.1.1c:** Concentration profile of CO<sub>2</sub> absorbed at 353K.

**Figure 4.1.2a:** Concentration profile of CO<sub>2</sub> absorbed at  $K_{gCO_2} = 0.5 \text{ mol.h}^{-1}\text{m}^{-2}\text{atm}^{-1}$

**Figure 4.1.2b:** Concentration profile of CO<sub>2</sub> absorbed at  $K_{gCO_2} = 0.7 \text{ mol.h}^{-1}\text{m}^{-2}\text{atm}^{-1}$

**Figure 4.1.2c:** Concentration profile of CO<sub>2</sub> absorbed at  $K_{gCO_2} = 0.3 \text{ mol.h}^{-1}\text{m}^{-2}\text{atm}^{-1}$

**Figure 4.1.3a:** Concentration profile of CO<sub>2</sub> absorbed at Concentration of CO<sub>3</sub><sup>2-</sup> = 0.02mol/m<sup>3</sup>.

**Figure 4.1.3b:** Concentration profile of CO<sub>2</sub> absorbed at Concentration of CO<sub>3</sub><sup>2-</sup> = 0.0001 mol/m<sup>3</sup>.

**Figure 4.1.3c:** Concentration profile of CO<sub>2</sub> absorbed at Concentration of CO<sub>3</sub><sup>2-</sup> = 0.06 mol/m<sup>3</sup>.

**Figure 4.1.4a:** Concentration profile of CO<sub>2</sub> absorbed at Concentration of DEA<sup>-</sup> = 0.002 mol/m<sup>3</sup>.

**Figure 4.1.4b:** Concentration profile of CO<sub>2</sub> absorbed at Concentration of DEA = 0.00001 mol/m<sup>3</sup>.

**Figure 4.1.4c:** Concentration profile of CO<sub>2</sub> absorbed at Concentration of DEA = 0.001 mol/m<sup>3</sup>.

**Figure 4.2.1:** Effect of Liquid Temperature to the Concentration of CO<sub>2</sub> at Top of the Column.

**Figure 4.2.2:** Effect of Carbonate Ion Concentration to the CO<sub>2</sub> Concentration at the Top Outlet of the Column.

**Figure 4.2.3:** Effect of Amine Concentration to the CO<sub>2</sub> Concentration at Top of the Column.

**Figure 4.2.4:** Effect of Gas Mass Transfer Coefficient ( $K_{gCO_2}$ ) to the Concentration of CO<sub>2</sub> at Top of the Column.

## **LIST OF TABLES**

<b>Table 3.1.1</b>	Modelled Chemical Species
<b>Table 3.1.2</b>	Reaction Rate Expression for Modelled Chemical Species
<b>Table 4.1</b>	Program Input Data

# CHAPTER 1

## INTRODUCTION

### 1.1 PROJECT BACKGROUND

Control of Carbon Dioxide (CO<sub>2</sub>) in hydrocarbon gas from the gas wells is important because of the long distances the gas pipelines run to the customers. Significant levels of CO<sub>2</sub> add cost to the compression and transport of the gas. CO<sub>2</sub> also causes problems by lowering the hydrate icing temperature of the gas causing major potential problems in its compression.

One particular CO<sub>2</sub> removal process technology is the Benfield Process, which uses potassium bicarbonate to remove the CO<sub>2</sub> in the form of potassium carbonate. Benfield process or also known as hot carbonated process was originally developed by Benson et al. [1], and has since undergone several improvement [2-4]. The most important improvement is the discovery that small amount of certain organic additives (promoters) can enhance the absorption rate largely [5].

Benfield solution is a mixture of 30% potassium carbonate solution, is dosed with 3% DEA (Diethyl Amine) and up to 200 ppm of antifoam, to improve solution characteristics, with 0.5% of Vanadium Pentoxide to inhibit corrosion. [18]

## 1.2 PROBLEM STATEMENT

In Hysys Steady State Simulation, the Benfield model for PETRONAS Gas Processing Plant-3 (GPP3) can not be developed accurately because of the limiting factor in the property package. The published information investigated the modeling and simulation of Benfield process is very little. In this project, further study was done in order to identify the effect of different parameters on the performance of the absorption system using FEMLAB. General model of CO<sub>2</sub> absorption by Benfield solution in falling film that investigated the combination effect of mass transfer and chemical reaction has been developed.

## 1.3 OBJECTIVE

The objective of this project is to study the CO<sub>2</sub> absorption from natural gas at various operating condition of Benfield solution. The study will focus on the effect of CO<sub>2</sub> exit concentration profile:

- i. At various temperature in the range of 333K to 353K and concentration of Benfield solution in the range of 0.0001 mol/m<sup>3</sup> to 0.06 mol/m<sup>3</sup>.
- ii. At various concentration of DEA in the range of 0.00001mol/m<sup>3</sup> to 0.002mol/m<sup>3</sup> in Benfield solution.
- iii. At different value of CO<sub>2</sub> gas mass transfer coefficient, KgCO<sub>2</sub> in the range of 0.3 to 0.7 kmol h<sup>-1</sup> m<sup>-2</sup> atm<sup>-1</sup>

## 1.4 SCOPE OF WORK

The scopes of work for this study are as follow:

- Identify general process description of Benfield absorption system and chemical reactions involved.
- Develop the best transport phenomena equation that describe the Benfield absorption system in mathematical form.
- Search on required coefficient value.
- Perform modeling using FEMLAB
- Documentation of FEMLAB output.
- Results analysis and justification with existing studies.

### 1.4.1 Relevancy of the Project

The separation of carbon dioxide from mixtures with other gases is a process of substantial industrial importance. Through modeling, the degree of the effectiveness of Benfield system to remove CO<sub>2</sub> from natural gas can be visualized. Thus, knowing CO<sub>2</sub> level in the gas at various points in a removal train allows large savings in operating costs. Optimization of the operation of each plant would yield CO<sub>2</sub> concentrations within specification but with minimal utilities and raw material usage. In this project, CO<sub>2</sub> absorption process incorporated with chemical reactions are fully integrated with transport phenomena with the aid of Finite Element Modelling.

## **CHAPTER 2**

### **LITERATURE REVIEW**

#### **2.1 Gas Treating Process**

Gas treating process variables such as solvent type and concentration, pressure and circulation can be manipulated to produce specification quality hydrocarbon products. Interest has increased recently in exploring the effects of inlet gas and solvent temperatures as an aid in meeting these specifications. In general, lower temperatures tend to promote absorption of lower molecular weight components based on vapour-liquid equilibrium.

Physical solvents exploit this principle by absorbing acid gases and water at lower temperatures. However, if the reaction is kinetically limited as is the case with CO<sub>2</sub> and Benfield solution, it is impossible to determine how temperature affects the absorption in the absence of additional information. This ambiguity results from the competing phenomena and opposite effect temperature has on reaction rates and solubility [14].

For gas treating, process performance is often defined relative to the ability of a solvent to absorb one component to a greater degree than another. This is often referred to as “selectivity”. For Benfield solution (chemical solvent), selectivity may occur due to reaction kinetics. In this case, selectivity may be dramatically improved by column operating temperature [14].

There is no sharp dividing line between pure physical absorption and absorption controlled by the rate of chemical reaction. Most cases fall in optimum value in which the rate of absorption is limited both by the resistance to diffusion and by finite velocity of the reaction [12].

## **2.2 FUNDAMENTALS OF CHEMICAL SOLVENT**

Chemical solvents use the same premise as physical solvents to absorb the component into solution. However, the chemical solvent now has the ability to change the absorbed component either by causing it to ionize or to transform into another component by chemical reaction involved. In either case, the absorbed component in solution is depleted by this reaction, resulting the ability of the solvent to absorb more of the component from the gas phase. This process continues until chemical and physical equilibrium is reached. Contact time in the absorber might prevent the attainment of equilibrium conditions depending on the rate of the reaction.[14].

## **2.3 FUNDAMENTALS OF CHEMICAL REACTION**

Reactions are governed by equilibrium constants, which are related to the Gibbs free energy. The reaction proceeds to a minimum in the Gibbs free energy. The equilibrium constant is used to determine the concentration of species at equilibrium at a given temperature and an initial feed. Large equilibrium constants results in larger concentrations of the products. Theoretically, more acid gas could be absorbed at higher temperature based solely on the equilibrium constants. However, the chemical reaction of the acid gas is not the only process occurring. The absorption of acid gas is less at higher temperatures for equilibrium processes due to primarily to the decrease in solubility [14].

The rate at which a chemical reaction happens is described by kinetics. If a chemical reaction is kinetically limited, then the reaction may not be necessarily approach equilibrium. A reaction that is thermodynamically possible but for which no reasonably rapid mechanism is available is said to be kinetically limited. The extent to which the

reaction approaches equilibrium depends on the time allowed to react, the temperature and the driving forces or concentrations [14] .

## 2.4 REACTION KINETICS

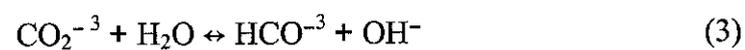
The basic reaction chemistry for aqueous hot potassium carbonate solution and CO<sub>2</sub> is represented by the following reversible reaction [8]:



Since potassium carbonate and bicarbonate are both strong electrolytes, it may be assumed that the metal is present only in the form of K<sup>+</sup> ions, so reaction (1) may be more realistically represented in the ionic terms as:



The above reaction is evidently made up of a sequence of elementary steps. The carbonate ion first reacts with water to generate hydroxyl ions, which then react with CO<sub>2</sub> as follows [8]:



Since reaction (3) is instantaneous reaction, reaction (4) is the rate-controlling step, so that the rate equation for reaction of carbon dioxide with un-promoted hot potassium carbonate leads to [8,14]:

$$r_{OH} = k_{OH}[OH^-][CO_2] - k_{-OH}[HCO_3^-] \quad (5)$$

where  $k_{OH}$  and  $k_{-OH}$  are forward and backward rate constants of reaction (4). At equilibrium condition Eq. (5) gives:

$$k_{-OH}[HCO_3^-] = k_{OH}[OH^-][CO_2]_e \quad (6)$$

where  $[CO_2]_e$  is the equilibrium concentration of  $CO_2$ . The expression for reverse reaction (4) in Eq. (6) has been evaluated by considering conditions at equilibrium, but it is generally true, even when the system is not at equilibrium [14–16]. Substituting Eq. (6) into Eq. (5) gives [14]:

$$r_{OH} = (k_{OH}[OH^-]) ([CO_2] - [CO_2]_e) \quad (7)$$

Carbonate–bicarbonate system is a buffer solution, so the concentration of  $OH^-$  ion in the solution near the surface of liquid is not significantly depleted by the absorbed  $CO_2$ . In this case, the carbon dioxide undergoes a pseudo-first order reaction and Eq. (7) may be rewritten as [8,14,15]:

$$r_{OH} = k_1([CO_2] - [CO_2]_e) \quad (8)$$

where  $k_1$  denotes apparent first-order rate constant.



## 2.5 MASS TRANSFER

The combined effect of chemical reaction presented by Eq. (12) and mass transfer are conveniently and adequately treated by the framework of penetration-surface renewal theory developed by Danckwerts [14]. The absorption rate of carbon dioxide in the liquid phase according to this theory and homogeneous catalysis mechanism can be expressed as follows [14–16]:

$$N_{CO_2} = Ek_L(C_{CO_2i} - C_{CO_2e}) \quad (24)$$

where  $C_{CO_2i}$  is the concentration of carbon dioxide at the interface and  $C_{CO_2e}$  is the equilibrium concentration of unreacted carbon dioxide in the bulk of liquid when the reverse reaction of carbon dioxide is appreciable.  $k_L$  is liquid phase mass transfer coefficient and  $E$  is the enhancement factor and describes the mass transfer coupled by chemical reactions as follows [14]:

$$E = [1 + (Dk/k_L^2)]^{0.5} \quad (25)$$

where  $k$  is defined by Eq. (13). The rate of absorption, which is defined by Eq. (24), can be rewritten in terms of physical solubility of carbon dioxide in solution,  $H$ , in the reactive  $K_2CO_3$  solution as:

$$N_{CO_2} = k_L H E (P_{CO_2i} - P_{CO_2e}) \quad (26)$$

The rate of mass transfer of carbon dioxide in the gas phase is also as follows:

$$N_{CO_2} = k_{gCO_2} (P_{CO_2} - P_{CO_2i}) \quad (27)$$

where  $k_{gCO_2}$  is gas phase mass transfer coefficient of carbon dioxide.

Combining Eqs. (26) and (27) and eliminating the interface partial pressure of carbon dioxide,  $P_{CO_2i}$ , gives rise to the following equation for the absorption rate:

$$\begin{aligned} N_{CO_2} &= [ k_{gCO_2} k_{LEH} / (k_{gCO_2} + k_{LEH}) ] (P_{CO_2} - P_{CO_2e}) \\ &= K_{gCO_2} (P_{CO_2} - P_{CO_2e}) \end{aligned} \quad (28)$$

where  $K_{gCO_2}$  is overall gas phase mass transfer coefficient of carbon dioxide.

## **CHAPTER 3**

### **METHODOLOGY**

#### **3.1 Simulation Strategy and Model Development**

The simulation strategies involve the development of transport phenomena equations, and simplification of chemical reactions equations for the absorption system. The purpose of simulation strategies is to describe the system in mathematical form, which then exported to the FEMLAB programme for model development.

##### **3.1.1 Transport Phenomena Equations**

The model treats a falling film, measuring absorption of CO<sub>2</sub> (g) in Benfield solution. The solution provides the concentration process of 6 species in the system.

Assumptions that made in order to simplify the model are:

- i. Condensation and evaporation of water in the system will not take into account.
- ii. Neglect homogeneous gas reactions
- iii. The flow in liquid phase is laminar
- iv. The radius of the tube is large enough, in comparison to the thickness of the falling film. Thus the effect of curvature in the tube can be neglected.
- v. The contribution of diffusion to the flux of species is negligible in the direction of convective flow i.e. in vertical direction.
- vi. The system is isothermal.

The chemical species that are modelled are tabulated below:

**Table 3.1.1: Modelled Chemical Species**

INDEX (i)	1	2	3	4	5	6
SPECIES	CO <sub>2</sub>	OH <sup>-</sup>	HCO <sub>3</sub> <sup>-</sup>	CO <sub>3</sub> <sup>2-</sup>	DEA	Carbamate

Momentum Balance gives the velocity profile  $v_y$  :

$$v_y = 1.5 v_{av} (1 - (x/\delta)^2)$$

The space coordinate  $x$  is 0 at the gas phase boundary and  $\delta$  at the wall of the tube. The coordinate  $y$  is 0 at the inlet and equal to the length of the tube at the outlet.

For mass balance the general expression for the flux vector of every species:

$$N_i = (-Di \partial c_i / \partial x, c_i v_y) \quad \text{in } \Omega \text{ where } i = 1,2,3,4,5,6$$

Mass balance incorporates with chemical reactions at steady state for the species:

$$N_i - \Sigma R_j = 0 \quad \text{in } \Omega \text{ where } i = 1,2,3,4,5,6$$

The equation above can be expressed in the following form:

$$-Di (\partial^2 c_i / \partial x^2) + v_y (\partial c_i / \partial y) - \Sigma R_j = 0 \quad \text{in } \Omega \text{ where } i = 1,2,3,4,5,6$$

This equation can be rewrite by using the transformation  $y = v_{av} t$ .

This gives the final system of equation in the domain:

$$(1.5 (1 - (x/\delta)^2)) \partial c_i / \partial t - Di (\partial^2 c_i / \partial x^2) - \Sigma R_j = 0 \quad \text{in } \Omega \text{ where } i = 1,2,3,4,5,6$$

This transformation implies that the boundary conditions at  $y=0$  become initial conditions. This gives the following initial conditions:

$$C_i(x,0) = 0$$

$$C_2(x,0) = C_{OH}$$

$$C_3(x,0) = C_{HCO_3^-}$$

$$C_4(x,0) = C_{CO_3^{2-}}$$

$$C_5(x,0) = C_{DEA}$$

$$C_6(x,0) = C_{CARB}$$

The corresponding boundary conditions:

$$-D_i(\partial c_i / \partial x)(0,t) = 0 \quad \text{for } i = 2,3,4,5,6$$

$$-D_1(\partial \theta_1 / \partial x)(0,t) = \text{kg CO}_2 (P_{CO_2} - P_{CO_2eqb})$$

Boundary condition at the tube wall:

$$-D_i(\partial \theta_i / \partial x)(\delta,t) \quad \text{for } i = 1,2,3,4,5,6$$

Which implies that there is no flux of species out of domain at this boundary.

### 3.1.2 Chemical Reactions Equations

In order to observe the concentration distribution of each ion in this system, rate of reactions in equation 2,3,4,9,10 are estimated as follows:

$$k_2, k_3 = k_{OH}$$

$$k_{-2}, k_{-3} = k_{-OH}$$

$$k_4, k_5 = k_{AM}$$

$$k_{-4}, k_{-5} = k_{-AM}$$

By assuming reaction (2) made up of a sequence of elementary steps which is reaction (3) and reaction (4). Reaction (3) is instantaneous reaction and reaction (4) is the rate-controlling step Thus reaction rate constant for reaction (2) is estimated as equal with  $k_{OH}$ . The same goes with reaction rate constant for reaction (3). (for forward reaction)

For Amine- $CO_2$  reaction, it is assumed that reaction (9) is rate-controlling step. Thus, the forward reaction rate constant for equation (9) and equation (10) are approximated equal with  $k_{AM}$ .

Where:

$$\text{Log}(k_{OH}) = (13.635 - (2895/T) + 0.081) / 3600$$

$$k_{AM} = 6.4 \times 10^8 \exp(14.97 \times (1 - (353/T)))$$

$$K1 = k_{OH} / k_{OH}$$

$$K2 = k_{AM} / k_{AM}$$

The reaction rate expressions for every species are tabulated in the Table 3.12.

**Table 3.1.2: Reaction Rate Expression for Modelled Chemical Species**

Species	Reaction Rate expression
$CO_2$	$r_{CO_2} = -k_{OH}[CO_2][OH^-] + k_{OH}[HCO_3^-] - k_{AM}[CO_2][DEA] - k_{AM}[CARB]$
$OH^-$	$r_{OH} = k_{OH}[CO_3^{2-}] - k_{OH}[HCO_3^-][OH^-] - k_{OH}[CO_2][OH^-] + k_{OH}[HCO_3^-] - k_{AM}[CARB][OH^-] + k_{AM}[HCO_3^-][DEA]$
$HCO_3^-$	$r_{HCO_3^-} = k_{OH}[CO_3^{2-}] - k_{OH}[HCO_3^-][OH^-] + k_{OH}[CO_2][OH^-] - k_{OH}[HCO_3^-] + k_{AM}[CARB][OH^-] - k_{AM}[HCO_3^-][DEA]$
$CO_3^{2-}$	$r_{CO_3^{2-}} = -k_{OH}[CO_3^{2-}] + k_{OH}[HCO_3^-][OH^-]$
DEA	$r_{DEA} = -k_{OH}[CO_2][DEA] + k_{AM}[CARB] + k_{AM}[CARB][OH^-] - k_{AM}[HCO_3^-][DEA]$
Carbamate	$r_{CARB} = k_{AM}[CO_2][DEA] - k_{AM}[CARB] - k_{AM}[CARB][OH^-] + k_{AM}[HCO_3^-][DEA]$

### 3.1.3 FEMLAB Modeling

The system is modelled using the FEMLAB Graphical User Interface. The modelling procedures are:

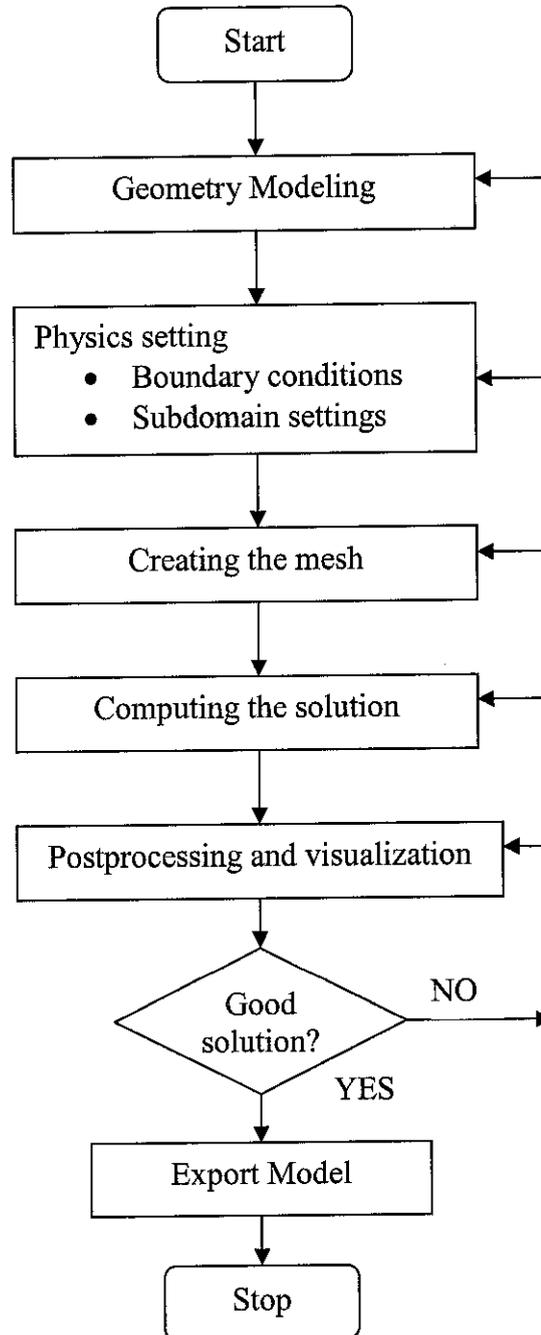


Figure 3.13: Step by Step of FEMLAB Modeling

## **CHAPTER 4**

### **RESULTS AND DISCUSSION**

#### **4.1 FEMLAB Program**

Nine FEMLAB program was run to simulate the CO<sub>2</sub> absorption by Benfield solution. The concentration profiles of CO<sub>2</sub> at the top of the column are observed and will be discussed in this chapter at various temperature and concentration of Benfield solution, at various concentration of DEA and at various value of CO<sub>2</sub> gas mass transfer coefficient,  $K_{gCO_2}$ .

Run 1, Run 2 and Run 3 simulate the system at different temperature which are 343K, 333K and 353K respectively. While Run 3, Run 4 and Run 5 showed the effect of different value of CO<sub>2</sub> mass transfer coefficient,  $K_{gCO_2}$ . The effects of Potassium Carbonate concentration in Benfield solution are simulated in Run 5, Run 6 and Run 7. Finally Run 7, Run 8 and Run 9 simulate the effect of promoter concentration to the absorption system. All of these can be achieved by changing the variable as desired. Table 4.1 shows the input of the program.

Table 4.1: Program Input Data

Variable	RUN1	RUN2	RUN3	RUN4	RUN5	RUN6	RUN7	RUN8	RUN9
T (K)	343	333	353	353	353	353	353	353	353
Vav (m/s)	0.0362	0.0362	0.0362	0.0362	0.0362	0.0362	0.0362	0.0362	0.0362
D1 (m <sup>2</sup> /h)	6.7e-6	5e-9	5e-4						
D2 (m <sup>2</sup> /h)	6.4e-9	6e-12	6e-7						
D3 (m <sup>2</sup> /h)	4.5e-9	4e-12	4e-7						
D4 (m <sup>2</sup> /h)	5e-7	5e-9	3.5e-5						
D5 (m <sup>2</sup> /h)	3.35e-5	4e-8	3.35e-4						
D6 (m <sup>2</sup> /h)	3.35e-5	4e-8	3.35e-4						
K <sub>OH</sub> (s <sup>-1</sup> )	1.9e5	1.05e5	3.27e5						
K <sub>AM</sub> (m <sup>3</sup> /kmol h)	4.14e8	2.6e8	6.4e8						
K <sub>1</sub> (kmol/m <sup>3</sup> )	4.43e-7	5e-7	4.198e-7						
K <sub>2</sub> (kmol/m <sup>3</sup> )	7.46e-11	7.189e-11	7.49e-11						
CCO2 (mol/m <sup>3</sup> )	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
COH (mol/m <sup>3</sup> )	0.02	0.02	0.02	0.02	0.02	0.02	0.02	0.02	0.02
CHCO3 (mol/m <sup>3</sup> )	0	0	0	0	0	0	0	0	0
CCO32 (mol/m <sup>3</sup> )	0.02	0.02	0.02	0.02	0.02	0.02	0.0001	0.06	0.06
DEA (mol/m <sup>3</sup> )	0.002	0.002	0.002	0.002	0.002	0.002	0.002	0.0001	0.001
PCO2 (atm)	0.5	0.5	0.5	0.5	0.5	0.5	0.5	0.5	0.5
PCO2eqb (atm)	0.05	0.05	0.05	0.05	0.05	0.05	0.05	0.05	0.05
K <sub>gco2</sub> (kmol h <sup>-1</sup> m <sup>2</sup> atm <sup>-1</sup> )	0.5	0.5	0.5	0.7	0.3	0.3	0.3	0.3	0.3
Delta (m)	0.1	0.1	0.1	0.1	0.1	0.1	0.1	0.1	0.1

## 4.2 Discussion

### 4.2.1 Effect of Liquid Temperature

Inlet temperature of lean solution has an influence on the absorption performance. The effect of Benfield solution inlet temperature to the concentration of CO<sub>2</sub> at the top of the column can be viewed in Figure 4.2.1. The liquid temperatures are varied at 333K, 343K and 353K. Initially by increasing the temperature, the absorption rate is increased, but further increment of temperature caused less CO<sub>2</sub> to be absorbed.

