

**Optimization Approaches & Strategies for Distillation Column  
Sequencing Separation for Olefins Production**

by  
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ID: 7045

Dissertation submitted in partial fulfillment of the requirements for the  
Bachelor of Engineering (Hons)  
(Chemical Engineering)

**JANUARY 2009**

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**CERTIFICATION OF APPROVAL**

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Approved by,

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January 2009

## **CERTIFICATION OF ORIGINALITY**

This is to certify that I am responsible for the work submitted in this project, that the original work is my own except as specified in the references and acknowledgements, and that the original work contained herein have not been undertaken or done by unspecified sources or persons.

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(LEE TZU FEN)

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## ABSTRACT

This main objective of this project is to develop a mathematical model for determining the optimal design of distillation sequencing for olefin production. The mathematical model with optimization procedure for the integration of olefin flow from refinery to a petrochemical plant is based on a process flowsheet superstructure representation that embeds all possible alternatives for the distillation sequencing. The model formulation includes material balances with fixed split fractions and logical constraints for representing design specifications and structural specifications based on engineering knowledge and past design experience and heuristics. Additionally, big-M logical constraints relating the continuous variables of flowrates to the binary 0–1 variables of column existence are incorporated. In this work, the intermediate superstructure representation is adopted to represent the distillation sequencing for olefin production because it has been shown to provide good computational performance in obtaining the global optimal solution (Caballero and Grossmann, 1999). The optimization model is investigated using different feedstock; ethane from Ethylene Polyethylene (M) Sdn. Bhd (EPMSB) and naphtha from University of Manchester's Process Integration (2005). By using different feedstocks, the computational results yield the same optimal sequencing. Furthermore, ~~The—the~~ optimal distillation sequencing with this model formulation is validated with the existing olefin plant. It is proved that the optimal distillation sequencing is consistent with the common heuristic in process plant synthesis. The optimization model is also investigated using integer cuts in order to check that they agree or conform to the heuristic for distillation sequencing. It is proved that the optimum solution has the least total mass flow rate.

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## ABBREVIATIONS & NOMENCLATURE

The following abbreviations and nomenclatures are used throughout this interim report.

Abbrev.	Full name
STN	State Task Network
SEN	State Equipment Network

### Sets and Indices

- $i$  process units
- $j$  process streams
- $k$  ~~final product~~ task as represented by a column

### Parameters

- TOTFEED total feed flowrate
- SPLTFRC(T,S) split fraction associated with task and stream

### Continuous Variables

- F(T) Flowrate associated with task
- F<sub>Sm</sub> set of all columns having intermediate product m as feed
- P<sub>Sm</sub> set of all columns that produce a given intermediate product m as distillate or bottoms
- IP set of all intermediate products

### Binary Variables

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$y_i$  existence of process unit  $i$

$z_j$  existence of material stream  $j$

~~where  $PS_m$  is the set of all columns that produce a given intermediate product  $m$  as distillate or bottoms;~~

~~$FS_m$  is the set of all columns having intermediate product  $m$  as feed;~~

~~$IP$  is the set of all intermediate products~~

# CHAPTER 1

## INTRODUCTION

### 1.1. Background Of Study

The goal of conceptual design (process synthesis) is the identification of best flow sheet structure system that must carry out for a specific task, such as conversion of raw material into a product or separation of a multi component mixture. To accomplish this goal, many alternatives design must be considered. There are three major approaches for determining an optimal topology or configuration of a petrochemical plant:

1) The heuristic and evolutionary approach

Heuristic method proposed by douglas relies on intuition and engineering knowledge. This method uses the 'onion diagram' approach where it considers the critical equipment like the reactors before progressing to the separation units and finally to heat transfer units. Douglas's method enables flow sheet structures to be determined at near optimal solution and at a faster time. (douglas, 1988)

2) Thermodynamic targets and physical insight approach (linhoff et al., 1993)

This method exploits the basic physical principles such as thermodynamics like pinch technology. This approach yields designs that features high energy efficiency and often near optimal solutions.

3) Algorithmic approach (Grossmann, 1996)

The algorithmic approach uses mathematical programming techniques. The formulation is based upon a superstructure that represents all possible process

flow sheets. It includes the simultaneous and rigorous considerations of all factors.

The study is aimed at exploring the third approach which is the algorithm approach to obtain the methodology for an optimal naphtha separation topology design.

### **1.2. Problem Statement**

The problem addressed in this study can be stated as follows: given are the availability and composition olefin feedstock, product demands, coefficient for fixed cost and variable cost, and availability of process units in terms of different choices of task and equipment, and the interconnections among them. The problem in this study is to synthesize the optimal flow sheet distillation sequence and satisfies the criteria of cost.