Clearly observed that the concentration of CO<sub>2</sub> is the smallest which is 0.7mol/m<sup>3</sup> at 343K. Temperature 333K and 353K gives 0.94 mol/m<sup>3</sup> and 0.93 mol/m<sup>3</sup> of CO<sub>2</sub> at the top outlet of the column respectively.

Theoretically, higher mass-transfer performance at lower temperature, which can be presented by decreasing the equilibrium vapour pressure of CO<sub>2</sub> over the portion of solution last contacted by gas. Meanwhile more acid gas could be absorbed at higher temperature, if equilibrium constant is based solely. However, the chemical reaction of the acid gas is not the only process occurring in Benfield absorption system.

### Effect of Liquid Temperature to the Concentration of Co2 at Top of the Column

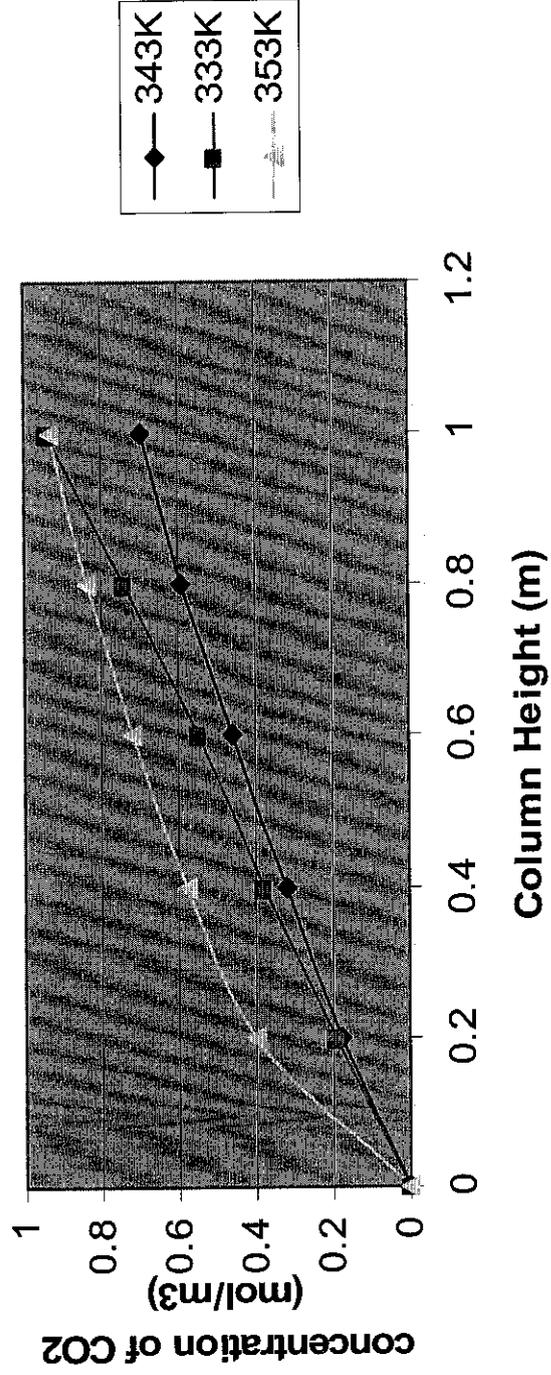


Figure 4.2.1: Effect of Liquid Temperature to the CO<sub>2</sub> Concentration at Top of the Column

#### 4.2.2 Effect of Potassium Carbonate Concentration

In this project, the effect of Potassium Carbonate concentration in Benfield solution are represented by the concentration of carbonate ion ( $\text{CO}_3^{2-}$ ). Three different value of  $\text{CO}_3^{2-}$  concentrations are simulated and the effect to the  $\text{CO}_2$  concentration at top of the column are observed.

The  $\text{CO}_3^{2-}$  concentrations are varied at  $0.02\text{mol/m}^3$ ,  $0.001\text{mol/m}^3$  and  $0.06\text{mol/m}^3$ . The results show that the concentration of  $\text{CO}_2$  is the smallest which is  $0.58\text{mol/m}^3$  at optimum  $\text{CO}_3^{2-}$  concentration,  $0.02\text{mol/m}^3$ .  $\text{CO}_3^{2-}$  concentration  $0.001\text{mol/m}^3$  and  $0.006\text{mol/m}^3$  gives  $0.94\text{ mole/m}^3$  and  $0.93\text{ mol/m}^3$  of  $\text{CO}_2$  at the top outlet of the column respectively.

Concentration is the driving force for absorption to occur. When the different in concentration of Potassium Carbonate solution with  $\text{CO}_2$  is high, it is predicted that more  $\text{CO}_2$  will be absorbed due to higher solubility of  $\text{CO}_2$ . The mass transfer is not the only process occurring. The absorption in Benfield system is dramatic between chemical reactions involved and the mass transfer. Thus, it can be concluded that the absorption will be efficient at optimum value of Potassium Carbonate concentration.

## Effect of Carbonate Ion Concentration to the CO<sub>2</sub> Top Outlet Concentration

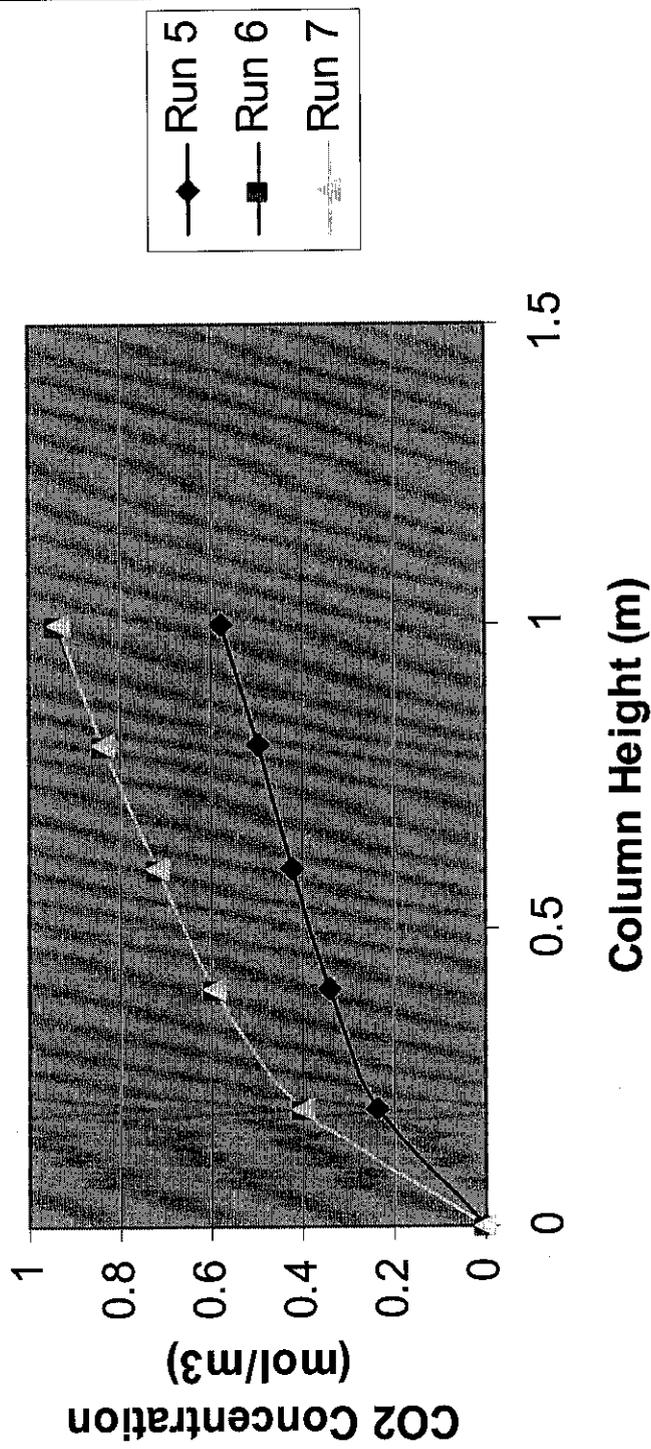


Figure 4.2.2: Effect of Carbonate Ion Concentration to the CO<sub>2</sub> Concentration at the Top Outlet of the Column

### 4.2.3 Effect of Promoter Concentration

Figure 4.2.3 shows that the changes in Amine concentration did not effect the concentration of CO<sub>2</sub> at the top of the column. Theoretically an increase in the amine concentration first induces a higher CO<sub>2</sub> removal while raising the amine content beyond a specific amount has no effect on the exit CO<sub>2</sub> concentration. The possible explanation for this behaviour is that increasing the amine concentration reflects the higher enhancement factor in the liquid phase, which is directly proportional to the overall K<sub>g</sub> in the case of liquid-phase controlled mass transfer. With more increasing the amine concentration, the gas phase mass transfer is considered the major factor controlling the absorption process so the CO<sub>2</sub> removal is unaffected by increasing the amine concentration.

Theoretically water is another component which substantially transported in gas phase across the interface. It may be assumed that there is no liquid-side resistance for the mass transfer of the solvent water vapour. Therefore, the overall mass transfer coefficient for water vapour is the same as the mass transfer coefficient in gas phase. In this project, the term of liquid –phase mass transfer coefficient did not introduced to the simulator. this is because in the model assumptions it already stated that the condensation and evaporation of water in the system did not take into account. This justify why the system did not effected by changing the Amine concentration.

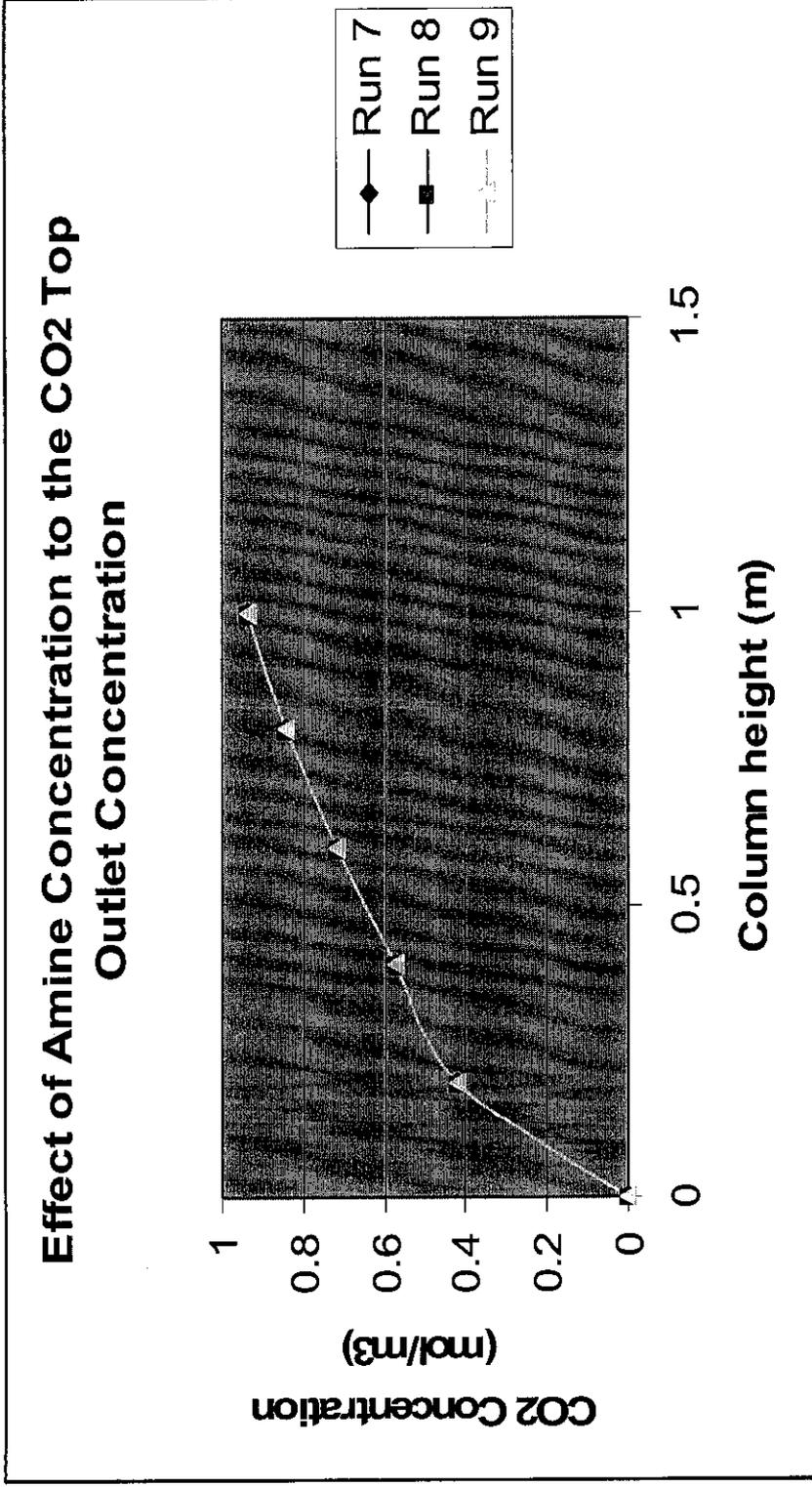


Figure 4.2.3 : Effect of Amine Concentration to the CO<sub>2</sub> Concentration at Top of the Column.

#### 4.2.4 Effect of Gas Mass Transfer Coefficient, $K_g\text{CO}_2$ .

The effect of gas mass transfer coefficient,  $K_g\text{CO}_2$  to the concentration of  $\text{CO}_2$  at the top of the column can be viewed in Figure 4.2.4. The values of  $K_g\text{CO}_2$  are varied at 0.5, 0.7 and 0.3  $\text{mol}\cdot\text{h}^{-1}\cdot\text{m}^{-2}\cdot\text{atm}^{-1}$ . Clearly observed that the concentration of  $\text{CO}_2$  is the smallest which is  $0.58 \text{ mol}/\text{m}^3$  at smallest value of  $K_g\text{CO}_2$ ,  $0.3 \text{ mol}\cdot\text{h}^{-1}\cdot\text{m}^{-2}\cdot\text{atm}^{-1}$ .  $K_g\text{CO}_2$  0.5,  $0.7 \text{ mol}\cdot\text{h}^{-1}\cdot\text{m}^{-2}\cdot\text{atm}^{-1}$  gives  $0.9 \text{ mole}/\text{m}^3$  and  $1.26 \text{ mol}/\text{m}^3$  of  $\text{CO}_2$  at the top outlet of the column respectively. The results showed that as  $K_g\text{CO}_2$  value is decreased, the absorption of  $\text{CO}_2$  will be efficient.

### Effect of Gas Mass Transfer Coefficient ( $K_gCO_2$ ) to the Concentration of $CO_2$ at Top of the Column

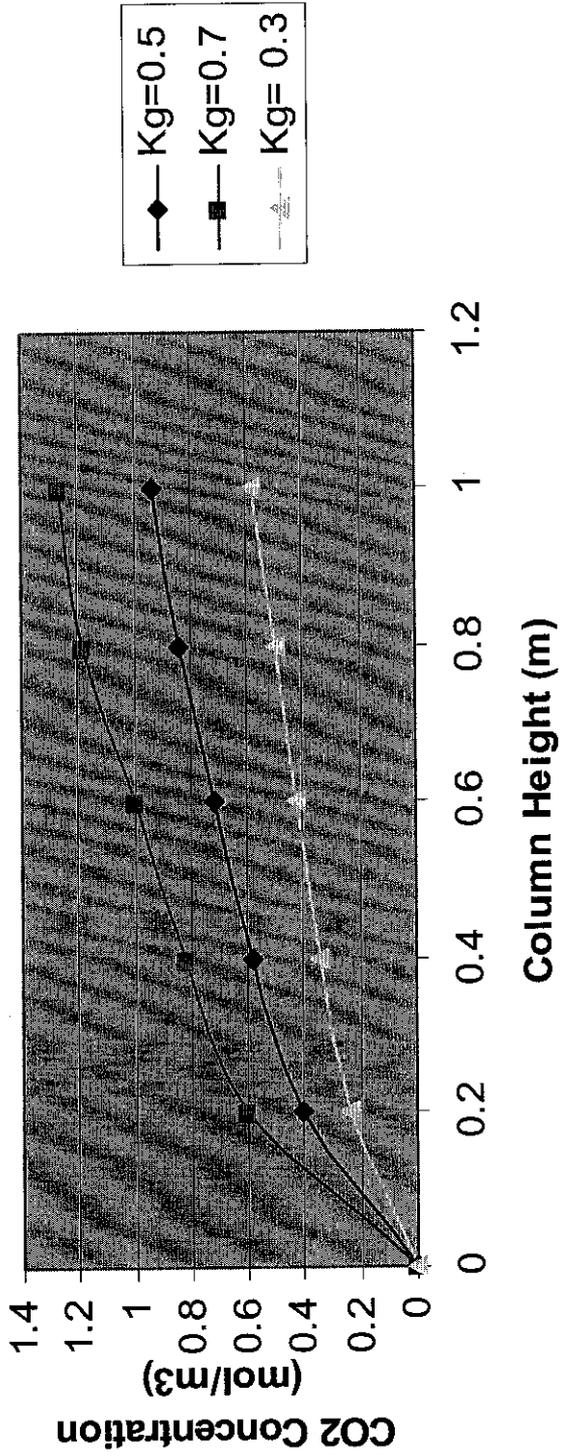


Figure 4.2.4: Effect of Gas Mass Transfer Coefficient ( $K_{gCO_2}$ ) to the Concentration of  $CO_2$  at Top of the Column.

## **CHAPTER 5**

### **CONCLUSION AND RECOMMENDATIONS**

#### **5.1 CONCLUSION**

This study has been conducted due to very little detailed of published information that investigated the modelling and simulation of Benfield absorption system. FEMLAB model of CO<sub>2</sub> absorption by Benfield solution in falling film has been developed using mass transport properties and equations of chemical reactions. The model was run at various operating conditions to observe the effect of CO<sub>2</sub> concentration at top outlet of the column.

At different temperature of lean Benfield, the absorption rate of CO<sub>2</sub> is increased initially, but further increment of temperature caused less amount of CO<sub>2</sub> could be absorbed. Thus for temperature 333K, 343K and 353K the optimum temperature for this system is found at 343K.

The effect of gas mass transfer coefficient,  $K_{gCO_2}$  to amount of CO<sub>2</sub> absorption in Benfield solution is inversely proportional.

At various concentration of potassium carbonate which are 0.0001 mol/m<sup>3</sup>, 0.02 mol/m<sup>3</sup> and 0.06 mol/m<sup>3</sup> the most efficient of CO<sub>2</sub> absorption occurred at 0.02 mol/m<sup>3</sup>.

The different in concentration of Amine did not affect the system.

From the results obtained it can be concluded that the absorption is limited by the resistance to diffusion and finite velocity of the reaction.

## **5.2 RECOMMENDATIONS**

In order to improve the project, it would be recommended to include the heat balance in the modelling system. In this case study, due to lack of information the heat balance cannot be incorporated in the system. Since this study already provides the fundamentals of Benfield absorption, it is suggested in the next level, focus will be more on estimation of constants value. Due to time constraints the constant values are only approximated.

## **CHAPTER 6**

### **REFERENCES**

- [1] H.E. Benson, J.H. Field, R.M. Jimson, CO<sub>2</sub> Absorption Employing Hot Potassium Carbonate Solution, Chem. Eng. Prog. 50 (1954) 356–364.
- [2] H.E. Benson, J.H. Field, W.P. Haynes, Improved Process for CO<sub>2</sub> Absorption Using Hot Carbonate Solution, Chem. Eng. Prog. 52 (1956) 433–438.
- [3] H.E. Benson, J.H. Field, New data for hot carbonate process, Petrol. Refinery 39 (1960) 127–132.
- [4] H.E. Benson, R.W. Parish, Improved Benfield Process, Hydrol. Process. 53 (4) (1974) 81–88.
- [5] F.C. Riesenfeld, J.F. Mullowney, Giammarco–Vetrocoke Processes, Petrol. Refinery 38 (5) (1959) 161–167.
- [6] G. Astarita, D.W. Savage, Promotion of CO<sub>2</sub> Mass Transfer in Carbonate Solutions, Chem. Eng. Sci. 36 (1981) 581–588.
- [7] P.V. Danckwerts, Gas–Liquid Reactions, McGraw-Hill, 1970.
- [8] P.V. Danckwerts, M.M. Sharma, The Absorption of Carbon Dioxide Into Solutions of Alkalis and Amines, Chem. Eng. 44 (1966) 244–280.

- [9] E. Leder, The absorption of CO<sub>2</sub> Into Chemically Reactive Solutions at High Temperature, Chem. Eng. Sci. 26 (1971) 1381–1390.
- [10] M.R.Rahimpour, A.Z Kashooli, Enhanced Carbon Dioxide Removal by Promoted Hot Potassium Carbonate in a Split-Flow Absorber, Chemical Engineering and Processing 43 (2004) 857-865.
- [11] J.Tim Cullinane, Gary T.Rochelle, Carbon Dioxide Absorption with Aqueous Potassium Carbonate Promoted by Piperizine, Chemical Engineering Science 59 (2004) 3619-3630.
- [12] Robert H.Perry, Don W.Green, Perry's Chemical Engineers' Handbook, Seventh Edition, McGraw Hill (1998) 5\_69-5\_71.
- [13] Octave Levenspiel, Chemical Reaction Engineering, Third Edition, John Wiley & Sons, (1999).
- [14] Kevin Lunsford, Gavin McIntyre, Decreasing Contactor Temperature Could Increase Performance, Bryan Research & Engineering (2001).
- [15] PFK Project, Training Textbook for Ammonia and Methanol Units Operation, Part1, Mitsubishi Heavy Industries, LTD, MCEC. 1998.

## **APPENDICES**

### 4.1.1 Run 1, Run 2 and Run 3 Results

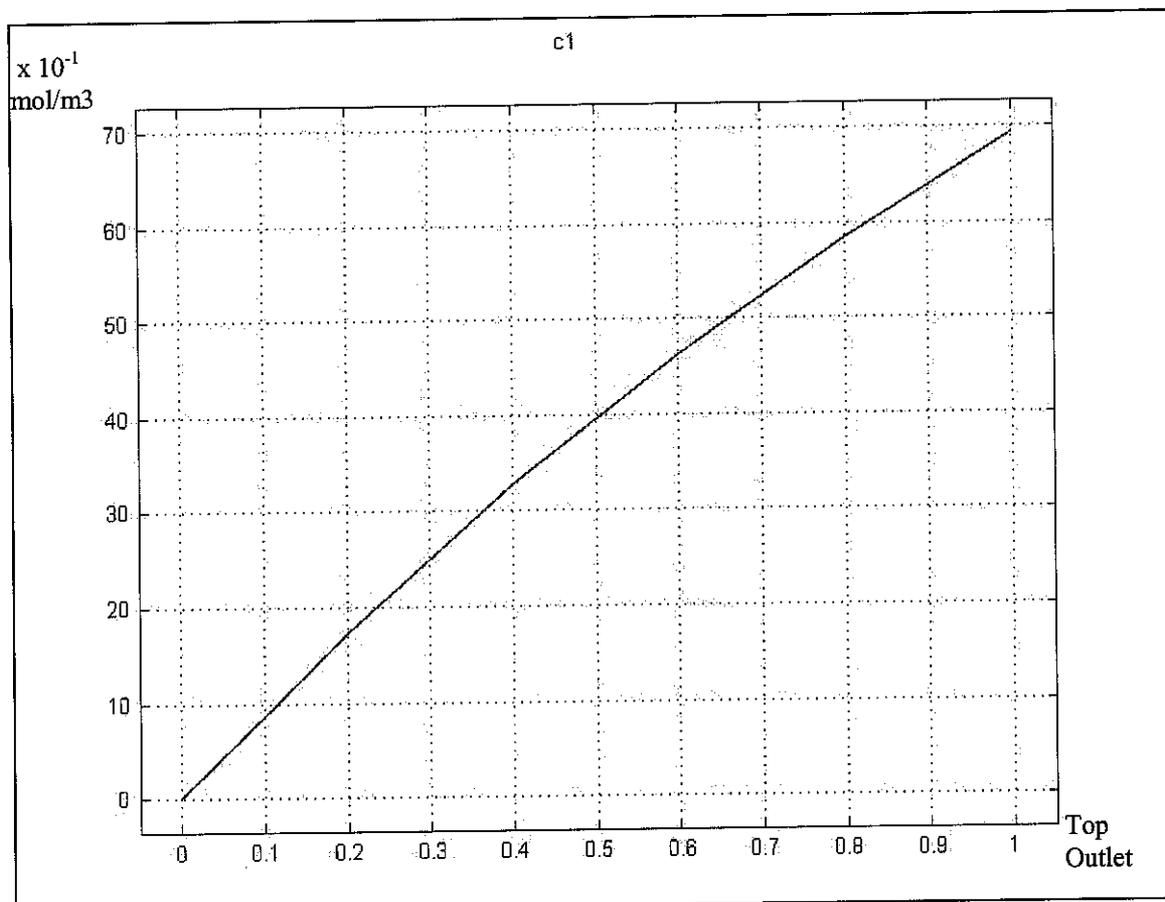


Figure 4.1.1a: Concentration profile of CO<sub>2</sub> absorbed at 343K (Run 1)

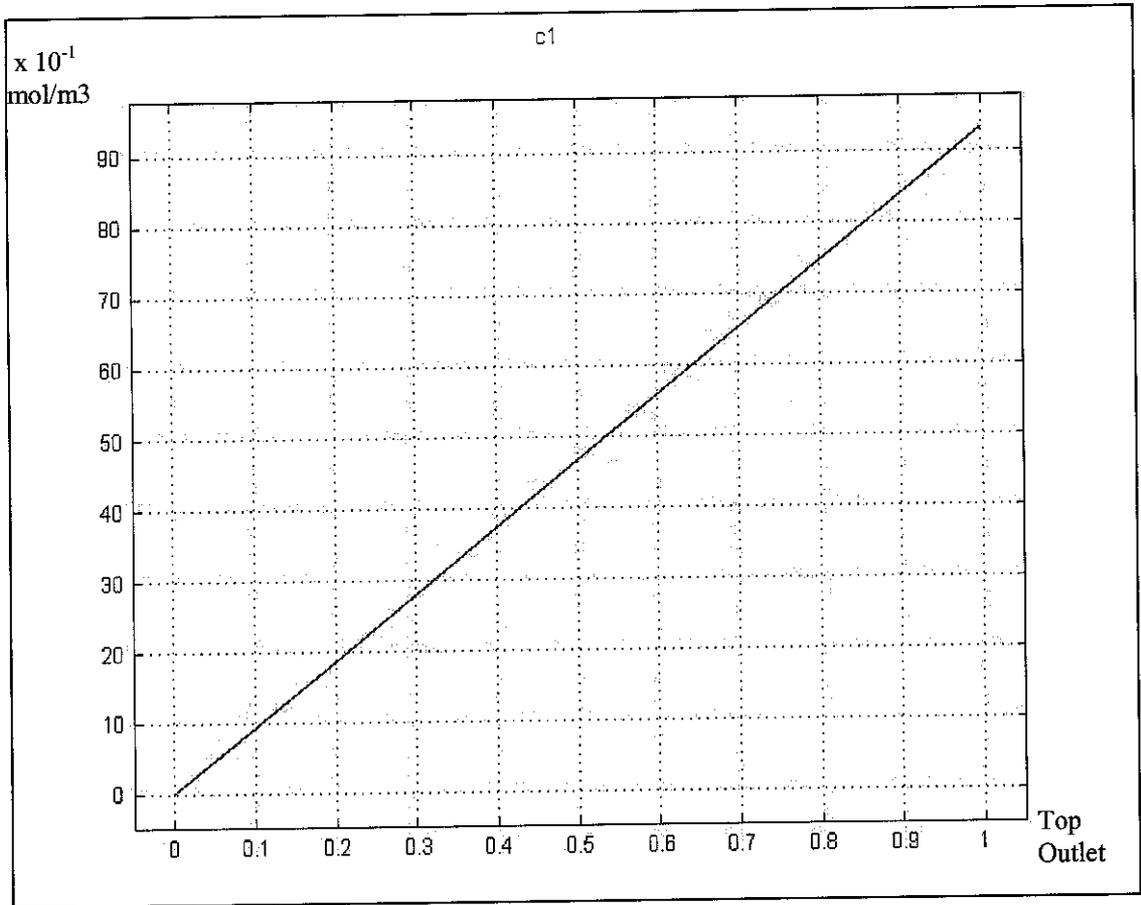


Figure 4.1.1b: Concentration profile of CO<sub>2</sub> absorbed at 333K (Run 2)

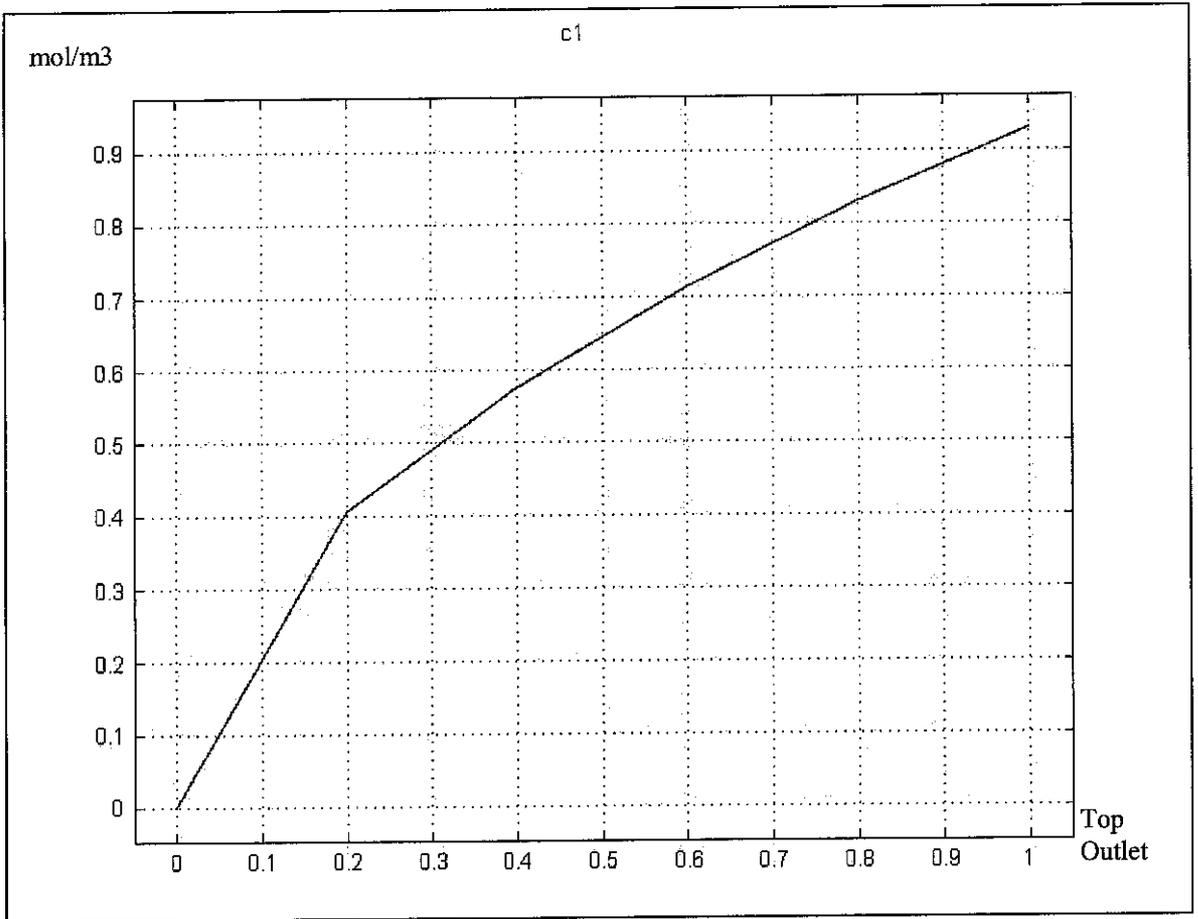


Figure 4.1.1c: Concentration profile of CO<sub>2</sub> absorbed at 353K (Run 3)

#### 4.1.2 Run 3, Run 4 and Run 5 Results

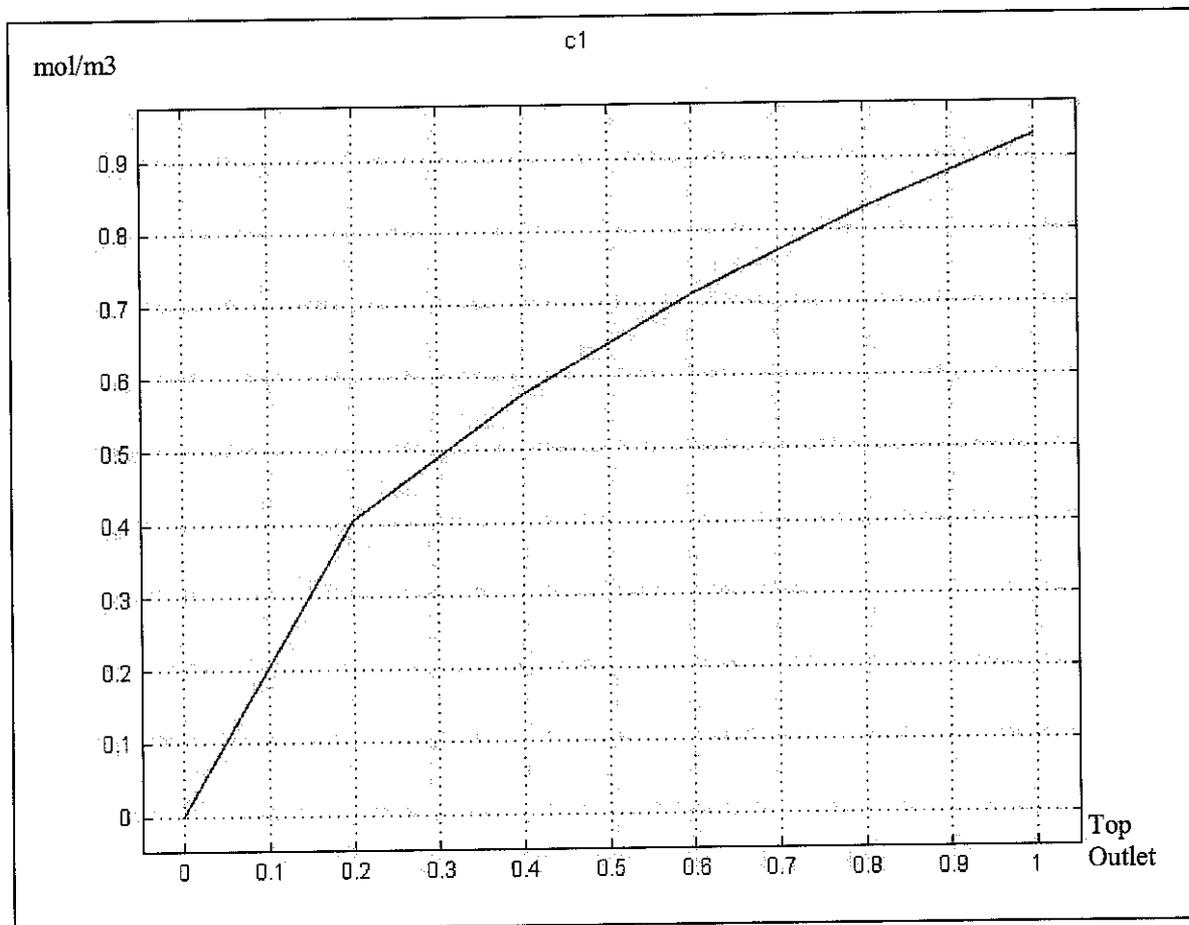


Figure 4.1.2a: Concentration profile of CO<sub>2</sub> absorbed at  $K_{gCO_2} 0.5 \text{ mol.h}^{-1} \text{ m}^{-2} \text{ atm}^{-1}$  (Run 3)

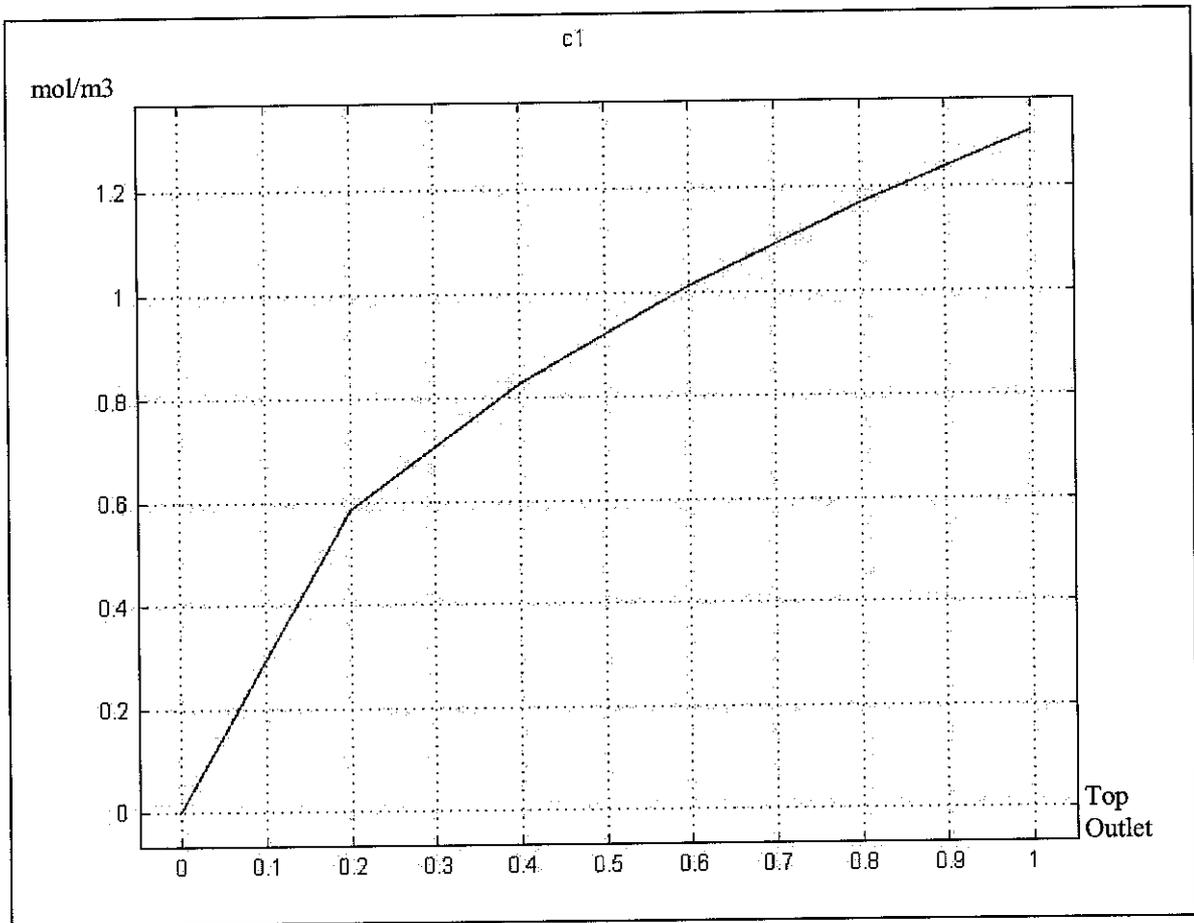


Figure 4.1.2b: Concentration profile of CO<sub>2</sub> absorbed at  $K_{gCO_2} 0.7 \text{ mol.h}^{-1}\text{m}^{-2}\text{atm}^{-1}$   
(Run 4)

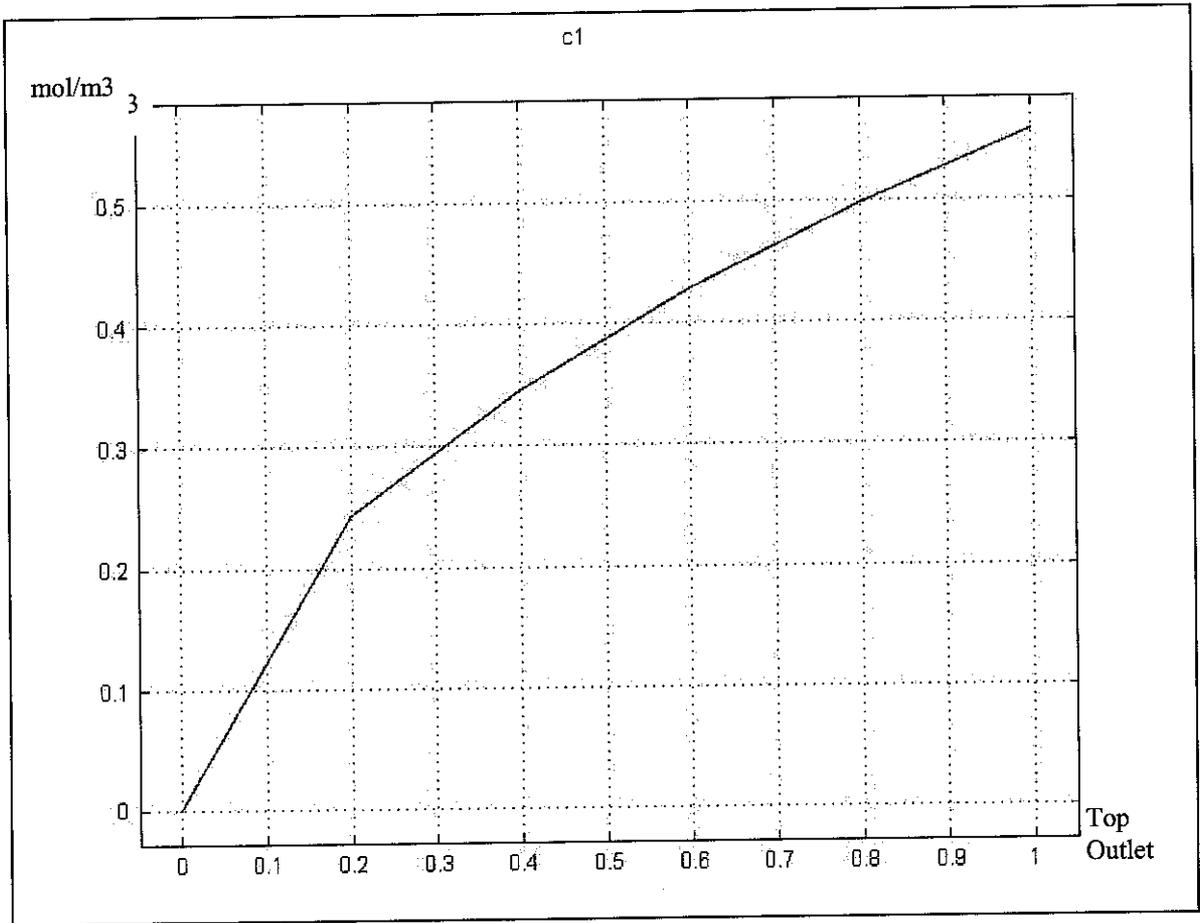


Figure 4.1.2c: Concentration profile of CO<sub>2</sub> absorbed at  $K_{gCO_2}=0.3\text{mol}\cdot\text{h}^{-1}\text{m}^{-2}\text{atm}^{-1}$  (Run 5)

### 4.1.3 Run 5, Run 6 and Run 7 Results

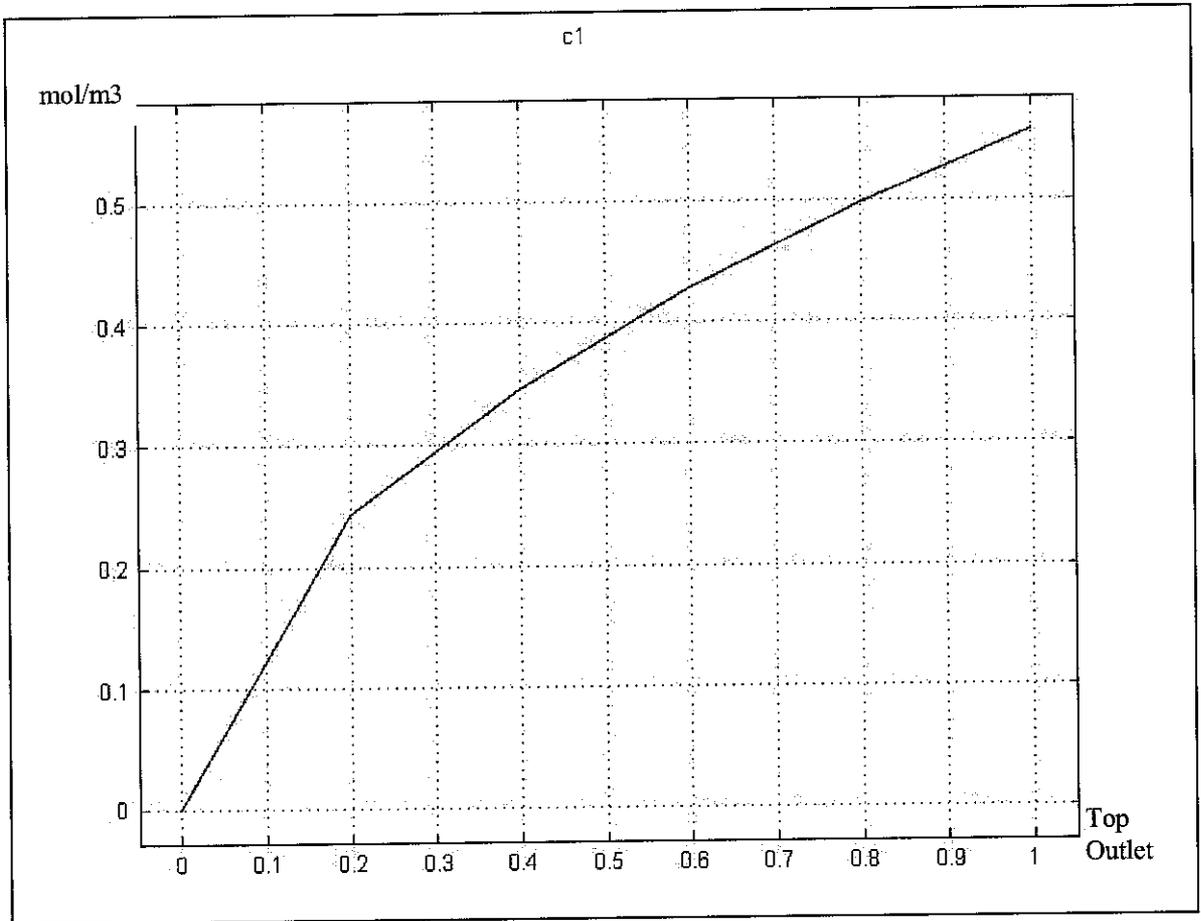


Figure 4.1.3a: Concentration profile of  $\text{CO}_2$  absorbed at Concentration of  $\text{CO}_3^{2-} = 0.02 \text{ mol/m}^3$ . (Run 5)