The basic assumptions made in this study are:

1. Each distillation column performs a simple split. (i.e. One feed and two products)
2. Each distillation column performs a sharp separation ( i.e. a component appears entirely on its own as a products; product is 100% pure component)

### **1.3. Objectives**

This main objective of this research is to develop a Mixed-Integer Linear program (MILP), whose solution will determine the optimal design of distillation sequences for producing olefins. The main variable in the proposed modeling approach are: (1) the flow rates of the material streams; (2) the selection of the process units to be selected and the interconnectivities among the selected units that give rise to their sequence. In order to achieve the main objective, the following sub-objectives are formed.

1. To consider a suitable superstructure representation for olefin production such as STN, SEN, and intermediate;

2. To derive a mathematical programming model with discrete and continuous variables to predict an optimum flow sheet design that includes linear mass balances and constraints for the selection of the alternative routes for the olefin production;
3. To solve the optimization model for optimal separation sequences for olefin production using modeling language interface GAMS (general algebraic modeling language);

#### **1.4. Scope**

The scope of the research is to formulate a mixed integer linear programming model (MILP) for olefin production. The scope for final year project I (fypI) is to develop the suitable superstructure for olefin production, formulate the linear mass balance, and develop logical constraints. The scope for final year project II (fypII) is to model the MILP model in GAMS and validate the results obtained with literature review.

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## CHAPTER 2

### LITERATURE REVIEW

#### 2.1 OLEFIN FEEDSTOCK

The typical feedstocks for petrochemical industry for olefin production are ethane, propane, naphtha and gas oil. Regardless of the feedstock, olefin production is a gigantic destroyer of energy, an enormous heat sink. Olefin production is very energy intensive (Hatch and Matar, 1981).

The gaseous feedstocks for ethylene production are ethane, propane, and *n*-butane, in various mixtures and proportions of these compounds (Hatch and Matar, 1981). The advantage of ethane as a feedstock is a high ultimate yield combined with a minimum of coproducts. The ultimate yields of ethylene is about 80% based on the ethane is being recycled to extinction (Hatch and Matar, 1981). For propane feedstock, it gives a lower ethylene yield and a larger quantity of coproducts than ethane feedstock (Figure-Table 1).

The major liquid feeds/feedstock for olefins production are light virgin naphtha, full range naphtha, reformer raffinate, atmospheric gas oil, vacuum gas oil, resids, and crude oil. The feedstock are usually cracked with lower residence times and higher temperatures and with higher steam dilution ratios than is used for gas feedstocks (Hatch and Matar, 1981). The advantage of naphtha over gas feedstocks is the wider spectrum of coproducts (Figure-Table 1). The important olefins and aromatics used for production in chemical industry are ethylene, propylene, butadiene, BTX. Thus, we wish to obtain a variety of coproducts. Figure-Table 1 shows that as feedstocks progress

from ethane through heavier fractionation with lower  $H_2$  content, the yield of ethylene is reduced and the variety of coproducts are increased.

**Table 1 Typical yield of feedstocks in olefin production**

Petrochemicals: Olefin				
Typical yields are:				
	Feedstocks			
	Ethane (wt %)	Propane (wt %)	Naphtha (wt %)	Gas Oil (wt %)
H <sub>2</sub>	3.6	1.3	0.8	0.6
CH <sub>4</sub>	4.2	24.7	15.3	10.6
C <sub>2</sub> H <sub>2</sub>	0.2	0.3	0.7	0.4
C <sub>2</sub> H <sub>4</sub>	48.2	34.5	29.3	24.0
C <sub>2</sub> H <sub>6</sub>	40.0	4.4	3.8	3.2
C <sub>3</sub> H <sub>4</sub>		0.3	1.1	1.0
C <sub>3</sub> H <sub>6</sub>	1.3	14.0	14.1	14.5
C <sub>3</sub> H <sub>8</sub>		10.0	0.3	0.4
1,3-C <sub>4</sub> H <sub>6</sub>			4.8	4.7
C <sub>4</sub> H <sub>8</sub>	1.6	3.7	4.2	4.5
C <sub>4</sub> H <sub>10</sub>			0.3	0.1
Pyrolysis	0.9	5.9	21.0	18.4
Gasoline				
Fuel Oil	-	0.9	3.8	17.6

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**Petrochemicals: Olefins**

• Typical yields are:

	Feedstocks			
	Ethane	Propane	Naphtha	Gas Oil
H <sub>2</sub>	3.6	1.3	0.8	0.6
CH <sub>4</sub>	4.2	24.7	15.3	10.6
C <sub>2</sub> H <sub>2</sub>	0.2	0.3	0.7	0.4
C <sub>2</sub> H <sub>4</sub>	48.2	34.5	29.3	24.0
C <sub>2</sub> H <sub>6</sub>	40.0	4.4	3.8	3.2
C <sub>3</sub> H <sub>4</sub>		0.3	1.1	1.0
C <sub>3</sub> H <sub>6</sub>	} 1.3	14.0	14.1	14.5
C <sub>3</sub> H <sub>8</sub>		10.0	0.3	0.4
1,3-C <sub>4</sub> H <sub>6</sub>			4.8	4.7
C <sub>4</sub> H <sub>8</sub>	} 1.6	} 3.7	4.2	4.5
C <sub>4</sub> H <sub>10</sub>			0.3	0.1
pyrolysis gasoline	0.9	5.9	21.0	18.4
fuel oil	-	0.9	3.8	17.6

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(retype) Figure 1 Typical yield of feedstocks in olefin production

An olefins plant, which utilizes a liquid feedstock, requires an additional pyrolysis furnace for cracking coproduct ethane and propane and an effluent quench exchanger.