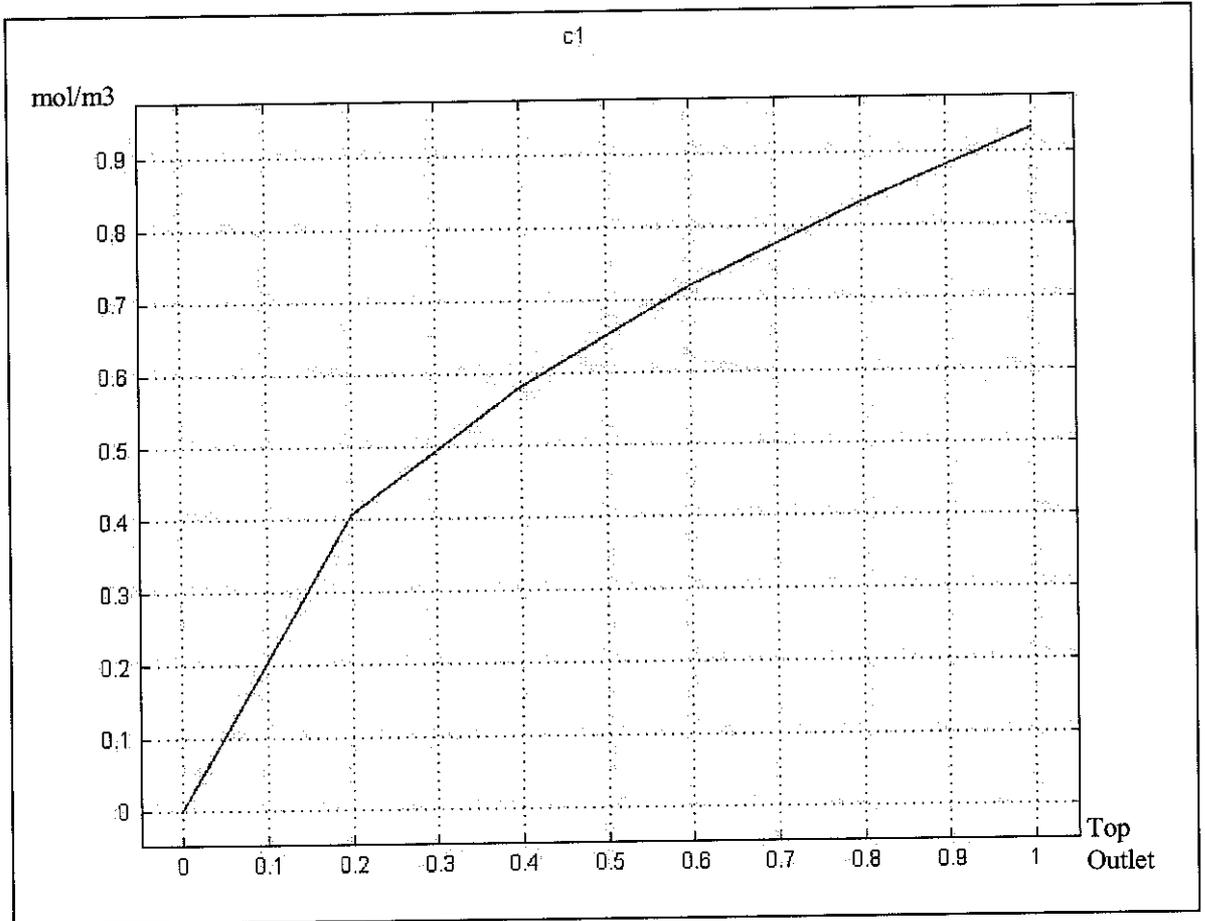


Figure 4.1.3b: Concentration profile of  $\text{CO}_2$  absorbed at Concentration of  $\text{CO}_3^{2-} = 0.0001 \text{ mol/m}^3$ . (Run 6)

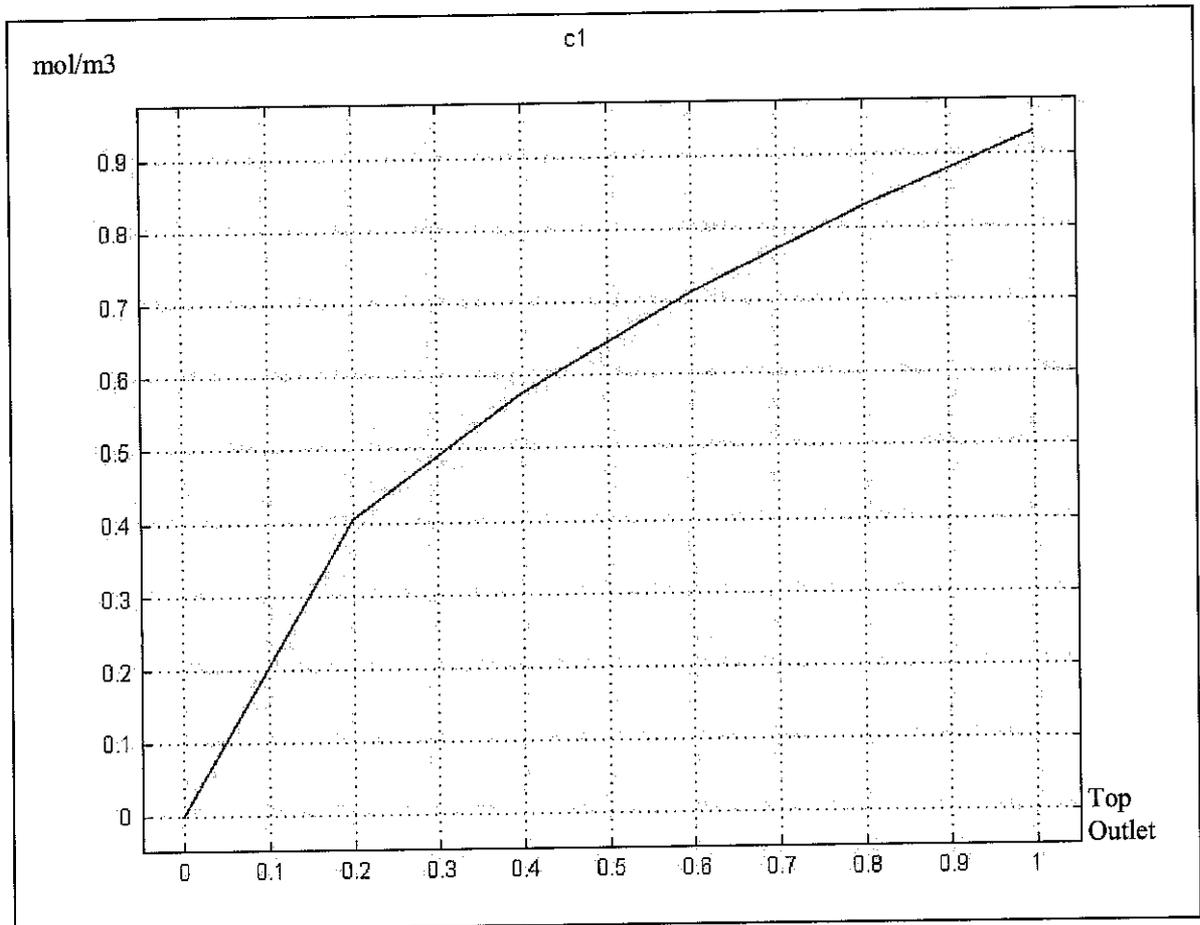


Figure 4.1.3c: Concentration profile of  $\text{CO}_2$  absorbed at Concentration of  $\text{CO}_3^{2-} = 0.06$   $\text{mol/m}^3$ . (Run 7)

#### 4.1.4 Run 7, Run 8 and Run 9 Results

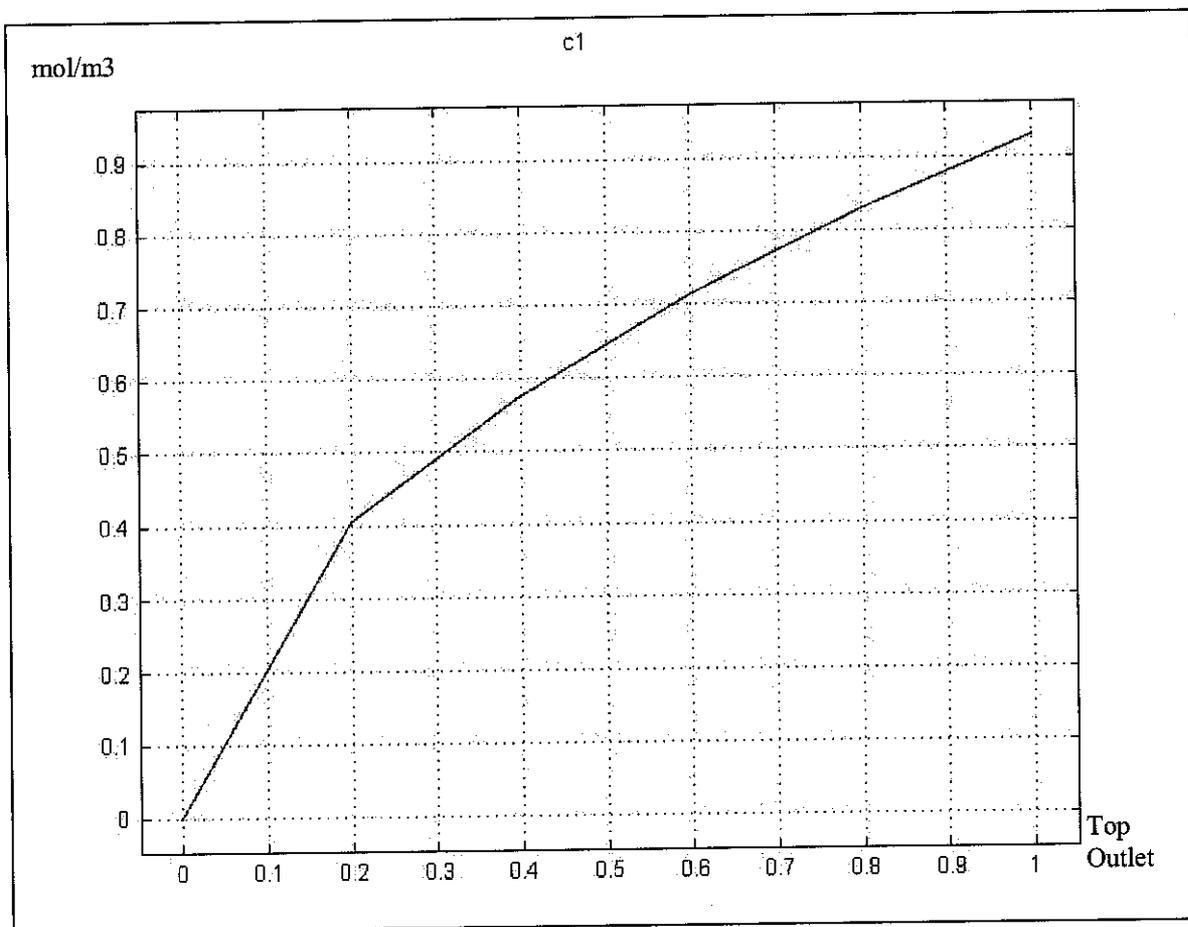


Figure 4.1.4a: Concentration profile of CO<sub>2</sub> absorbed at Concentration of DEA<sup>-</sup> = 0.002mol/m<sup>3</sup>. (Run 7)

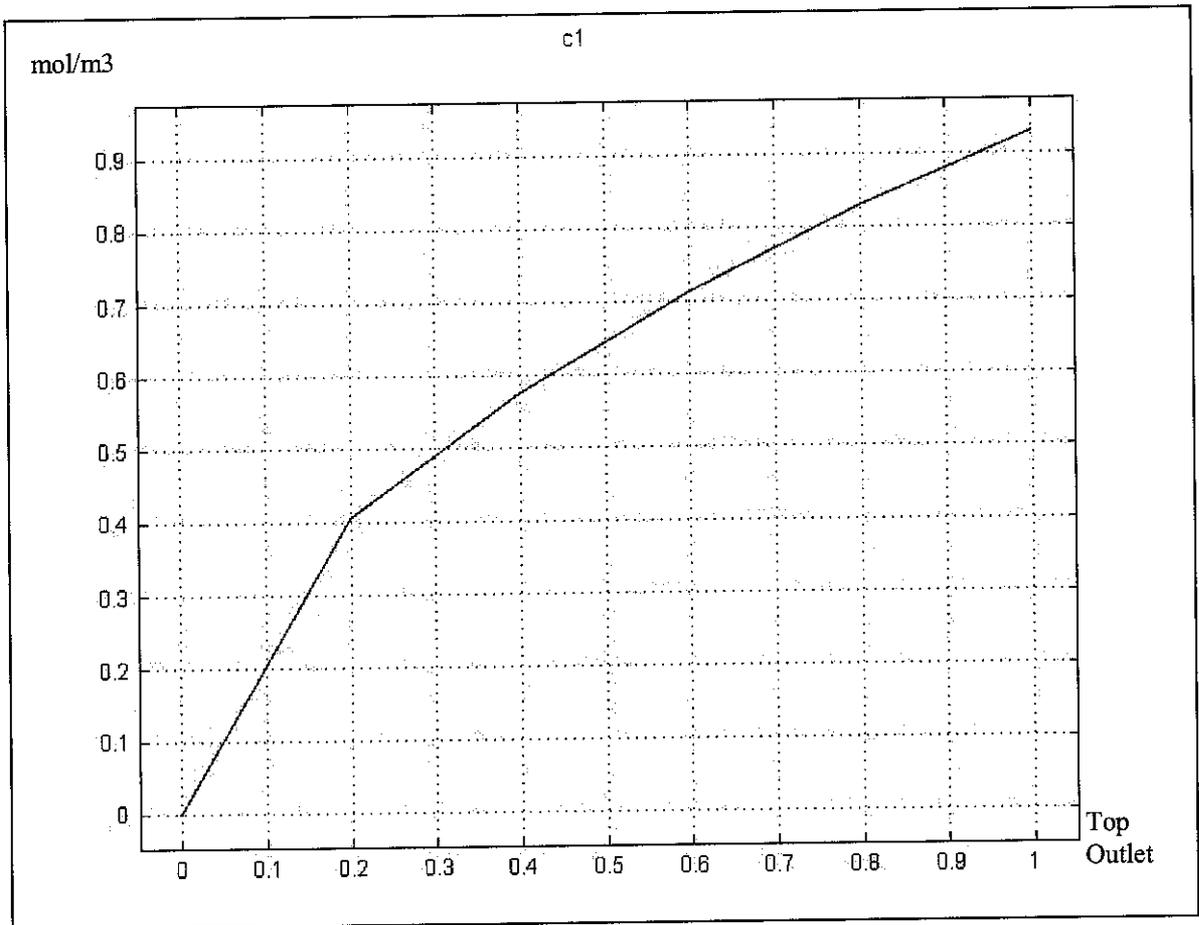


Figure 4.1.4b: Concentration profile of CO<sub>2</sub> absorbed at Concentration of DEA = 0.00001 mol/m<sup>3</sup>. (Run 8)

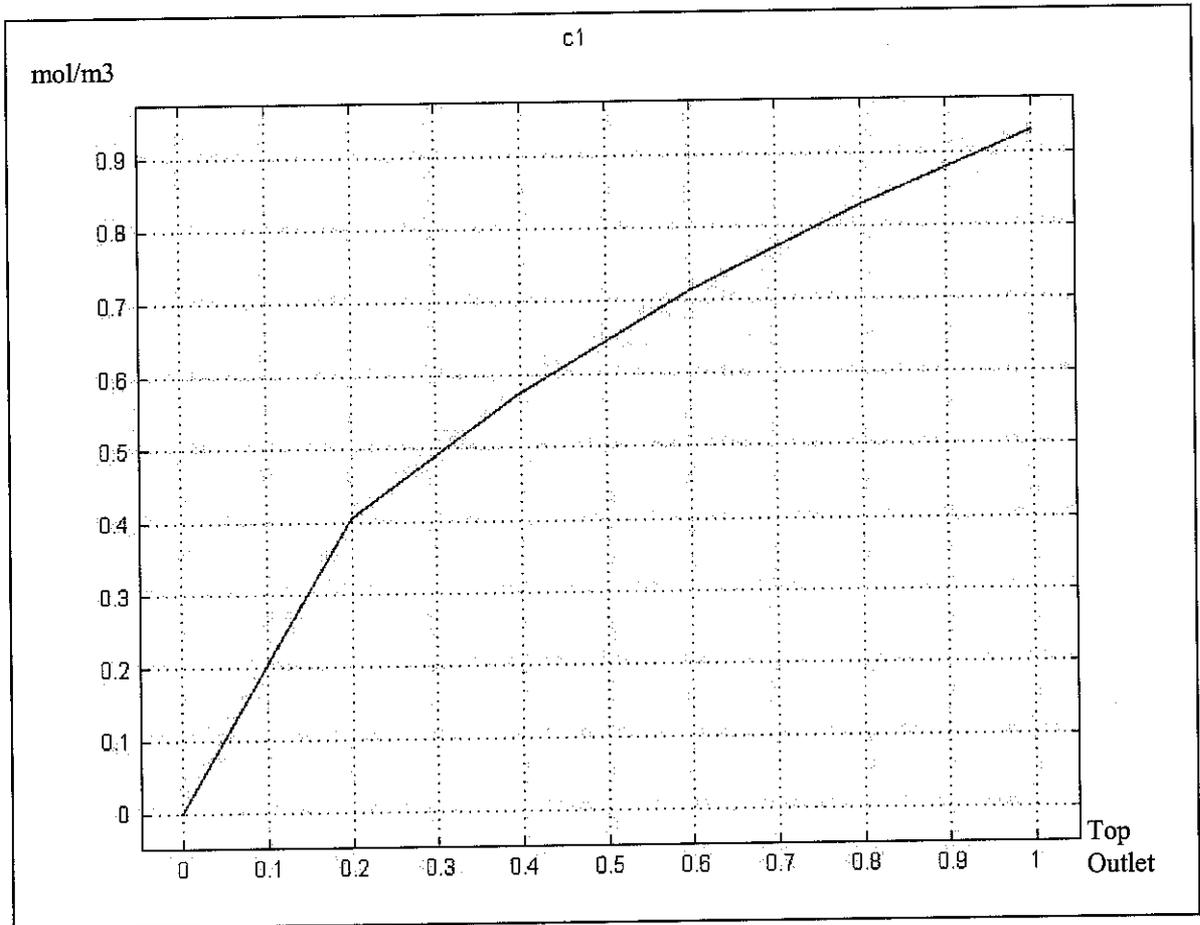


Figure 4.1.4c: Concentration profile of CO<sub>2</sub> absorbed at Concentration of DEA = 0.001 mol/m<sup>3</sup>. (Run 9)

# Carbon dioxide absorption with aqueous potassium carbonate promoted by piperazine

J. Tim Cullinane, Gary T. Rochelle\*

*Department of Chemical Engineering, 1, University Station C0400, The University of Texas at Austin, Austin, TX 78712, USA*

Received 5 August 2002; received in revised form 28 January 2004; accepted 31 March 2004

## Abstract

Many commercial processes for the removal of carbon dioxide from high-pressure gases use aqueous potassium carbonate systems promoted by secondary amines. This paper presents thermodynamic and kinetic data for aqueous potassium carbonate promoted by piperazine. Research has been performed at typical absorber conditions for the removal of CO<sub>2</sub> from flue gas. Piperazine, used as an additive in 20–30 wt% potassium carbonate, was investigated in a wetted-wall column using a concentration of 5 m at 40–80°C. The addition of 0.6 m piperazine to a 20 wt% potassium carbonate system decreases the CO<sub>2</sub> equilibrium partial pressure by approximately 85% at intermediate CO<sub>2</sub> loading. The distribution of piperazine species in the solution was determined by proton NMR. Using the speciation data and relevant equilibrium constants, a model was developed to predict system speciation and equilibrium. The addition of 0.6 m piperazine to 20 wt% potassium carbonate increases the rate of CO<sub>2</sub> absorption by an order of magnitude at 60°C. The rate of CO<sub>2</sub> absorption in the promoted solution compares favorably to that of 5.0 M MEA. The addition of 0.6 m piperazine to 20 wt% potassium carbonate increases the heat of absorption from 3.7 to 10 kcal/mol. The capacity ranges from 0.4 to 0.8 mol-CO<sub>2</sub>/kg-H<sub>2</sub>O for 15 wt% CO<sub>2</sub> solutions, comparing favorably with other amines.  
© 2004 Elsevier Ltd. All rights reserved.

**Keywords:** Absorption; CO<sub>2</sub> removal; Gas treating; Kinetics; Phase equilibria; Separations

## 1. Introduction

The absorption of carbon dioxide with amine or potassium carbonate solvents has gained widespread acceptance for the removal of CO<sub>2</sub> from natural gas and H<sub>2</sub>. Primary and secondary amines react with CO<sub>2</sub> to form amine carbamates. Aqueous primary amine solutions, such as monoethanolamine (MEA), have been shown to have fast reaction rates (Astarita, 1961). While aqueous secondary amines, such as diethanolamine (DEA), are common, their reaction rates have been found to be somewhat slower than primary amines. Numerous investigators have explored the stability and reaction rate of CO<sub>2</sub> in aqueous potassium carbonate (Benson et al., 1954, 1956; Tosh et al., 1959). These studies indicate that potassium carbonate has a low energy of regeneration, but its rate of reaction is slow compared to amines.

Several researchers have shown that the blending of amines accelerates the absorption process (Bosch et al., 1989a; Bishnoi, 2000; Dang, 2001). Likewise, many have investigated amine/potassium carbonate blends with some success (Savage and Sartori, 1984; Tseng et al., 1988; Bosch et al., 1989b).

This work focuses on expanding the investigation of promoted potassium carbonate (K<sub>2</sub>CO<sub>3</sub>) using piperazine (PZ) as the amine. Previous research has indicated that PZ is an effective promoter in methyldiethanolamine (MDEA) and MEA solutions (Bishnoi, 2000; Dang, 2001). Piperazine has a cyclic diamine structure that may favor rapid formation of the carbamates. As a mild base, it may serve to catalyze proton extractions in the reaction mechanism. Also, the molecule can theoretically absorb two moles of CO<sub>2</sub> for every mole of amine. The promoted potassium carbonate is expected to retain its low energy of regeneration, and the reaction of carbonate in the bulk solution is expected to give the solution a high capacity.

This work demonstrates that PZ is an effective promoter in potassium carbonate. The heat of absorption of CO<sub>2</sub> is

\*Corresponding author. Tel.: +1-512-471-7230; fax: +1-512-7824.

E-mail address: rochelle@che.utexas.edu (G.T. Rochelle).

dependent on the relative concentrations of amines and potassium carbonate. NMR indicates that PZ speciation, therefore loading, has a significant effect on absorption. Equilibrium and rate modeling demonstrates the strong dependence of capacity and the apparent rate constant of PZ on potassium concentration. Experiments suggest that PZ performance is competitive with other amine systems.

## Materials and methods

The wetted-wall column, depicted in Fig. 1, was used as a gas–liquid contactor throughout the equilibrium and rate experiments. The contactor is the same equipment used in the work of Bishnoi (2000) and Dang (2001). The stainless steel wetted-wall, measuring 9.1 cm in height and 1.26 cm in diameter, is a tube extending from the liquid feed line inside the column housing. The chemical solution of interest is pumped through the inside of the tube, overflows, and is then distributed across the outer surface of the tube. After collection at the base of the column, the fluid is pumped to a liquid reservoir. Gas enters near the base of the column, counter-currently contacting the fluid as it flows up the gas outlet.

The gas–liquid contact region is enclosed by a 2.54 cm thick-walled glass tube, separating it from an insulating layer of paraffin oil. The outermost region of the column accommodates the circulating bath of paraffin oil in a 1.26 cm OD thick-walled glass annulus.

The chemical solvent was contained in a 1.4 l reservoir connected from a modified calorimetric bomb. A Cole-Parmer micropump pushes the solution from the reservoir through a coil submerged in a heated circulator. After heating, the solution flows into the wetted-wall column. After

contacting the gas stream, the solvent returns to the reservoir, flowing through a rotameter for flowrate determination.

A 20 SLPM mass flow controller was used to meter nitrogen flow. The carbon dioxide flowrate was metered with a 1 SLPM mass flow controller. The metered gases were mixed prior to entering the wetted-wall column and were saturated with water in a calorimetric bomb heated in a water bath. After exiting the contactor, excess water was removed by passing the stream through a condenser. A drying column filled with magnesium perchlorate removed the remaining moisture. A carbon dioxide analyzer was used to measure the CO<sub>2</sub> concentration of the dry gas with infrared spectroscopy.

The inlet gas flowrate and the outlet gas flowrate provide the necessary information to calculate the flux of CO<sub>2</sub> into, or out of, the solvent. The partial pressure of carbon dioxide was varied, giving both absorption and desorption conditions. From this, an equilibrium partial pressure was interpolated.

Liquid samples, taken from the wetted-wall column at steady state conditions, were diluted and injected into a reaction vessel for analysis using an infrared, gas analyzer. The sample was reacted with 30 wt% phosphoric acid, stripping the CO<sub>2</sub> present. A calibration curve was obtained from a known CO<sub>2</sub> source (7 mM Na<sub>2</sub>CO<sub>3</sub>) and the concentration of CO<sub>2</sub> in the liquid samples was calculated. Measurements indicated that measured concentrations of CO<sub>2</sub> matched the nominal amount of CO<sub>2</sub> input into the solution; therefore, the nominal CO<sub>2</sub> concentration was used to define solution loading.

Proton spectra were obtained with a Varian INOVA 500 NMR to determine piperazine speciation in K<sub>2</sub>CO<sub>3</sub>. Characteristic peaks for piperazine, piperazine carbamate, and piperazine dicarbamate were previously determined by <sup>13</sup>C NMR and correlated to <sup>1</sup>H spectra for quantitative interpretation of peak areas (Bishnoi, 2000). In the samples, deuterated water (99.9% purity) was substituted for DI water.

Solutions were prepared with potassium carbonate, potassium bicarbonate or potassium hydroxide, and piperazine. The potassium carbonate, 99.6% pure, and the potassium bicarbonate, 99.9% pure, were purchased from Mallinckrodt. Potassium hydroxide from EM Science was > 85% pure. Anhydrous piperazine of greater than 99% purity was ordered from Aldrich Chemical Company. Solution CO<sub>2</sub> loading was varied using ratios of carbonate and bicarbonate or carbonate and hydroxide.

## 3. Modeling and data representation

### 3.1. Modeling equilibrium

A simple thermodynamic model was developed to predict the equilibrium and speciation in promoted potassium carbonate. This model was adapted from previous modeling work by Bishnoi (2000) and Dang (2001). Representation

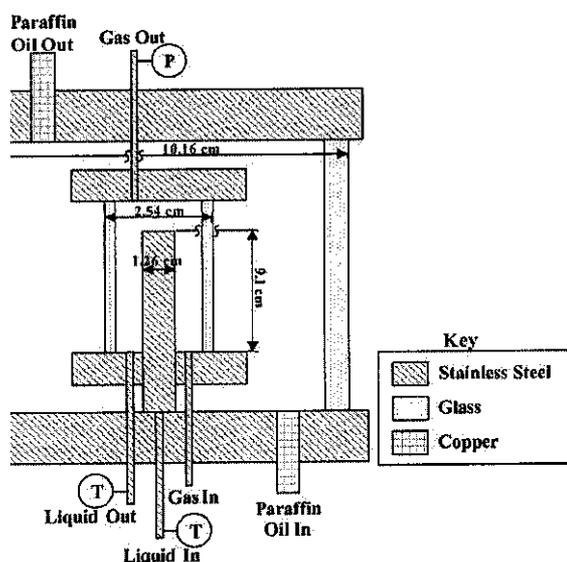
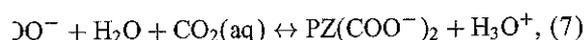
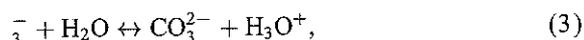
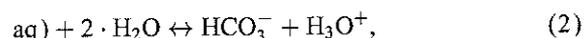


Fig. 1. Schematic of the wetted-wall column.

solution was accomplished using a stand-alone FORTRAN code, which includes the reactions shown below for absorption in PZ promoted  $K_2CO_3$ .



The equilibrium constants for the reactions are shown in Table 1. These reactions, along with total mole balances and charge balance, were used to arrive at an equilibrium ion composition.

Henry's constant for  $CO_2$  in an aqueous solution was calculated using the method of Danckwerts (1970). This method involves ion specific constants describing the solubility of  $CO_2$  in high ionic strength solutions. For the purposes of this work, Henry's constant was calculated for the  $CO_3/KHCO_3$  concentrations; PZ was assumed to have no effect on gas solubility.

Instead of using activity coefficients, equilibrium constants were adjusted to match experimental data with high potassium concentrations. An un-promoted potassium carbonate solution at  $60^\circ C$  was used as a starting point for the model. Adjustments, notated as  $\beta$ , to the equilibrium constants were made such that the new equilibrium constants are reported as

$$K_3^- = \beta \cdot K_{HCO_3^-}, \quad (9)$$

$$K_3^- = \beta^2 \cdot K_{CO_3^{2-}} \quad (10)$$

where  $\beta$ , used in this context, represents an activity coefficient defined by the given reaction. Using a least squares regression of the model predictions,  $\beta$  was altered so that the model fits smoothed  $P_{CO_2}^*$  data at  $60^\circ C$  as extrapolated by Tosh et al. (1959).

For a 20 wt%  $K_2CO_3$  solution, no adjustment was necessary, indicating that the ratio of adjustment factors,  $\beta^2$ :  $\beta$  as in Eqs. (9) and (10), must equal approximately one. The model was also compared to the 30 wt%  $K_2CO_3$  solution investigated by Tosh et al. (1959). The value of  $\beta$ , in this case, was found to be 0.31 demonstrating the large idealities associated concentrated electrolyte solutions.

A similar procedure was followed to match data for the speciation of PZ in the solutions, with each equilibrium constant treated independently (Cullinane, 2002). For a 20 wt%  $K_2CO_3$  solution containing 0.6 m PZ at  $60^\circ C$ , the equilibrium constants were adjusted by matching predictions to NMR speciation data so that

$$K'_{PZCOO^-} = 0.75 \cdot K_{PZCOO^-}, \quad (11)$$

$$K'_{PZ(COO^-)_2} = 0.70 \cdot K_{PZ(COO^-)_2}. \quad (12)$$

The constants regressed allowed relatively accurate VLE modeling for the conditions considered in this work.

### 3.2. Modeling diffusion with chemical reaction

In addition to the equilibrium model, a rate model has been developed to predict the flux of  $CO_2$  into the solvent. Rigorous accounting of equilibrium and mass transfer effects has allowed the estimation of rate constants suitable for describing the observed absorption phenomena.

Mass transfer is an important consideration and must be considered in modeling absorption processes. For the modeling of the boundary layer of  $CO_2$  absorption, Bishnoi (2000) found that the eddy diffusivity theory, shown in Eq. (13) with a pseudo-first order assumption in the reaction term, performed as well as the Higbie penetration theory and the surface renewal theory. With the advantage of being a time-independent equation, this theory was selected for use in modeling in this work. Further details concerning the solution to this equation can be found in Glasscock (1990).

$$\frac{\partial}{\partial x} \left[ (D_{CO_2} + \epsilon x^2) \frac{\partial [CO_2]}{\partial x} \right] - k_1 [CO_2] = 0. \quad (13)$$

Bishnoi (2000) developed a rate model that integrates the ordinary differential equation for eddy diffusivity using multiple nodes across a dimensionless boundary layer. The solution is a function of gas film resistance, liquid film resistance of reactants and products, and bulk solution composition. The model requires an estimation of the diffusion coefficient of reactants and products, but accounts rigorously for gas phase resistance, equilibrium, and kinetics within the gas-liquid interface. The diffusion coefficient was assumed to be that of  $CO_2$  in water and was calculated by the expression given in Versteeg and van Swaaij (1988).

$$D_{CO_2}(m^2/s) = 2.35 \times 10^{-6} \exp\left(\frac{-2119}{T(K)}\right). \quad (14)$$

The model predicts a flux by using a bulk gas phase partial pressure of  $CO_2$  and the bulk solution composition as found by the equilibrium model. The model iteratively solves for an interface partial pressure until a continuous solution is obtained, satisfying the gas film and liquid film resistances. The absorption rates predicted by the model were compared to experimental data. With the use of a non-linear regression package, GREG (Caracotsios, 1986), rate constants were

Equilibrium equations in equilibrium model, mole fraction-based

Equilibrium Constant	ln $K_i = A + B/T + C \ln T$			Source
	A	B	C	
$K_{\text{HCO}_3^-} = \frac{x_{\text{HCO}_3^-} \cdot x_{\text{H}_3\text{O}^+}}{x_{\text{CO}_2} \cdot x_{\text{H}_2\text{O}}}$	231.4	-12092	-36.78	Edwards et al. (1978), Posey (1996)
$K_{\text{CO}_3^{2-}} = \frac{x_{\text{H}_3\text{O}^+} \cdot x_{\text{CO}_3^{2-}}}{x_{\text{HCO}_3^-} \cdot x_{\text{H}_2\text{O}}}$	216.0	-12432	-35.48	Edwards et al. (1978), Posey (1996)
$K_w = \frac{x_{\text{H}_3\text{O}^+} \cdot x_{\text{OH}^-}}{x_{\text{H}_2\text{O}}}$	132.9	-13446	-22.48	Edwards et al. (1978), Posey (1996)
$K_{\text{PZCOO}^-} = \frac{x_{\text{PZCOO}^-} \cdot x_{\text{H}_3\text{O}^+}}{x_{\text{PZ}^+} \cdot x_{\text{CO}_2} \cdot x_{\text{H}_2\text{O}}}$	-29.31	5615	0.0	Bishnoi (2000)
$K_{\text{PZ}^+} = \frac{x_{\text{PZ}^+} \cdot x_{\text{H}_3\text{O}^+}}{x_{\text{PZH}^+} \cdot x_{\text{H}_2\text{O}}}$	-11.91	-4351	0.0	Pagano et al. (1961)
$K_{\text{PZ}(\text{COO}^-)_2} = \frac{x_{\text{PZ}(\text{COO}^-)_2} \cdot x_{\text{H}_3\text{O}^+}}{x_{\text{PZCOO}^-} \cdot x_{\text{CO}_2} \cdot x_{\text{H}_2\text{O}}}$	-30.78	5615	0.0	Bishnoi (2000)
$K_{\text{H}^+\text{PZCOO}^-} = \frac{x_{\text{PZCOO}^-} \cdot x_{\text{H}_3\text{O}^+}}{x_{\text{H}^+\text{PZCOO}^-} \cdot x_{\text{H}_2\text{O}}}$	-8.21	-5286	0.0	Bishnoi (2000)

ted so that a minimum in the least squares error was needed.

In addition to the rigorous rate model, the data was analyzed with the common pseudo-first order assumption. Many amine reactions can be considered first order in CO<sub>2</sub> concentration and first order in amine concentration. Under all conditions, the amine is at a nearly constant concentration across the boundary layer and the reaction rate can be presented by a pseudo-first order rate constant,  $k_1$ , and concentration of CO<sub>2</sub> as in Eq. (13). Under these conditions, the solution for the flux is

$$= \frac{\sqrt{D_{\text{CO}_2} k_{\text{Am}} [\text{Am}]_b}}{H_{\text{CO}_2}} (P_{\text{CO}_2,i} - P_{\text{CO}_2}^*), \quad (15)$$

where the pseudo-first order rate constant is replaced by a constant,  $k_{\text{Am}}$ , and the concentration of the amine in the solution,  $[\text{Am}]_b$ .  $P_{\text{CO}_2,i}$  and  $P_{\text{CO}_2}^*$  represent the partial pressure of CO<sub>2</sub> at the interface and the equilibrium partial pressure of CO<sub>2</sub> in the bulk solution, respectively.

It is important to recognize that the liquid phase driving force must necessarily be small to satisfy the assumption of negligible depletion of amine across the boundary layer. The validity of this assumption was tested by comparing the instantaneous flux to the actual, measured flux. The instantaneous flux can be calculated by

$$= k_{l,\text{prod}} ([\text{CO}_2]_{T,i}^* - [\text{CO}_2]_{T,b}), \quad (16)$$

where  $[\text{CO}_2]_{T,i}^*$  is the concentration of all CO<sub>2</sub> species in equilibrium with the gas phase at the interface,  $[\text{CO}_2]_{T,b}$  is the total CO<sub>2</sub> concentration in the bulk solution, and  $k_{l,\text{prod}}$  is the liquid phase transfer coefficient of the products of

reaction. This was estimated as

$$k_{l,\text{prod}} = k_l \sqrt{\frac{D_{\text{prod}}}{D_{\text{CO}_2}}}, \quad (17)$$

where  $k_l$  is the liquid phase transfer coefficient of CO<sub>2</sub>.  $D_{\text{prod}}$  and  $D_{\text{CO}_2}$  are the diffusion coefficients of products and CO<sub>2</sub>, respectively, whose ratio was estimated as 0.5.

The actual flux is defined similarly; however, the concentration of CO<sub>2</sub> species at the interface,  $[\text{CO}_2]_{T,i}$ , is not in equilibrium with the gas. In this case, flux is represented by

$$N_{\text{act}} = k_{l,\text{prod}} ([\text{CO}_2]_{T,i} - [\text{CO}_2]_{T,b}). \quad (18)$$

A ratio of actual and instantaneous flux, Eq. (19), gives an approach to instantaneous behavior. A small fraction indicates the pseudo-first order approximation is valid.

$$\frac{N_{\text{act}}}{N_{\text{inst}}} = \frac{[\text{CO}_2]_{T,i} - [\text{CO}_2]_{T,b}}{[\text{CO}_2]_{T,i}^* - [\text{CO}_2]_{T,b}}. \quad (19)$$

This analysis was performed on the data in this work to show that most of the data can be represented as pseudo-first order. This is only necessary for simplified representations of the data, not for the rigorous rate model predictions.

### 3.3. Reaction kinetics

In addition to the equilibria defined, modeling the absorption rate requires defining reaction rates important to the absorption mechanism. In this work, Eqs. (2), (5), and (7) were considered with reversible rate expressions. The remaining equations were considered to be in equilibrium.

The reaction mechanism of CO<sub>2</sub> absorption into water consists of the conversion of carbonate to bicarbonate (Eq. (2)). The controlling mechanism, however, is generally

as a reaction of CO<sub>2</sub> with a hydroxyl ion to give a carbonate ion.



rate is well defined and can be predicted using a second order rate constant that is proportional to the hydroxyl concentration and corrected for ionic strength (Astarita et al., 1991).

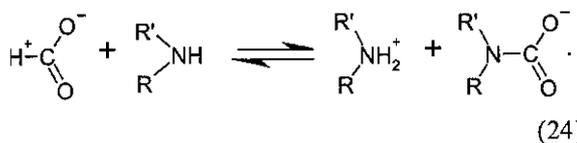
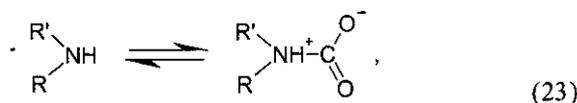
$$k_{\text{OH}^-} = 13.635 - 2895/T + 0.08I \quad (21)$$

the reversible rate defined in terms of concentrations and defined equilibrium constants is

$$r_{\text{OH}^-} = \left( [\text{OH}^-][\text{CO}_2] - \frac{K_{\text{HCO}_3^-}}{K_w} [\text{HCO}_3^-] \right) \quad (22)$$

the rate is considerably slower than the reaction of CO<sub>2</sub> with amines and plays only a minor role in defining CO<sub>2</sub> absorption in amine-based solvents.

The accepted mechanism of amines reacting with CO<sub>2</sub>, the zwitterion mechanism, was proposed by Caplow (1968). In this mechanism, the CO<sub>2</sub> and the amine form a zwitterion intermediate (Eq. (23)). Following formation, the intermediate can be deprotonated by a base, such as the free amine (Eq. (24)) or water.



Using this mechanism, the kinetic expression, as given by Boudart and Kramers (1970), can be expressed as

$$r = \frac{k_f[\text{CO}_2][\text{Am}]}{1 + k_r/\sum k_b[B]} \quad (25)$$

When the formation of the intermediate is the rate controlling step, the contribution of the bases,  $\sum k_b[B]$ , is negligible and the denominator reduces to a value of one. When the deprotonation of the intermediate is rate controlling,  $\sum k_b[B]$  is not negligible and the denominator must be considered.

In this work, the forward rate of PZ reacting with CO<sub>2</sub> was represented as a zwitterion mechanism in which hydroxide and water are the acting bases for proton extraction. This leads to the following expansion of Eq. (25):

$$r = \frac{k_f[\text{CO}_2][\text{Am}]}{1 + [k_r/k_{b,\text{OH}^-}[\text{OH}^-] + k_{b,\text{H}_2\text{O}}]} \quad (26)$$

where  $k_{b,\text{OH}^-}$  represents the extraction of protons from PZ by hydroxide and  $k_{b,\text{H}_2\text{O}}$  represent a pseudo-zero order rate constant associated with the extraction of protons by water from PZ. This expression can be further simplified by assuming the denominator is negligible compared to the contribution of the bases and by combining the rate constants. With this

simplification, the reversible rate for Eq. (5) can be written as

$$r = (k_{\text{PZ}} + k_{\text{PZ-OH}^-}[\text{OH}^-]) \times \left( [\text{PZ}][\text{CO}_2] - \frac{K_w}{K_{\text{PZCOO}^-}} \frac{[\text{PZCOO}^-]}{[\text{OH}^-]} \right) \quad (27)$$

where  $k_{\text{PZ}}$  is the combination of  $k_{b,\text{H}_2\text{O}}$ ,  $k_f$ , and  $k_r$  and  $k_{\text{PZ-OH}^-}$  is defined similarly.

Likewise, for Eq. (7) it is found that the reversible rate is

$$r = k_{\text{PZCOO}^-} ([\text{PZCOO}^-][\text{CO}_2] - \frac{K_w}{K_{\text{PZ}(\text{COO}^-)_2}} \frac{[\text{PZ}(\text{COO}^-)_2]}{[\text{OH}^-]}) \quad (28)$$

The concentration of hydroxide is negligible at any condition where PZCOO<sup>-</sup> is significant and is, therefore, not considered as an acting base in this reaction.

### 3.4. Representation of experimental data

The flux of CO<sub>2</sub> into or out of the solution can be characterized by mass transfer coefficients such as the overall gas transfer coefficient.

$$N_{\text{CO}_2} = K_G(P_{\text{CO}_2,b} - P_{\text{CO}_2}^*) \quad (29)$$

Data was taken at various bulk partial pressures such that the equilibrium partial pressure,  $P_{\text{CO}_2}^*$ , could be found by considering points close to equilibrium and interpolating to a flux of 0.0. The overall mass transfer coefficient,  $K_G$ , is calculated as the slope of the flux versus the log mean pressure,  $\Delta P_{lm}$ . The  $\Delta P_{lm}$  is defined as a log mean difference in bulk gas partial pressures of CO<sub>2</sub> across the wetted-wall column.

$$\Delta P_{lm} = \frac{P_{\text{CO}_2,\text{in}} - P_{\text{CO}_2,\text{out}}}{\ln(P_{\text{CO}_2,\text{in}}/P_{\text{CO}_2,\text{out}})} \quad (30)$$

A demonstration of this procedure is shown in Fig. 2.

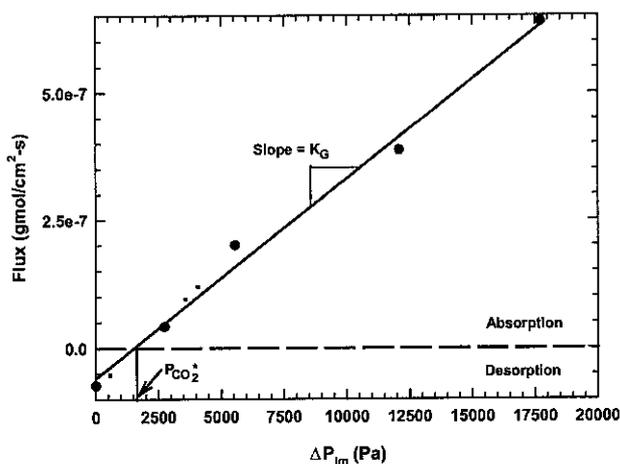


Fig. 2. Determination of  $P_{\text{CO}_2}^*$  and  $K_G$  for 3.6 m K<sup>+</sup>/0.6 m PZ at 40°C and  $\alpha = 0.221$ .

$k_g$  is the gas phase mass transfer coefficient,  $k_g$ , for the wall column was calculated using a correlation defined by Pacheco (1998).

$$1.075 \left( Re Sc \frac{d}{h} \right)^{0.85}, \quad (31)$$

$Re$  is the Reynolds number,  $Sc$  is the Schmidt number,  $d$  is the hydraulic diameter of the column, and  $h$  is the height of the column. The Sherwood number,  $Sh$ , yields  $k_g$  from

$$\frac{RTk_g h}{D_{CO_2}}, \quad (32)$$

$R$  is the gas constant,  $T$  is temperature, and  $D_{CO_2}$  is the diffusion coefficient of  $CO_2$ .

liquid film resistance can be written as

$$= k'_g (P_{CO_2,i} - P_{CO_2}^*), \quad (33)$$

$k'_g$  is a normalized flux, a mass transfer coefficient for partial pressure driving force across the liquid film. The normalized flux was calculated from the following expression

$$\left( \frac{1}{K_G} - \frac{1}{k_g} \right)^{-1}, \quad (34)$$

that the value of  $k'_g$  as calculated from experimental data does not require any pseudo-first order assumption.

## Results and discussion

### Speciation

The relative concentration of each piperazine species was determined by proton NMR (Cullinane, 2002) and is given in Table 2 as a function of composition, loading, and temperature (Table 2). Note that NMR does not distinguish between protonated and protonated forms of the same species. Temperature has a minimal effect on the speciation; however, free piperazine concentration generally increases as temperature increases (Fig. 3).

Loading has a significant effect on speciation as shown in Fig. 4. In this sample, piperazine carbamate and piperazine dicarbamate do not exist at low loading. There is a maximum fraction of piperazine carbamate at a loading near 0.0. At high loading, piperazine dicarbamate becomes an important species, but a significant concentration of the reactant species piperazine carbamate remains. Loading trends over a range of temperatures are comparable (Fig. 5).

The continuous lines in Figs. 3–5 are predictions of the equilibrium model. Throughout the range of loading, the model performs well. There is a slight discrepancy at high loading where the model over-predicts the conversion of piperazine to its carbamate form and the conversion of carbamate to dicarbamate. Model accuracy diminishes as temperature moves away from 60°C, the temperature of the equilibrium constant regressions, indicating that ionic strength affects the temperature dependence of piperazine equilibrium constants.

Table 2  
Integrated NMR peaks as percentage of piperazine species

[K <sup>+</sup> ] (m)	[PZ] (m)	Loading <sup>a</sup>	T (K)	PZ + PZH <sup>+</sup> (%)	PZCOO <sup>-</sup> + H <sup>+</sup> PZCOO <sup>-</sup> (%)	PZ(COO <sup>-</sup> ) <sub>2</sub> (%)
3.6	0.6	-0.347	303	99.3	0.7	0.0
			313	99.3	0.7	0.0
			333	99.5	0.6	0.0
		-0.229	303	78.2	21.8	0.0
			313	79.0	21.0	0.0
			333	78.0	22.0	0.0
		-0.032	303	18.4	47.3	34.3
			313	19.5	48.6	31.9
			333	22.7	49.3	28.0
			303	8.5	41.3	50.3
0.222	303	8.5	41.3	50.3		
	333 <sup>b</sup>	12.6	44.0	43.4		
6.2	0.6	-0.035	313	19.7	49.2	31.1
			333	22.5	49.0	28.5
			353	32.5	39.1	28.4
		0.278	313	5.7	32.7	61.6

<sup>a</sup> mol  $CO_2$ ,TOT/(mol PZ + mol  $K_2$ ) - 1.

<sup>b</sup> Manual graphical integration in lieu of numerical integration.

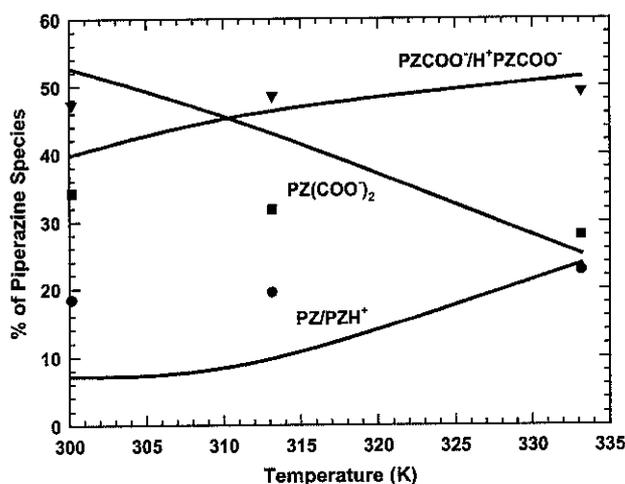
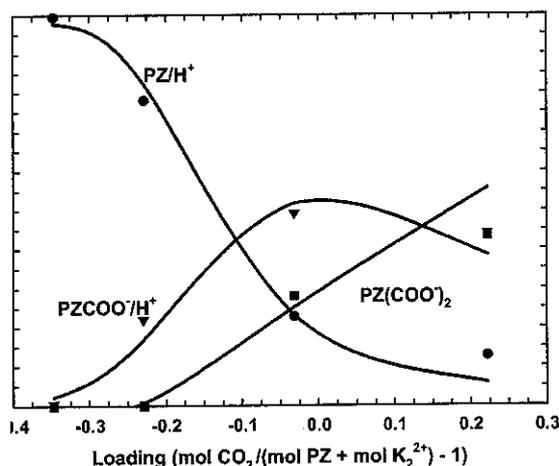


Fig. 3. Piperazine speciation in 3.6 m  $K^+$ /0.6 m PZ at  $\alpha = -0.032$ , points: NMR data, lines: model predictions.

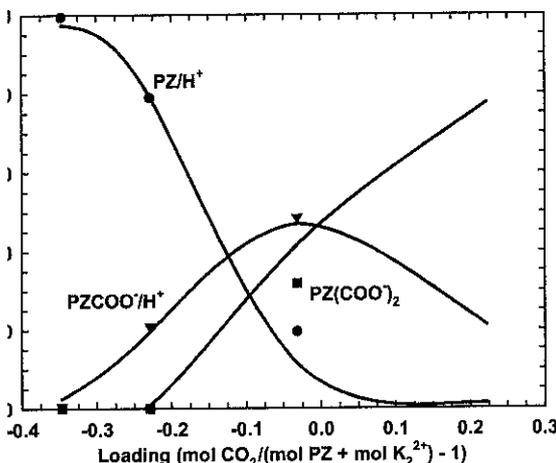
### 4.2. Equilibrium

Fig. 6 shows the effects of PZ addition to potassium carbonate on  $CO_2$  solubility. As shown by the continuous lines, the simple VLE model accurately predicts the equilibrium partial pressure in a solution of both promoted and un-promoted potassium carbonate. The less satisfactory fit at low loading suggests that the selected relationship for the adjustment factors does not hold at low loading conditions. A summary of all equilibrium data collected in the wetted-wall column is presented in Table 3.

The calculated solvent capacity of potassium carbonate solutions compares favorably to amine solvents as shown in



Piperazine speciation in 3.6 m K<sup>+</sup>/0.6 m PZ at 60°C, points: experimental data, lines: model predictions.



Piperazine speciation of 3.6 m K<sup>+</sup>/0.6 m PZ at 40°C, points: experimental data, lines: model predictions.

4. The addition of 0.6 m PZ to 20 wt% K<sub>2</sub>CO<sub>3</sub> yields significant changes in capacity. An increase in potassium concentration produces a large increase in solvent capacity, suggesting further increases would make the capacity equivalent to or greater than that of MEA.

The heat of absorption of CO<sub>2</sub> was calculated from the temperature dependence of the CO<sub>2</sub> solubility (Fig. 7). The addition of 0.6 m PZ to 20 wt% potassium carbonate reduces the heat of absorption from 3.7 kcal/mol (Tosh, 1959) to around 10 kcal/mol. With a comparable loading and PZ concentration, more potassium carbonate is required to decrease the heat of absorption only slightly, suggesting that the amine is largely responsible for the reaction with CO<sub>2</sub>. A decrease in loading results in a marked increase in the heat of absorption, most likely due to a decrease in heats of absorption of piperazine and of piper-carbamate. These results also suggest that promoted

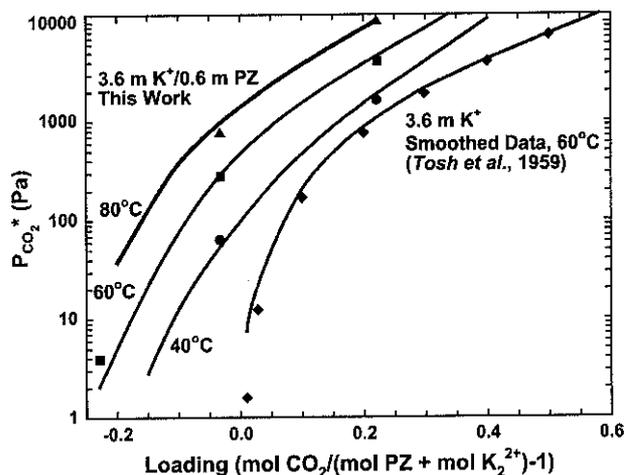


Fig. 6. CO<sub>2</sub> Equilibrium in promoted and un-promoted K<sub>2</sub>CO<sub>3</sub>, points: experimental data, lines: model predictions with  $\beta = 1.0$ .

potassium carbonate solutions would possess a lower heat of absorption than comparable amine systems.

#### 4.3. Absorption rates

Table 3 and Figs. 8 and 9 summarize the normalized flux of CO<sub>2</sub> absorption as measured in the wetted-wall column. The addition of 0.6 m PZ to 3.6 m potassium yields a dramatic change in the rate of CO<sub>2</sub> absorption, increasing the normalized flux by a factor of ten at 60°C. The rate behavior of this solvent approaches that of 7 m MEA at both 40°C and 60°C. Increasing the potassium concentration to 4.8 m does little to affect the absorption rate. At a rich loading, both promoted K<sub>2</sub>CO<sub>3</sub> solutions compare favorably with an MDEA/piperazine blend investigated by Bishnoi (2000). At a constant CO<sub>2</sub> vapor pressure, increasing the temperature from 40°C to 80°C increases the rate of CO<sub>2</sub> absorption by a factor of two (Fig. 9). In this temperature range, a reduction in gas solubility is countered by an increase in sorption kinetics.

The rate data of PZ-promoted K<sub>2</sub>CO<sub>3</sub> is compared to data on two other promoters used in K<sub>2</sub>CO<sub>3</sub> solutions, diethanolamine (DEA) and an unspecified hindered amine investigated by Sartori and Savage (1983), in Fig. 10. For this comparison, CO<sub>2</sub> loading was represented as conversion of CO<sub>3</sub><sup>2-</sup> to HCO<sub>3</sub><sup>-</sup> and Henry's constant was estimated accounting only for the K<sub>2</sub>CO<sub>3</sub> in solution. While each promoter improves the rates over un-promoted K<sub>2</sub>CO<sub>3</sub> to some degree, piperazine at 60°C gives the best improvement. From knowledge of the rate dependence on temperature, the other promoters, DEA and the hindered amine at 90°C, would compare even less favorably to piperazine at 90°C. This behavior can be partially attributed to improved rate behavior and partially to "salting out" of CO<sub>2</sub> at high temperatures and high ionic strengths.

Table 3  
Summary of experimental results from the wetted-wall column, gas flow: 4–7 LPM,  $P_{CO_2}$ : 0–25,000 Pa, liquid flow: 2.5–3.5 cm<sup>3</sup>/s, contact area: 38 cm<sup>2</sup>

T (°C)	[K <sup>+</sup> ] (m)	[PZ] (m)	Nominal loading <sup>a</sup>	$P_{CO_2}^b$ (Pa) (WWC)	$P_{CO_2}$ (Pa) (Model)	Avg. $k_g \times 10^{10c}$ (gmol/Pa cm <sup>2</sup> s)	Avg. $k_l^{dc}$ (cm/s)	$k_g' \cdot 10^{10de}$ (gmol/Pa cm <sup>2</sup> s)	Driving force <sup>f</sup> (Pa)		$\frac{N_{inst,g}}{N_{inst}}$
									Max.	Min.	
60	3.6	0.0	0.176 0.551	515 ± 50 10369 ± 4990	728 10942	2.02 2.83	0.012 0.012	0.11 ± 0.01 0.06 ± 0.01	170 14000	-440 -7070	0.00 0.03
60	3.6	0.6	-0.347 -0.229 -0.032 0.222	< 1 ± 5 3 ± 1 279 ± 30 3539 ± 1300	0 2 305 4784	2.30 2.18 1.75 3.00	0.012 0.013 0.013 0.012	4.41 ± < 0.001 2.47 ± < 0.001 1.81 ± 0.08 0.48 ± 0.07	310 160 270 15310	30 18 -270 -3510	0.01 0.01 0.05 0.21*
40	3.6	0.6	-0.033 0.221	64 ± 8 1635 ± 340	56 1951	1.95 3.01	0.009 0.009	1.32 ± 0.18 0.45 ± 0.03	390 16090	-62 -1620	0.01 0.19*
80	3.6	0.6	-0.033 0.221	756 ± 50 10197 ± 80	1007 10724	2.66 3.11	0.016 0.017	4.24 ± 0.39 0.76 ± 0.03	3830 7740	-230 -6770	0.24* 0.12
60	4.8	0.6	0.290	6212 ± 1070	6526	2.95	0.011	0.49 ± 0.03	14470	-6130	0.18*
40	4.8	0.6	0.290	2453 ± N/A	2978	3.08	0.008	0.26 ± 0.03	17650	390	0.11
80	4.8	0.6	0.290	14161 ± 4890	13533	3.20	0.015	0.52 ± 0.06	8650	-10560	0.16*
60	6.2	1.2	0.205	6014 ± 610	3805	2.75	0.010	0.55 ± 0.04	14270	-2420	0.22*

<sup>a</sup> mol-CO<sub>2</sub>/(mol-PZ + mol-K<sub>2</sub>) - 1.

<sup>b</sup> Found by interpolating to Flux = 0.

<sup>c</sup> Calculated as an average of individual data points taken from WWC.

<sup>d</sup> Calculated from slope of flux versus (P-P\*) for several data points.

<sup>e</sup>  $k_g' = N_{CO_2} / (P_{CO_2,i} - P_{CO_2}^*)$ .

<sup>f</sup> Highest (P<sub>CO<sub>2</sub>,i</sub> - P<sub>CO<sub>2</sub>}<sup>\*</sup>) in experiment.</sub>

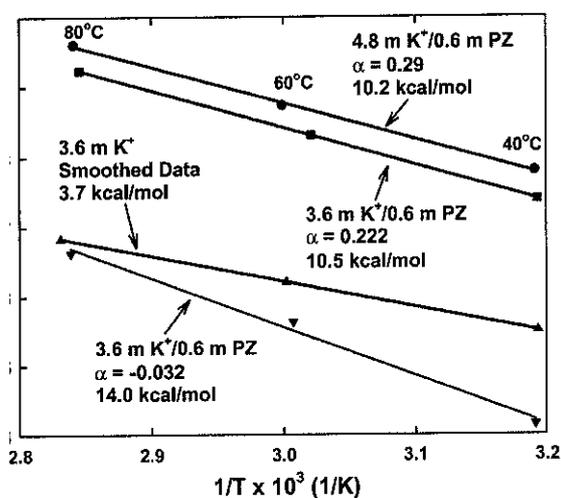
<sup>g</sup> Actual flux/calculated instantaneous flux.

\* Indicates a significant approach to instantaneous behavior.

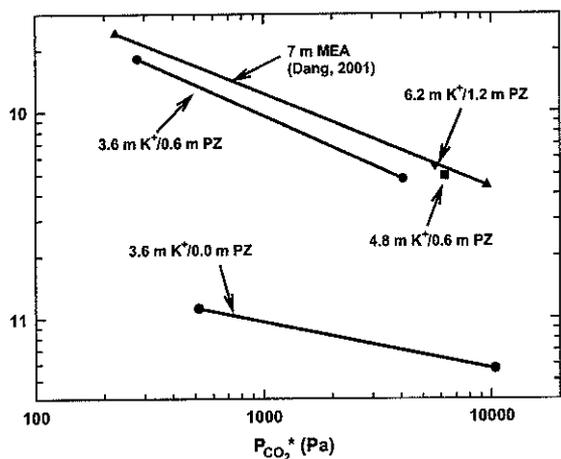
comparison of K<sub>2</sub>CO<sub>3</sub> and amine solvents, lean: 0.01 atm CO<sub>2</sub>, rich: 0.1 atm CO<sub>2</sub>, 33% approach to equilibrium, 60°C

	3.6 m K <sup>+</sup>	3.6 m K <sup>+</sup> /0.6 m PZ	6.2 m K <sup>+</sup>	7 m MEA	1.2 m PZ/8.5 m MDEA	10 m AMP
lg. <sup>a</sup> (m)	2.0	2.3	3.4	9.4	9.1	11.1
τ (m)	0.41	0.50	0.73	0.81	0.78	1.75

ing here is defined as mol CO<sub>2</sub>/kg H<sub>2</sub>O.



CO<sub>2</sub> heat of absorption in K<sub>2</sub>CO<sub>3</sub>/PZ, points: WWC data, lines: regression.



CO<sub>2</sub> absorption rates in K<sub>2</sub>CO<sub>3</sub> and MEA solutions at 60°C.

rate model was able to successfully predict values of  $k_g$  by using regressed rate constants and temperature dependences. As previously mentioned, GREG was used to determine rate constants suitable for Eqs. (27) and (28). The results of the regressions, including values obtained by Bishnoi (2000) for aqueous piperazine, are shown in Table 5.

The rate constants for piperazine and piperazine carbamate used in the model were of the form shown in Eq. (35) to account

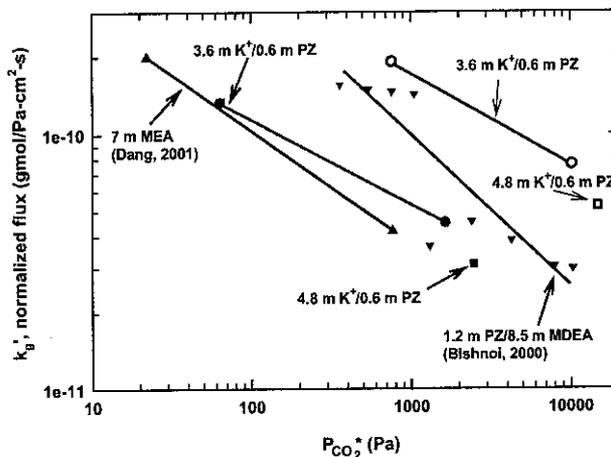


Fig. 9. CO<sub>2</sub> absorption rates in various solvents, closed points: 40°C, open points: 80°C.

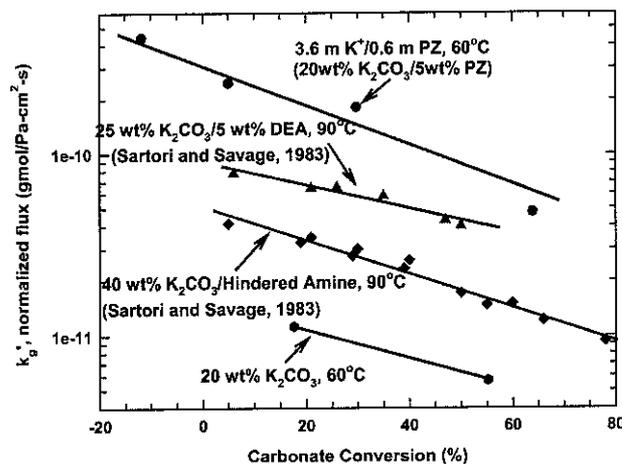


Fig. 10. Comparison of promoted K<sub>2</sub>CO<sub>3</sub> solutions.

for temperature dependence. The PZ-hydroxide rate constant neglects temperature dependence, or  $\Delta H_a = 0$ .

$$k_i = k_i^0 \exp \left[ -\frac{\Delta H_a}{R} \left( \frac{1}{T} - \frac{1}{298.15 \text{ K}} \right) \right] \quad (35)$$

It should be recognized that, while the  $k_g'$  reported is valid for all data, rigorous modeling as performed in this work is required to account for instantaneous behavior and obtain an actual rate constant. Several solutions in Table 3 are noted with an asterisk, indicating that the effect of instantaneous rate is becoming significant. These solutions are typically at

rate constants regressed from various rate equations,  $\Delta H_a = 3.36\text{e4 kJ/mol}$  for piperazine and piperazine carbamate (Bishnoi, 2000)

	Piperazine-hydroxide $k_{\text{PZ-OH}}^0$ ( $\text{m}^6/\text{kmol}^2 \text{ s}$ )	Piperazine $k_{\text{PZ}}^0$ ( $\text{m}^3/\text{kmol s}$ )	Piperazine carbamate $k_{\text{PZCOO}^-}^0$ ( $\text{m}^3/\text{kmol s}$ )
Bishnoi (2000)	0.0 <sup>a</sup>	5.38e4	4.70e4
This work (Fig. 11)	0.0 <sup>a</sup>	1.29e6	1.93e4
This work (Fig. 12)	2.69e6 <sup>b</sup>	2.85e5	4.70e4 <sup>a</sup>

<sup>a</sup>: regressed.

<sup>b</sup>:  $\Delta H_a = 0 \text{ kJ/mol}$ .

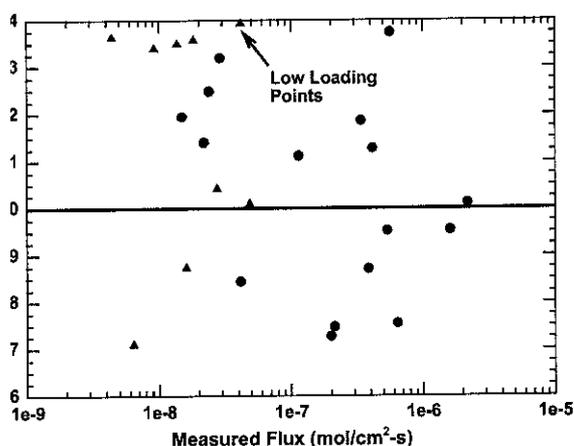


Fig. 11. Parity plot of promoted  $\text{K}_2\text{CO}_3$  fluxes with two regressed rate constants:  $k_{\text{PZ}}^0 = 1.29\text{e6 M}^{-1} \text{ s}^{-1}$  and  $k_{\text{PZCOO}^-}^0 = 1.93\text{e4 M}^{-1} \text{ s}^{-1}$ .

loading or high temperature. The approach to instantaneous rate is a “worst case” estimate for amine depletion in the boundary layer and represents the highest fraction of a data set. Most of the data, however, could be well represented by a pseudo-first order approximation. In this case the kinetics could be found from

$$\frac{\sqrt{D_{\text{CO}_2} k_{\text{Am}} [\text{Am}]_b}}{H_{\text{CO}_2}} \quad (36)$$

using the form of Eq. (15).

Two regressions of the data were performed without and with the PZ-hydroxide rate constant (Cullinane, 2002). The resulting fits of data for 3.6 m  $\text{K}^+$ /0.6 m PZ are shown in Figs. 11 and 12. Note that without the PZ-hydroxide rate constant, seemingly unreasonable changes in the rate constants occur and an unsatisfactory fit of the data results, particularly at low loadings. By including a term prevalent only at low loadings, the PZ-hydroxide rate constant, the fit is improved and more reasonable rate constants are obtained. Including the low loading interaction term, the PZ rate constant is increased by a factor of five from its value in water as reported in Bishnoi (2000). The rate constant for piperazine carbamate gives satisfactory results when its value in 8.5 m MEA is used (Bishnoi, 2000). Previous research suggests that accelerated rate behavior is a result of a catalytic effect of carbonate or of increased ionic strength. Laddha and Kerkwerts (1982) compared effects of  $\text{K}_2\text{CO}_3$  and  $\text{K}_2\text{SO}_4$

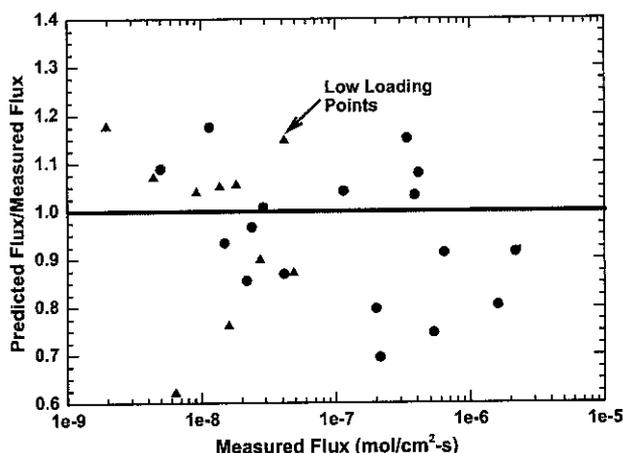


Fig. 12. Parity plot of promoted  $\text{K}_2\text{CO}_3$  fluxes with three regressed rate constants:  $k_{\text{PZ-OH}^-}^0 = 2.69\text{e6 M}^{-2} \text{ s}^{-1}$ ,  $k_{\text{PZ}}^0 = 2.85\text{e5 M}^{-1} \text{ s}^{-1}$ , and  $k_{\text{PZCOO}^-}^0 = 4.70\text{e4 M}^{-1} \text{ s}^{-1}$ .

on MEA and DEA and found that potassium carbonate significantly increases the kinetics of DEA above ionic strength contributions from potassium sulfate addition, suggesting a catalytic effect of the carbonate. The kinetics of MEA are affected equivalently by  $\text{K}_2\text{CO}_3$  and  $\text{K}_2\text{SO}_4$ . Sartori and Savage (1983) and Tseng et al. (1988) also report accelerated rate behavior of DEA/carbonate solutions. Pohorecki et al. (1988) found, however, that the rate constant of ethylaminoethanol, another secondary amine, is a function of ionic strength, not carbonate concentration. The current data on PZ/ $\text{K}_2\text{CO}_3$  does not support attributing the increased kinetics specifically to ionic strength or to carbonate concentration.

The PZ-hydroxide term at a high concentration of hydroxide, 0.45 M, in 3.6 m  $\text{K}^+$  gives an apparent rate constant 22 times faster than in water. This may indicate that the proton extraction, rather than the formation of the zwitterion intermediate, is the rate-limiting step. With large amounts of the strong base hydroxide, it would be expected that this term would be required at low loading. If the proton extraction is rate-limiting even at the low loading conditions (i.e. more base), it is implied that it should be rate-limiting at high loading conditions where there is less base for the catalysis effect.

The simple rate expression (i.e. no PZ-hydroxide term) failed to accurately predict the rate behavior of

zine/ $K_2CO_3$ . Regardless of the mechanism, values relative to one another, that the  $CO_2$ –piperazine reaction in water is much faster than the  $CO_2$ –MEA reaction. Additionally, the piperazine rate is increased over its value in the presence of aqueous potassium carbonate.

## Conclusions

Piperazine is an effective promoter of  $CO_2$  absorption in aqueous potassium carbonate. Rates comparable to those in 7 m MEA are achieved in a 20 wt%  $K_2CO_3$  solution loaded with 0.6 m piperazine.

Model predictions indicate that capacity is somewhat independent of PZ concentration; conversely, an increase in potassium carbonate yields a large increase in capacity. A direct comparison with 7 m MEA and 1.2 m PZ/8.5 m MEA reveals that a 20 wt%  $K_2CO_3$  is not competitive. A 20 wt%  $K_2CO_3$  solution approaches the capacity of MEA. Analysis of equilibrium data indicates that the heat of absorption of  $CO_2$  increases with the addition of PZ to aqueous potassium carbonate. Values for  $\Delta H_{abs}$  vary from 10.5 kJ/mol (Tosh et al., 1959) in 20 wt%  $K_2CO_3$  to 15.5 kJ/mol for a 0.6 m PZ/20 wt%  $K_2CO_3$ .

FTIR NMR suggests that piperazine carbamate is the dominant species at high loading. Consequently, it is responsible for most of the reaction rate. Given that piperazine reacts much faster than the carbamate, it can be concluded that loading has a significant effect on absorption rates. Using regression data from the rate model, the apparent rate constant of piperazine in 20 wt%  $K_2CO_3$  is approximately five times faster than in water. The apparent rate constant for piperazine carbamate is the same as in 20 wt% MDEA. The apparent rate constant for piperazine in 0.6 m piperazine/3.6 m  $K^+$  solution is 22 times faster than in water, emphasizing the suspected catalytic effects of potassium carbonate on  $CO_2$  absorption. For interpretation as an actual rate constant, a rigorous analysis of the absorption is needed to account for effects of instantaneous flux.

Piperazine is an effective additive in that it substantially increases the absorption rate of  $CO_2$ . Current studies reiterate that, coupled with the low heat of absorption associated with aqueous  $K_2CO_3$ , the PZ/ $K_2CO_3$  system could potentially reduce energy costs associated with  $CO_2$  removal. Expanded study of the solvent over a broader range of operationally significant conditions is warranted. A rigorous thermodynamic model will be necessary to encompass the extended solvent concentrations and conditions.

## Acknowledgements

This research was supported by the Separations Research Program at The University of Texas at Austin and The Texas Advanced Technology Program.

## References

- Astarita, G., 1961. Carbon dioxide absorption in aqueous ethanolamine solutions. *Chemical Engineering Science* 16, 202–207.
- Astarita, G., Savage, D.W., Bisio, A., 1983. *Gas treating with chemical solvents*. Wiley, New York.
- Benson, H.E., Field, J.H., Jameson, R.M., 1954.  $CO_2$  absorption employing hot potassium carbonate solutions. *Chemical Engineering Progress* 50 (7), 356–364.
- Benson, H.E., Field, J.H., Haynes, W.P., 1956. Improved process for  $CO_2$  absorption uses hot carbonate solutions. *Chemical Engineering Progress* 52 (10), 433–438.
- Bishnoi, S., 2000. Carbon dioxide absorption and solution equilibrium in piperazine activated methyldiethanolamine. Ph.D. Thesis, The University of Texas at Austin, Austin, TX.
- Bosch, H., Versteeg, G.F., Van Swaaij, W.P.M., 1989a. Gas–liquid mass transfer with parallel reversible reactions—III. Absorption of  $CO_2$  into solutions of blends of amines. *Chemical Engineering Science* 44 (11), 2745–2750.
- Bosch, H., Versteeg, G.F., Van Swaaij, W.P.M., 1989b. Gas–liquid mass transfer with parallel reversible reactions—II. Absorption of  $CO_2$  into amine-promoted carbonate solutions. *Chemical Engineering Science* 44 (11), 2735–2743.
- Caplow, M., 1968. Kinetics of carbamate formation and breakdown. *Journal of the American Chemical Society* 90 (24), 6795–6803.
- Caracotsios, M., 1986. Model parametric sensitivity analysis and nonlinear parameter estimation. Theory and applications. Ph.D. Thesis, The University of Wisconsin, Madison, WI.
- Cullinane, J.T., 2002. Carbon dioxide absorption in aqueous mixtures of potassium carbonate and piperazine. M.S. Thesis, The University of Texas at Austin, Austin, TX.
- Danckwerts, P.V., 1970. *Gas–Liquid Reactions*. Carberry, J.J. (Ed.), McGraw-Hill, New York.
- Dang, H., 2001.  $CO_2$  absorption rate and solubility in monoethanolamine/piperazine/water. M.S. Thesis, The University of Texas at Austin, Austin, TX.
- Edwards, T., Maurer, G., Newman, J., Prausnitz, J., 1978. Vapor–liquid equilibria in multicomponent aqueous solutions of volatile weak electrolytes. *A.I.Ch.E. Journal* 24 (6), 966–976.
- Glasscock, D.A., 1990. Modeling and experimental study of carbon dioxide absorption into aqueous alkanolamines. Ph.D. Thesis, The University of Texas at Austin, Austin, TX.
- Laddha, S.S., Danckwerts, P.V., 1982. The absorption of  $CO_2$  by amine-potash solutions. *Chemical Engineering Science* 37 (5), 665–667.
- Pacheco, M.A., 1998. Mass transfer, kinetics and rate-based modeling of reactive absorption. Ph.D. Thesis, The University of Texas at Austin, Austin, TX.
- Pagano, J.M., Goldberg, D.E., Fernelius, W.C., 1961. A thermodynamic study of homopiperazine, piperazine, and n-(2-aminoethyl)-piperazine and their complexes with copper(II) ion. *Journal of Physical Chemistry* 65, 1062.
- Pohorecki, R., Xoan, D.T., Moniuk, W., 1988. Study of carbon dioxide absorption in aqueous solution of potassium carbonate containing ethylaminoethanol. II. Kinetic relations for 2-(ethylamino)ethanol. *Inzynieria Chemiczna Procesowa* 9 (4), 667–680.
- Posey, M.L., 1996. Thermodynamics model for acid gas loaded aqueous alkanolamine solutions. Ph.D. Thesis, The University of Texas at Austin, Austin, TX.
- Sartori, G., Savage, D.W., 1983. Sterically hindered amines for  $CO_2$  removal from gases. *Industrial and Engineering Chemistry Fundamentals* 22, 239–249.
- Savage, D.W., Sartori, G., 1984. Amines as rate promoters for carbon dioxide hydrolysis. *Faraday Discussions of the Chemical Society* 77, 17–31.

I.S., Field, J.H., Benson, H.E., Haynes, W.P., 1959. Equilibrium of the system potassium carbonate, potassium bicarbonate, carbon dioxide, and water. United States Bureau of Mines, 5484.

P.C., Ho, W.S., Savage, D.W., 1988. Carbon dioxide absorption promoted carbonate solutions. *A.I.Ch.E. Journal* 34 (6), 928–931.

Versteeg, G.F., van Swaaij, W.P.M., 1988. Solubility and Diffusivity of Acid Gases ( $\text{CO}_2, \text{N}_2\text{O}$ ) in Aqueous Alkanolamine Solutions. *Journal of Chemical Engineering Data* 33 (1), 29–34.



## Enhanced carbon dioxide removal by promoted hot potassium carbonate in a split-flow absorber

M.R. Rahimpour\*, A.Z. Kashkooli

*Department of Chemical Engineering, Shiraz University, Shiraz, P.O. Box 71345, Shiraz, Iran*

Received 4 February 2003; received in revised form 9 May 2003; accepted 30 May 2003

ct

In this work, a comprehensive model has been developed for the absorption of carbon dioxide into promoted hot potassium carbonate. The model, which is based on penetration theory, incorporates an extensive set of important reactions and takes into account the effect of mass transfer and chemical kinetics. The penetration theory provides an appropriate absorption rate and enhancement factor for chemical absorption. Operating data for carbon dioxide absorption into DEA–hot potassium carbonate solution has been compared with model predictions. The impact of parameters such as inlet temperature of lean solution, promoter concentration, liquid split fraction, hot gas inlet temperature and type of promoter on the performance of a split-flow absorber have been examined. The use of other promoters is an efficient way to enhance the carbon dioxide absorption, which has been discussed in this paper.

© Elsevier B.V. All rights reserved.

*Keywords:* Hot potassium carbonate; Split-flow absorber; Carbon dioxide absorption; Promoters; Enhanced absorption

### 1. Introduction

The separation of carbon dioxide from mixtures with other gases is a process of substantial industrial importance. In the production of ammonia from hydrocarbons or coal feeds, the removal of carbon dioxide from the synthesis gas is a necessary process step. Large volumes of natural gas are also processed for carbon dioxide removal. Several processes are in use for CO<sub>2</sub> removal but process selection must be based on economic and clean-up ability. Among the processes, the promoted hot carbonate process provides an economic and efficient way for removing large quantities of CO<sub>2</sub> from synthesis gases. In this process, the amine generally provides a high absorption rate, while the carbonate–bicarbonate buffer provides the advantages of large capacity for CO<sub>2</sub> and ease of regeneration.

The promoted hot carbonated process was originally developed by Soudan et al. [1], and has since undergone several improvements [2–4]. The most important improvement is the discovery that small amount of certain organic or inorganic additives (promoters) can enhance the absorption rate largely

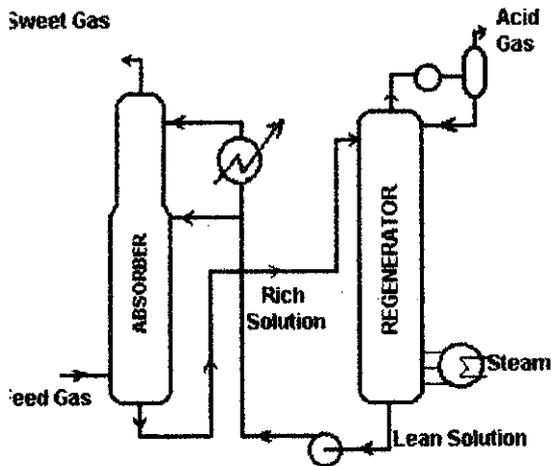
[5]. The concept of the addition of amine to carbonate system to enhance CO<sub>2</sub> absorption has been known for a long time [6,7].

In the mechanism, which is called homogeneous catalysis, the promoter first forms an intermediate with CO<sub>2</sub> and the intermediate is then hydrolyzed to produce the final product, bicarbonate [5]. In another mechanism, which is called shuttle, the promoter acts as a carrier to provide an additional pathway for the transport of CO<sub>2</sub> from the gas–liquid interface to the bulk liquid [7]. Astarita et al. [8] concluded that the two mechanisms are different only quantitatively, not qualitatively. Savage and Astarita [9] indicated that the rate promotion effect of amine in carbonate solutions could be described very well from the viewpoint of homogeneous catalysis at higher temperatures in the range of industrial operating conditions. In a recent study [10], the joint action of two promoters on the absorption of CO<sub>2</sub> in alkaline buffer solution measured experimentally.

A number of authors already investigated the modeling and simulation of hot potassium carbonate process [11,12], but the published information is very little detailed. The recent model proposed by Sanyal et al. [11] for an industrial hot potassium carbonate process, simplified the calculations and gave reasonable predictions but it did not consider the effect of chemical reactions on CO<sub>2</sub> absorption and neglected

\*Corresponding author. Tel.: +98-711-2303-071; Fax: +98-711-6287-294.

E-mail address: [rahimpour@shirazu.ac.ir](mailto:rahimpour@shirazu.ac.ir) (M.R. Rahimpour).



Schematic diagram of a conventional split-flow absorber-stripper system.

effect of amine concentration on the absorption performance. However, no previous work has examined the effect and types of promoters in the split-flow absorber and configurations of split-stream or attempted to exploit this behavior to develop better process. Therefore, we decided to investigate more thoroughly the effect of these parameters on the carbon dioxide absorption with potassium carbonate. In this work a general model for the mass transfer/reaction processes in carbon dioxide absorber using promoted hot potassium carbonate has been developed. The combined effect of mass transfer and chemical reaction was treated by the reaction-renewal penetration theory. The effect of different promoters on the performance of a split-flow absorber has been investigated and the design consequences of different promoters have been discussed.

### Process description

Fig. 1 shows a schematic diagram of a conventional split-flow absorber-stripper [13]. The process scheme is simple, the feed gas is contacted counter-currently with the hot potassium carbonate in the absorber, and essentially all of the carbon dioxide is removed. The effluent gas which contains only a very small amount of carbon dioxide can be used in ammonia synthesis. The rich solution loaded with carbon dioxide passes to the regenerator where it is stripped by counter-current contacting with a stream of piping steam. A portion of lean solution from the regenerator is cooled and fed into the top of the absorber while the major portion is added at a point some distance below the top without any changing in temperature. This simple configuration, which is called split-flow process, improves the purity of the product gas by decreasing the equilibrium vapor pressure of the  $\text{CO}_2$  over the portion of solution last contacted by the gas. Tables 1 and 2 show the characteristics of two absorption columns.

Table 1

Characteristics of the absorption tower, packing and system for  $\text{CO}_2$  absorption for the first column [13]

Parameters	Top section	Bottom section	Units
Height of packing	19.84	21	m
Diameter of packed bed	3.4	4.5	m
Packing size ( $d_p$ )	51	47	mm
Packing shape	Metal mini rings	Metal mini rings	–
Specific surface of packing ( $a$ )	123	144	$\text{m}^{-1}$
Packing void fraction	0.975	0.878	–

### 3. Chemical reactions

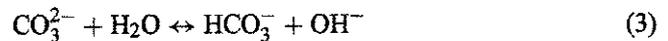
The basic reaction chemistry for aqueous hot potassium carbonate solution and  $\text{CO}_2$  is represented by the following reversible reaction [8]:



Since potassium carbonate and bicarbonate are both strong electrolytes, it may be assumed that the metal is present only in the form of  $\text{K}^+$  ions, so reaction (1) may be more realistically represented in the ionic terms as:



The above reaction is evidently made up of a sequence of elementary steps. The carbonate ion first reacts with water to generate hydroxyl ions, which then react with  $\text{CO}_2$  as follows [8]:



Since reaction (3) is instantaneous reaction, reaction (4) is the rate-controlling step, so that the rate equation for reaction of carbon dioxide with un-promoted hot potassium carbonate leads to [8,14]:

$$r_{\text{OH}} = k_{\text{OH}}[\text{OH}^-][\text{CO}_2] - k_{-\text{OH}}[\text{HCO}_3^-] \quad (5)$$

where  $k_{\text{OH}}$  and  $k_{-\text{OH}}$  are forward and backward rate constants of reaction (4). At equilibrium condition Eq. (5) gives:

$$k_{-\text{OH}}[\text{HCO}_3^-] = k_{\text{OH}}[\text{OH}^-][\text{CO}_2]_e \quad (6)$$

Table 2

Characteristics of the absorption tower, packing and system for  $\text{CO}_2$  absorption for the second column [11]

Parameters	Column specifications	Units
Height of packing	17.2	m
Diameter of packed bed	1.4	m
Packing size ( $d_p$ )	37	mm
Packing shape	Intalox saddles (ceramic)	–
Specific surface of packing ( $a$ )	144	$\text{m}^{-1}$
Packing void fraction	0.80	–

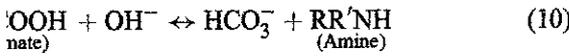
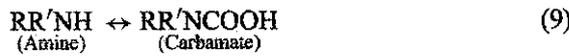
$[CO_2]_e$  is the equilibrium concentration of  $CO_2$ . The ion for reverse reaction (4) in Eq. (6) has been evaluated considering conditions at equilibrium, but it is true, even when the system is not at equilibrium. Substituting Eq. (6) into Eq. (5) gives [14]:

$$(k_{OH}[OH^-])([CO_2] - [CO_2]_e) \quad (7)$$

ate-bicarbonate system is a buffer solution, so the concentration of  $OH^-$  ion in the solution near the surface of is not significantly depleted by the absorbed  $CO_2$ . In equilibrium, the carbon dioxide undergoes a pseudo-first order reaction and Eq. (7) may be rewritten as [8,14,15]:

$$k_1([CO_2] - [CO_2]_e) \quad (8)$$

$k_1$  denotes apparent first-order rate constant. When a small amount of amine is added into the solution, the absorption rate of carbon dioxide is enhanced greatly according to the following reactions [8]:



At higher temperatures in the range of industrial operating conditions, the rate of reaction (10) increases significantly, and is better represented by the homogeneous catalytic mechanism [15,8], and reaction (9) is rate-controlling. Using the same approach for deriving Eq. (8), gives the following pseudo-first order rate equation for  $r_{Am}$  [14]:

$$(k_{Am}[Am])([CO_2] - [CO_2]_e) \quad (11)$$

$k_2$  is apparent first-order rate constant. Combining Eqs. (7) and (11) leads to the overall pseudo-first order rate equation of carbon dioxide with promoted hot amine carbonate in liquid phase:

$$k([OH^-] + k_{Am}[Am])([CO_2] - [CO_2]_e) \quad (12)$$

$k$  is the overall apparent first-order rate constant and is defined as:

$$k = k_{OH}[OH^-] + k_{Am}[Am] \quad (13)$$

**Mathematical development**

A differential material and energy balance around a differential element of column shown in Fig. 2, gives the mathematical model of a packed absorber [17]. Envelope III is an element volume in the differential packed height ( $\Delta Z$ ) of the absorber, consisting of the gas and liquid phase denoted by envelopes I and II, respectively. The major assumptions are (1) steady-state conditions prevail, (2) pressure drop across the packed bed is negligible, and (3)  $CO_2$  and  $H_2O$  are the components transported across the interface.

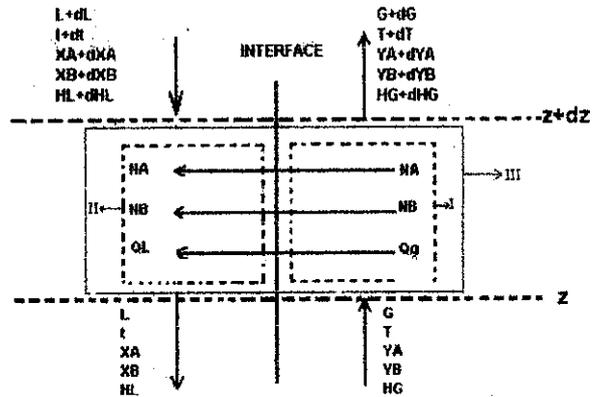


Fig. 2. Differential section of packed absorber.

**4.1. Mole balance**

**4.1.1. Gas phase**

A differential mole balance in the gas phase around  $\Delta z$  gives a differential equation for gas flow along the bed:

$$\frac{dG}{dz} = -(N_{CO_2} + N_{H_2O})a \quad (14)$$

where  $G$  is superficial molar velocity of gas;  $N_{CO_2}$  and  $N_{H_2O}$  are mass transfer fluxes of  $CO_2$  and water, and  $a$  is the specific surface area of packing.

A differential mole balance in gas phase for  $CO_2$  and water gives the following differential equations for mole fraction of carbon dioxide and water in the gas phase:

$$\frac{dy_{CO_2}}{dz} = \frac{[(N_{H_2O}y_{CO_2} - N_{CO_2}(1 - y_{CO_2}))]a}{G} \quad (15)$$

$$\frac{dy_{H_2O}}{dz} = \frac{[(N_{CO_2}y_{H_2O} - N_{H_2O}(1 - y_{H_2O}))]a}{G} \quad (16)$$

**4.1.2. Liquid phase**

Here it has been assumed that for the amine-promoted carbonate solution the reaction is fast and hence the reaction takes place at the same rate at which the carbon dioxide is reached to reactants in each element of liquid [12,14]. Therefore, we can develop the differential equation for molar flow rate and compositions of liquid phase when the rate of absorption and stoichiometry of reaction (1) are taken into account.

A differential mole balance in liquid phase gives an equation for liquid flow rate as follows:

$$\frac{dL}{dz} = -N_{H_2O}a \quad (17)$$

where  $L$  is the superficial molar velocity of liquid.

In the liquid phase,  $K_2CO_3$  consumed by chemical reaction as the solution moves down the packing bed. Hence, when the reaction stoichiometry is taken into account, differential moles balance for  $K_2CO_3$  gives:

$$\frac{d(Lx_{K_2CO_3})}{dz} = N_{CO_2}a \quad (18)$$

ing  $dL$  by Eq. (17) gives rise to the following differential equation for mole fraction of  $K_2CO_3$ :

$$\frac{dC_{CO_2}}{dz} = \frac{[N_{H_2O}x_{K_2CO_3} + N_{CO_2}]a}{L} \quad (19)$$

Since  $KHCO_3$  is the reaction product in the liquid phase, we can develop the differential equation for mole fraction of  $HCO_3^-$ , when the reaction stoichiometry is taken into account:

$$\frac{dC_{HCO_3^-}}{dz} = \frac{[N_{H_2O}x_{KHCO_3} - 2N_{CO_2}]a}{L} \quad (20)$$

A balance for  $H_2O$  also yields the following equation in liquid phase:

$$\frac{dC_{H_2O}}{dz} = \frac{[N_{CO_2} - N_{H_2O}(1 - x_{H_2O})]a}{L} \quad (21)$$

#### Energy balance

A differential energy balance for the gas phase around a differential height of packed bed ( $dz$ ), gives rise to the following differential equation for temperature of gas phase:

$$\begin{aligned} &= \frac{(N_{CO_2} + N_{H_2O})a}{G} T \\ &- \frac{(N_{CO_2}C_{P_{CO_2}} + N_{H_2O}C_{P_{H_2O}})a}{GC_{P_G}} T - \frac{h_g a(T - t)}{GC_{P_G}} \end{aligned} \quad (22)$$

where the heat effects due to bulk motion, mass transfer and reaction between phases are taken into account [11]. Similarly, an energy balance in the liquid phase gives rise to the following differential equation for temperature of liquid phase:

$$\begin{aligned} &= \frac{N_{H_2O}a}{L} t - \frac{(N_{CO_2}C_{P_{CO_2}} + N_{H_2O}C_{P_{H_2O}})a}{LC_{P_L}} T \\ &- \frac{h_g a(T - t)}{LC_{P_L}} - \frac{(N_{CO_2}\Delta H_{CO_2} + N_{H_2O}\Delta H_{H_2O})a}{LC_{P_L}} \end{aligned} \quad (23)$$

where  $\Delta H_{CO_2}$  is heat of absorption and reaction of  $CO_2$ ,  $\Delta H_{H_2O}$  is heat of vaporization of water [11].

#### Mass transfer

The combined effect of chemical reaction presented by Eq. (12) and mass transfer are conveniently and adequately described by the framework of penetration-surface renewal theory developed by Danckwerts [14]. The absorption rate of carbon dioxide in the liquid phase according to this theory and homogeneous catalysis mechanism can be expressed as follows [14–16]:

$$N_{CO_2} = Ek_L(C_{CO_2_i} - C_{CO_2_e}) \quad (24)$$

where  $C_{CO_2_i}$  is the concentration of carbon dioxide at the interface and  $C_{CO_2_e}$  is the equilibrium concentration of

unreacted carbon dioxide in the bulk of liquid when the reverse reaction of carbon dioxide is appreciable.  $k_L$  is liquid phase mass transfer coefficient and  $E$  is the enhancement factor and describes the mass transfer coupled by chemical reactions as follows [14]:

$$E = \sqrt{1 + \frac{D_{CO_2}k}{k_L^2}} \quad (25)$$

where  $k$  is defined by Eq. (13). The rate of absorption, which is defined by Eq. (24), can be rewritten in terms of physical solubility of carbon dioxide in solution,  $H$ , in the reactive  $K_2CO_3$  solution as:

$$N_{CO_2} = k_L H E (P_{CO_2_i} - P_{CO_2_e}) \quad (26)$$

The rate of mass transfer of carbon dioxide in the gas phase is also as follows:

$$N_{CO_2} = k_{g_{CO_2}} (P_{CO_2} - P_{CO_2_i}) \quad (27)$$

where  $k_{g_{CO_2}}$  is gas phase mass transfer coefficient of carbon dioxide.

Combining Eqs. (26) and (27) and eliminating the interface partial pressure of carbon dioxide,  $P_{CO_2_i}$ , gives rise to the following equation for the absorption rate:

$$\begin{aligned} N_{CO_2} &= \left( \frac{k_{g_{CO_2}} k_L E H}{k_{g_{CO_2}} + k_L E H} \right) (P_{CO_2} - P_{CO_2_e}) \\ &= K_{g_{CO_2}} (P_{CO_2} - P_{CO_2_e}) \end{aligned} \quad (28)$$

where  $K_{g_{CO_2}}$  is overall gas phase mass transfer coefficient of carbon dioxide.

Water is another component, which is substantially transported in gas phase across the interface. It may be assumed that there is no liquid-side resistance for the mass transfer of the solvent water vapor. Therefore, the overall mass transfer coefficient for the water vapor is the same as the mass transfer coefficient in gas phase, and then the mass transfer rate of water per unit interfacial area is:

$$N_{H_2O} = K_{g_{H_2O}} (P_{H_2O} - P_{H_2O_e}) \quad (29)$$

where  $K_{g_{H_2O}}$  is overall gas phase mass transfer coefficient of water.

#### 4.4. Equilibrium, kinetic and transport parameters

The kinetic parameters of different amines are provided in Table 3 and the equilibrium and transport parameters are tabulated in Table 4.

### 5. Numerical solution

The proposed nine differential Eqs. (14)–(17) and Eqs. (19)–(23), need to be solved to simulate a column of

stants of reaction between amines and CO<sub>2</sub> where *t* is liquid ure (K) [16]

$k_{Am}$ (m <sup>3</sup> kmol <sup>-1</sup> h <sup>-1</sup> )
$6.4 \times 10^8 \exp \left[ 14.97 \left( 1 - \frac{353}{t} \right) \right]$
$3.4 \times 10^8 \exp \left[ 13.54 \left( 1 - \frac{353}{t} \right) \right]$
$12 \times 10^8 \exp \left[ 13.40 \left( 1 - \frac{353}{t} \right) \right]$

height by taking into account the boundary conditions, the flow rate, composition and temperature of the gas entering the column at its bottom and the flow rate, composition and temperature of the liquid phase entering the column at its top are known in simulation problem. To solve the integration procedure, the flow rate, concentration and temperature of the liquid phase at the bottom of the column need to be estimated. With the help of the estimated

um, kinetics and transport parameters

r Expression	Source
$\alpha = \frac{[K^+]}{[K^+] + 2[CO_3^{2-}]} = \frac{[HCO_3^-]}{[K^-]}$	[15]
$P_{CO_2} = 2 \frac{K_2[K^+]}{K_1H} \frac{\alpha^2}{1-\alpha}$	[15]
$\log(K_1) = -(3404.7/t) + 14.843 - 0.03279t$	[15]
$\log(K_2) = -(2902.4/t) + 6.498 - 0.0238t$	[15]
$\log(H/H_W) = -K_3I; K_3 = 0.06, I = 6.2$	[15]
$\log H_W = (1140/t) - 5.30$	[15]
$\log P_{H_2O} = -(L'/2.303R)((1/t) - 2.45 \times 10^{-3}) - 1.1672 + C; L' = 40983.6$	[18]
$C = 1.2014 + (0.2857/x_c) - (0.0537/x_c^2)$	[18]
$x_c = \frac{0.691(\%KHCO_3)}{\%K_2CO_3 + 0.691(\%KHCO_3)}$	[18]
$\log(k_{OH}) = 13.635 - (2895/t) + 0.081$	[19]
$\frac{k_{gk} RT}{aD_{gk}} = 5.32 \left( \frac{\hat{G}}{a\mu_g} \right)^{0.7} \left( \frac{\mu_g}{\rho_g D_{gk}} \right)^{1/3} (ad_p)^{-2.0}$	[14]
$k_L \left( \frac{\mu_1^2}{\rho_1^2} \right)^{1/3} / D_{CO_2} = 0.015 \left( \frac{\hat{L}}{a\mu_1} \right) \left( \frac{\mu_1}{\rho_1 D_{CO_2}} \right)^{1/3}$	[20]
$\log D_{CO_2} = -3.0188 - \frac{586.9729}{t} - 0.4437$	[21]
$h_g = \sum_k y_k h_{gk}$	[22]
$h_{gk} = k_{y_k} C_{p_k} (L_e)^{2/3}$	[22]
$C_{p_L} = 4.1774 - 0.0382\omega - 0.4445 \times 10^{-3}\omega^2 + 1.2798 \times 10^{-5}\omega^3$	[24]
$\Delta H_{CO_2} = 27228.2 + 81.37\omega + 5.32\omega^2 - 0.1313\omega^3 + 1.654 \times 10^{-3}\omega^4$	[23]
$\omega = \frac{\%K_2CO_3 + 0.691(\%KHCO_3)}{\%K_2CO_3 + 0.781(\%KHCO_3) + \%H_2O}$	[11]

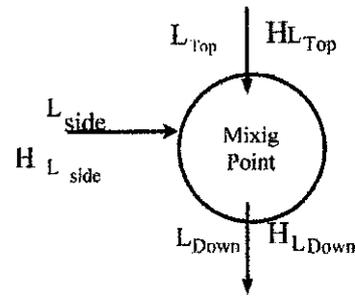


Fig. 3. Schematic diagram of mixing point between split-flow and downward liquid stream.

values, the column equations can be integrated by using the Euler method up to the top point where the split hot lean solution is added to the column. At this point the following equations, which are the results of mass and energy balance at the mixing point, are used to calculate molar flow rate, composition and temperature of the liquid stream in the next upper increment as follows:

$$L_{Top} = L_{Down} - L_{Side} \tag{30}$$

$$x_{Top} = \frac{L_{Down}x_{Down} - L_{Side}x_{Side}}{L_{Top}} \tag{31}$$

$$T_{L_{Top}} = \frac{L_{Down}C_{pL_{Down}}T_{L_{Down}} - L_{Side}C_{pL_{Side}}T_{L_{Side}}}{L_{Top}C_{pL_{Top}}} \tag{32}$$

in which *Down* denotes the stream below mixing point, *Top* denotes the stream above mixing point and subscript *Side* represents the side feed stream as shown in Fig. 3.

The numerical procedure is continued from mixing point up to the top of the column to obtain actual values of liquid entering, with the help of which further iteration can be made using shooting method until satisfactory convergence is obtained [25–27]. In this method two values for the liquid flow rate at the bottom,  $L_b^{(1)}$  and  $L_b^{(2)}$ , are assumed and the corresponding values for the liquid flow rates at the top,  $L_t^{(1)}$  and  $L_t^{(2)}$ , are calculated by the model. The points A and B are plotted at  $(L_b^{(1)}, L_t - L_t^{(1)})$  and  $(L_b^{(2)}, L_t - L_t^{(2)})$  in a xy plane, where  $L_t$  is the observed liquid flow rate at the top. Line AB is extended to intersect the x axis at C, which provides the next guess for  $L_b$  say  $L_b^{(3)}$  [27].

The remaining six variables, liquid temperature, *t*, and liquid mole fractions,  $x_{K_2CO_3}$ ,  $x_{KHCO_3}$ ,  $x_{H_2O}$ ,  $x_{DEA}$  and  $x_{KVO_3}$  are treated in the same manner. A computer program to solve the model equations was written in FORTRAN language.

### 6. Model validation

A verification of the model was carried out by comparison with the operating data of hot carbonate process, under the design specification for two different columns summarized in Table 1 from Shiraz Petrochemical Complex [13] and Table 2 from data reported by Sanyal et al. [11]. The

5

Comparison of calculated results with the observed plant data [13] with specification indicated in Table 1 for the first column

Parameters	Inlet	Outlet		Error (%)
		Observed	Calculated	
Temperature (K)	343.2	388.2	394.6	-1.69
	401.0			
Flow rate (kmol h <sup>-1</sup> )	15418.7	63660.2	62117.1	2.42
	46259.6			
Composition (mole fraction)				
	0.03663	0.01260	0.01331	-5.63
H <sub>2</sub> S	0.02527	0.07110	0.07121	-0.15
	0.92943	0.90766	0.90689	0.08
(anti-corrosion)	0.00722	0.00720	0.00715	0.69
	0.00145	0.00144	0.00144	0.00
Temperature (K)	388.2	343.2	357.2	-4.09
Flow rate (kmol h <sup>-1</sup> )	8459.0	6660.0	6576.6	1.25
Composition (mole fraction)				
	0.17150	0.00197	0.00199	-1.03
	0.00187	0.00241	0.00241	-0.19
	0.00376	0.00483	0.00484	-0.18
	0.57510	0.73910	0.73964	-0.09
	0.18590	0.23850	0.23910	-0.25
	0.00224	0.00285	0.00288	-0.88
	0.05970	0.01081	0.01002	7.41

Comparison of calculated results and actual data are presented in Tables 5 and 6. Overall, for all the cases the obtained agreement is satisfactory.

6

Comparison of calculated results with the observed plant data [11] with specification indicated in Table 2 for the second column

Parameters	Inlet	Outlet		Error (%)
		Observed	Calculated	
Temperature (K)	343.0	392.0	379.0	3.32
	371.0			
Flow rate (kmol h <sup>-1</sup> )	2630.0	5308.0	5350.5	-0.80
	2630.0			
Composition (mole fraction)				
	0.04013	0.015800	0.01579	0.08
H <sub>2</sub> S	0.02015	0.066300	0.06711	-1.22
	0.93200	0.919800	0.90949	1.12
(anti-corrosion)	0.00719	0.007005	0.00712	-1.62
	0.00055	0.000540	0.00055	-1.80
Flow rate (kmol h <sup>-1</sup> ) with inlet temperature 408 K	762.9	547.1	545.1	0.36
Composition (mole fraction)				
	0.16590	0.00100	0.00091	8.73
	0.00184	0.00257	0.00258	-0.20
	0.00263	0.00366	0.00368	-0.57
	0.53060	0.73880	0.74260	-0.51
	0.17330	0.24130	0.24254	-0.51
	0.00210	0.00290	0.00294	-1.35
	0.12370	0.00990	0.00879	11.22

## 7. Results and discussion

The performance of the carbon dioxide absorption was investigated by conducting absorption simulations over some runs under the design and operating conditions summarized in Tables 1 and 5 for the first column. The simulation results were plotted as profiles of the dependent parameters versus independent variables, along with plant data. In addition, the effects of different parameters on the absorption performance were investigated.

### 7.1. Effect of promoter concentration

According to Fig. 4, an increase in the amine concentration first induces a higher CO<sub>2</sub> removal while raising the amine content beyond a specific amount has no effect on the exit CO<sub>2</sub> concentration. The possible explanation for this behavior is that increasing the amine concentration reflects the higher enhancement factor in the liquid phase, which is directly proportional to the overall K<sub>g</sub> in the case of liquid-phase controlled mass transfer. With more increasing the amine concentration, the gas phase mass transfer is considered the major factor controlling the absorption process so the CO<sub>2</sub> removal is unaffected by increasing the promoter concentration.

### 7.2. Effect of promoter type

The role of amine type in carbon dioxide removal is shown in Fig. 5. Three types of promoter were compared

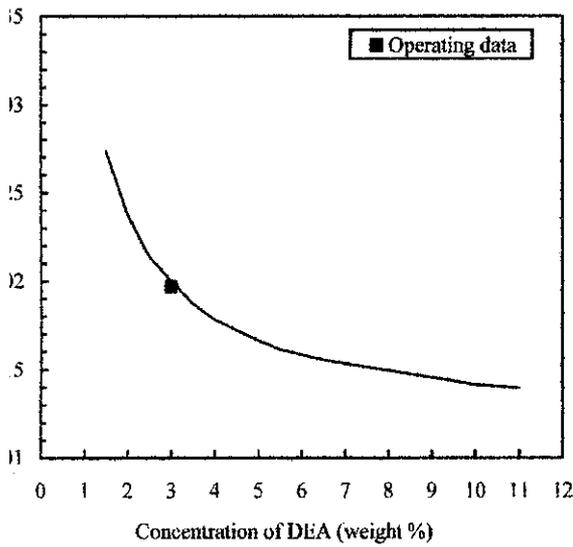


Fig. 4. Exit CO<sub>2</sub> concentration versus the weight percent of amine in solution.

From this figure, MAE provides more absorption efficiency than DEA and MEA. The difference between the CO<sub>2</sub> removal efficiency by the three types of amines is preliminarily estimated by second-order rate constant,  $k_{Am}$  as provided in Table 3.

*Effect of liquid split fraction*

In split-stream absorption systems, the carbon dioxide absorption behavior is further complicated by the presence of a hot liquid side feed. In this system a fraction of the lean solution from regenerator is cooled and fed at the bottom of absorber. As it is clearly demonstrated in Fig. 7, an increase in this stream would result in a higher outlet CO<sub>2</sub> concentration of synthesis gas, due to the lowering vapor pressure of CO<sub>2</sub> at lower temperature. As this fraction increases, the amount of hot lean solution fed at middle of column also increases which would result in lower temperature at the bottom section of column. However, in this case, the influence of overall mass transfer coefficient seems to dominate over the driving force, thus results to less sensitivity of CO<sub>2</sub> removal to the increase in cold liquid split fraction.

*Effect of liquid temperature*

The temperature of lean solution also has an influence on absorption performance as demonstrated in Fig. 7. The figure indicates the higher mass-transfer performance at lower temperature, which can be presented by decreasing the equilibrium vapor pressure of CO<sub>2</sub> over the portion of gas last contacted by the gas. It is clear that as we attain higher inlet concentrations, the absorber curves A and B have a

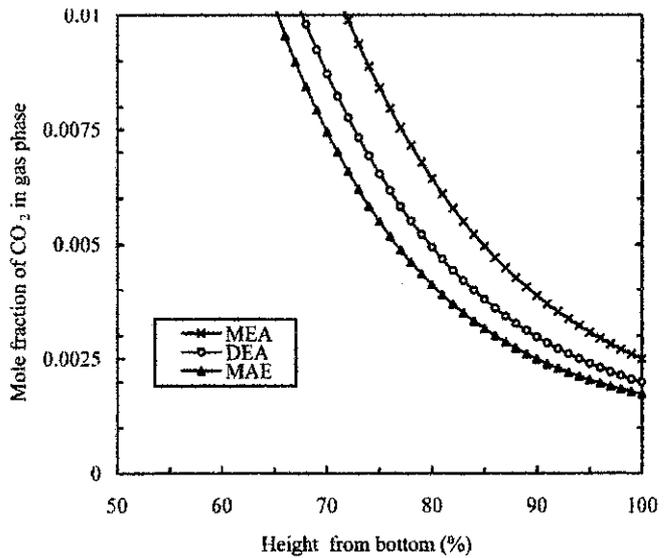


Fig. 5. Exit CO<sub>2</sub> concentration profiles along the packed bed height for various promoters.

horizontal asymptote, so a large decrease in the inlet liquid temperature is required to obtain a small reduction in outlet carbon dioxide concentration. Hence, beside the influence of the equilibrium vapor pressure of CO<sub>2</sub>, the overall mass transfer coefficient, which depends on temperature directly, plays an important role on the absorption performance.

*7.5. Effect of hot split-stream*

A change in the location of the entering hot stream has an effect on the concentration of CO<sub>2</sub> in exit gas stream as shown in Fig. 8. The change of hot split-stream location primarily affects liquid flow rate profile, which would result

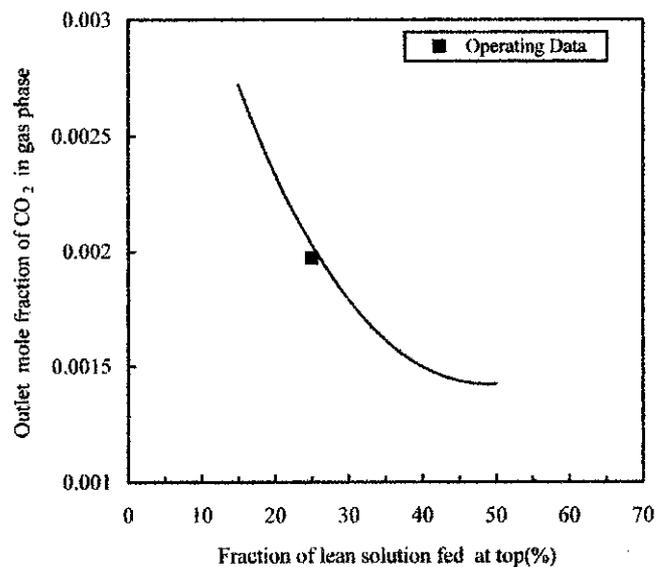
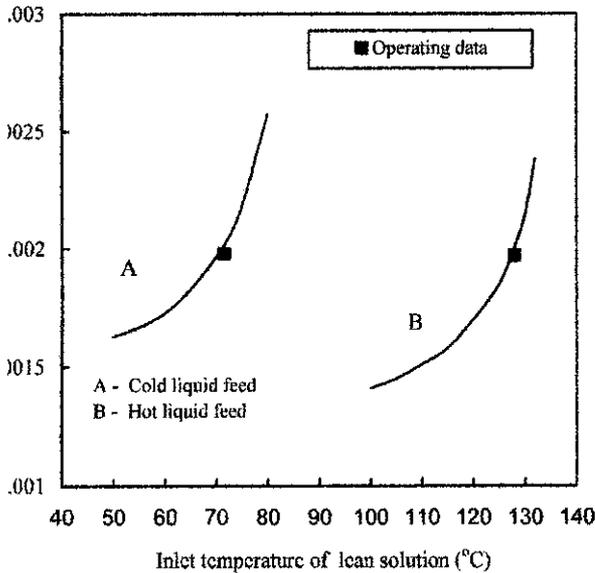
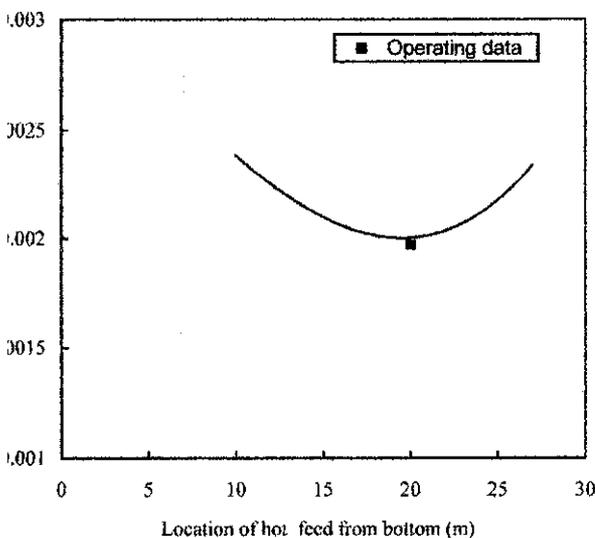


Fig. 6. Exit CO<sub>2</sub> concentration vs. fraction of lean solution fed at the top of column.



7. Exit CO<sub>2</sub> concentration vs. inlet temperature of lean solution.

ges in liquid temperature and mass transfers coefficient es. An interesting feature of this figure is that we usually observe a point of minimum carbon dioxide removal, arises at the transition between two region of column section, i.e. that in as location of hot side feed moves the column allows lower liquid temperature at top in which would result in higher mass transfer performance by decreasing the vapor pressure of carbon dioxide, that in which as the location of hot side feed moves towards higher liquid temperature and flow rate at bottom in which would result in higher mass transfer performance by increasing overall mass transfer coefficient. Therefore, hot feed location from bottom must be chosen in order to optimize this compromise.



8. Exit CO<sub>2</sub> concentration vs. location of hot split-stream location.

## 8. Conclusion

The model presented in this work, accurately predicted absorber performance when the results were compared with operating data. The results indicate the performance of hot potassium carbonate process can be improved by finding better process systems. Judicious selection of the inlet split-streams temperature, hot split-stream location, and ratio of the cold feed rate to the hot feed rate can, therefore, lead to design that achieve high carbon dioxide removal. Promoter type is considered as another essential factor affecting the efficiency of CO<sub>2</sub> absorption process. The use of other amines is an efficient way to enhance the separation, which has been addressed in this paper. The model provides a procedure to investigate the effect of new promoters on the CO<sub>2</sub> absorption.

## Acknowledgements

The authors gratefully acknowledge the financial support of Shiraz Petrochemical Complex.

## Appendix A. Nomenclature

$a$	specific surface area ( $\text{m}^2 \text{m}^{-3}$ )
$C_k$	concentration of kth component ( $\text{kmol m}^{-3}$ )
$C_{ke}$	equilibrium concentration of kth component in the bulk of liquid ( $\text{kmol m}^{-3}$ )
$C_{ki}$	concentration of kth component at interface ( $\text{kmol m}^{-3}$ )
$C_{PG}$	molar specific heat of gas ( $\text{kJ kmol}^{-1} \text{K}^{-1}$ )
$C_{PK}$	specific heat of kth component ( $\text{kJ kmol}^{-1} \text{K}^{-1}$ )
$C_{pL}$	molar specific heat of liquid ( $\text{kJ kmol}^{-1} \text{K}^{-1}$ )
$C'_{pL}$	specific heat of liquid ( $\text{kJ kg}^{-1} \text{K}^{-1}$ )
$D_{\text{CO}_2}$	diffusivity of CO <sub>2</sub> in K <sub>2</sub> CO <sub>3</sub> solution ( $\text{m}^2 \text{h}^{-1}$ )
$D_{g\text{CO}_2}$	diffusivity of CO <sub>2</sub> in gas ( $\text{m}^2 \text{h}^{-1}$ )
$d_p$	packing nominal size (m)
$E$	enhancement factor
$G$	molar velocity of gas ( $\text{kmol m}^{-2} \text{h}^{-1}$ )
$\hat{G}$	mass velocity of inert gas ( $\text{kg m}^{-2} \text{h}^{-1}$ )
$H$	solubility of carbon dioxide in solution ( $\text{kmol atm}^{-1} \text{m}^{-3}$ )
$h$	heat transfer coefficient in gas phase ( $\text{kJ m}^{-2} \text{h}^{-1} \text{K}^{-1}$ )
$\Delta H_{\text{CO}_2}$	heat of reaction and absorption of CO <sub>2</sub> ( $\text{kJ kmol}^{-1}$ )
$\Delta H_{\text{H}_2\text{O}}$	heat of vaporization of water ( $\text{kJ kmol}^{-1}$ )
$I$	ionic strength of solution ( $\text{kg ion m}^{-3}$ )
$k$	pseudo first order rate constant ( $\text{h}^{-1}$ )
$k_{\text{Am}}$	second order rate constant of amine ( $\text{m}^3 \text{kmol}^{-1} \text{h}^{-1}$ )
$k_{\text{OH}}$	forward rate constant of reaction (4) ( $\text{m}^3 \text{kmol}^{-1} \text{s}^{-1}$ )

backward rate constant of reaction (4) ( $s^{-1}$ )  
 as side mass transfer coefficient  
 ( $cmol\ h^{-1}\ m^{-2}\ atm^{-1}$ )  
 overall mass transfer coefficient  
 ( $cmol\ h^{-1}\ m^{-2}\ atm^{-1}$ )  
 as side mass transfer coefficient ( $kmol\ h^{-1}\ m^{-2}$ )  
 liquid side mass transfer coefficient ( $m\ h^{-1}$ )  
 first ionization constant for carbonic acid  
 ( $cmol\ m^{-3}$ )  
 second ionization constant for carbonic acid  
 ( $cmol\ m^{-3}$ )  
 molar velocity of liquid ( $kmol\ m^{-2}\ h^{-1}$ )  
 liquid mass flow rate ( $kg\ h^{-1}$ )  
 heat of vaporization of water ( $kJ\ kmol^{-1}$ )  
 Lewis number  
 mass transfer flux of kth component ( $kmol\ m^{-2}\ h^{-1}$ )  
 partial pressure of kth component in gas phase (atm)  
 equilibrium vapor pressure of kth component  
 in gas phase (atm)  
 partial pressure of kth component in the  
 liquid–gas interface (atm)  
 universal gas constant ( $m^3\ atm\ kmol^{-1}\ K^{-1}$ )  
 cross sectional area of column ( $m^2$ )  
 as temperature (K)  
 liquid temperature (K)  
 mole fraction of kth component in the liquid phase  
 mole fraction of kth component in the gas phase  
 spatial variable along the height of the column (m)

#### Symbols

carbonation ratio  
 gas phase viscosity ( $kg\ m^{-1}\ h^{-1}$ )  
 liquid phase viscosity ( $kg\ m^{-1}\ h^{-1}$ )  
 gas phase density ( $kg\ m^{-3}$ )  
 liquid phase density ( $kg\ m^{-3}$ )  
 stoichiometric weight percent of  $K_2CO_3$

#### References

Benson, J.H. Field, R.M. Jimson,  $CO_2$  absorption employing hot potassium carbonate solution, *Chem. Eng. Prog.* 50 (1954) 356–364.  
 Benson, J.H. Field, W.P. Haynes, Improved process for  $CO_2$  absorption using hot carbonate solution, *Chem. Eng. Prog.* 52 (1956) 438.

- [3] H.E. Benson, J.H. Field, New data for hot carbonate process, *Petrol. Refinery* 39 (1960) 127–132.
- [4] H.E. Benson, R.W. Parish, Improved benfield process, *Hydrol. Process.* 53 (4) (1974) 81–88.
- [5] F.C. Riesenfeld, J.F. Mallowney, Giammarco–Vetrocoke processes, *Petrol. Refinery* 38 (5) (1959) 161–167.
- [6] D.H. Killeffer, Promotion of mass transfer in carbonate solution, *Ind. Eng. Chem.* 29 (1937) 1293–1298.
- [7] A.L. Shrier, P.V. Danckwerts, Promotion effect of amines in carbonate solutions at room temperature, *Ind. Eng. Chem.* 8 (1969) 581–590.
- [8] G. Astarita, D.W. Savage, Promotion of  $CO_2$  mass transfer in carbonate solutions, *Chem. Eng. Sci.* 36 (1981) 581–588.
- [9] D.W. Savage, G. Astarita, Amines as rate promoters for carbon dioxide hydrolysis, *Faraday Discuss. Chem. Soc.* 77 (1984) 17–31.
- [10] G. Vazquez, F. Chenlo, G. Periera, Enhancement of the absorption of  $CO_2$  in alkaline buffer solutions: joint action of two enhancer, *Ind. Eng. Chem. Res.* 38 (1999) 2160–2162.
- [11] D. Sanyal, N. Vasishtha, D.N. Saraf, Modeling of carbon dioxide absorber using hot carbonate process, *Ind. Eng. Chem. Res.* 27 (1988) 2149–2156.
- [12] M.M. Suenson, C. Georgaklis, L.B. Evans, Steady-state and dynamic modeling of a gas absorber–stripper system, *Ind. Eng. Chem. Fundam.* 24 (1985) 288–295.
- [13] Shiraz Petrochemical Complex, Ammonia Plant, Operating Data of Benfield Process, 2002.
- [14] P.V. Danckwerts, *Gas–Liquid Reactions*, McGraw-Hill, 1970.
- [15] P.V. Danckwerts, M.M. Sharma, The absorption of carbon dioxide into solutions of alkalis and amines, *Chem. Eng.* 44 (1966) 244–280.
- [16] E. Leder, The absorption of  $CO_2$  into chemically reactive solutions at high temperature, *Chem. Eng. Sci.* 26 (1971) 1381–1390.
- [17] A.Z. Kashkooli, M.Sc. Thesis, Shiraz University, Shiraz, Iran 2002.
- [18] J.S. Tosh, H.E. Benson, J.H. Field, Equilibrium study of the system  $K_2CO_3$ ,  $CO_2$ ,  $KHCO_3$  and water, *Bur. Min. Rep. Invest.* 23 (1959) 54–84.
- [19] G. Astarita, *A Gas Treating with Chemical Solvent*, Wiley, New York, 1983.
- [20] D.W. Van Krevelen, P. Hofstijzer, Kinetics of simultaneous absorption and chemical reaction, *Chem. Eng. Prog.* 44 (1948) 529–534.
- [21] D.W. Savage, G. Astarita, S. Joshi, Chemical absorption and desorption of carbon dioxide from hot carbonate solutions, *Chem. Eng. Sci.* 35 (1980) 1513–1522.
- [22] R.C. Reid, J.M. Prausnitz, T.K. Sherwood, *The Properties of Gases and Liquids*, McGraw-Hill, New York, 1977.
- [23] G.P. Bocard, B.J. Maryland, Investigation of the equilibrium between vapor, carbon dioxide and hot potassium carbonate solutions, *Hydrol. Proc. Petrol. Refinery* 41 (1962) 128–135.
- [24] A.L. Kohl, F.C. Risenfeld, *Gas purification*, Houston, TX, Gulf, 1985.
- [25] L. Fox, *Numerical Solution of Two-Point Boundary Problems in Ordinary Differential Equation*, Oxford University Press, Oxford, London, 1957.
- [26] H.B. Keller, *Numerical Method for Two-Point Boundary Value Problems*, Blaisdell, Walthams, MA, 1968.
- [27] S.M. Roberts, J.S. Shipman, *Two-Point Boundary Value Problems: Shooting Methods*, American Elsevier, New York, 1972.