This is followed by an oil quench and a primary fractionator for fuel oil separation. In contrast, a gas cracker requires a simple direct-contact water quench tower off the cracking unit. A liquid feed cracker also contains a propylene tower and a methylacetylene removal unit. A unit for first stage hydrotreating of pyrolysis gasoline may also be included (Hatch and Matar, 1981).

## **2.2 Petrochemical Industry in Malaysia**

The availability of hydrocarbon feedstocks from indigenous oil and gas has led to the development of the petrochemical industry. The two ethane crackers in Kertih which use ethane from the six GPPs in Kertih and Tok Arun provide feedstock for the polyethylene plants, acetic acid plant and DOW PETRONAS ethylene derivatives complex. Condensates from the GPPs also provide feedstock to the aromatic plant in Kertih for the production of paraxylene and benzene.

Propane from the GPPs is the raw material for the propane dehydrogenation plant in Gebeng. This provides feedstock to the polypropylene and MTBE plants and also to the BASF Petronas highly integrated propylene derivatives complex for the production of acrylics, oxo alcohols, butanediol, butylacrylates, plasticizers and tetrahydrofurane.

Titan's integrated operation in Pasir Gudang-Tanjung Langsat, Johor includes a naphtha cracker which provides feedstock for its own production of polypropylene, polyethylene and aromatics. It also provides feedstock for the production of ethylene vinyl acetate (EVA). Naphtha is available from the petroleum refineries and Shell's middle distillates synthesis (MDS) plant in Bintulu, Sarawak. However a large proportion of the naphtha requirement is still being imported.

### Production of Petrochemical Feedstocks (as at January 2005)

Petrochemical Products	Capacity (mtpa)	Company/Refinery
Naphtha	2,380,000	<ul style="list-style-type: none"> <li>• Petronas Penapisan (Terengganu) Sdn Bhd</li> <li>• Petronas Penapisan (Melaka) Sdn Bhd</li> <li>• Malaysia Refinery Company Sdn Bhd</li> <li>• Shell Refinery Company (FOM) Bhd</li> <li>• Esso (Malaysia) Bhd</li> </ul>
Methane (sales gas)	2,000 mmscfd	<ul style="list-style-type: none"> <li>• Petronas Gas Berhad</li> </ul>
Olefins:		
<i>Ethane</i>	1,383,000	
<i>Propane</i>	1,799,000	
<i>Butane</i>	1,166,000	
<i>Condensate</i>	1,260,000	
Propane	148,400	<ul style="list-style-type: none"> <li>• Malaysia LNG Tiga Sdn Bhd</li> </ul>
Butane	273,900	
Liquefied Petroleum Gas (LPG)	137,700	
Ethylene	1,560,000	<ul style="list-style-type: none"> <li>• Titan Petrochemical (M) Sdn Bhd</li> <li>• Ethylene Malaysia Sdn Bhd</li> <li>• Optimal Olefins (M) Sdn Bhd</li> </ul>
Propylene	766,000	<ul style="list-style-type: none"> <li>• Titan Petrochemical (M) Sdn Bhd</li> <li>• MTBE (M) Sdn Bhd</li> <li>• Optimal Olefins (M) Sdn Bhd</li> </ul>
Benzene, Toulene and Xylene (BTX)	775,000	<ul style="list-style-type: none"> <li>• Titan Petrochemical (M) Sdn Bhd</li> <li>• Aromatics Malaysia Sdn Bhd</li> </ul>

Figure 1 Figure 2 Production of Petrochemical Feedstock (as at January 2005) (MIDA, 2005)

## **2.3 OVERVIEW ON PROCESS DESCRIPTION OF NAPHTHA CRACKING**

The optimization-based mathematical model for the integration of flow from a refinery to a petrochemical plant is based on a process flowsheet superstructure representation that embeds all possible alternatives for the design of an olefin plant.

### **2.3.1 CRACKING OR PYROLYSIS SECTION**

The primary process step in producing olefins from hydrocarbon feeds is thermal cracking, usually referred to as pyrolysis. This process converts the feed to lower molecular weight hydrocarbons at relatively high temperature and low pressure. Light naphtha is supplied to the cracker plant from storage tank via pumps. Pyrolysis is the heart of steam cracker. The naphtha feed is first entered to the convection section, where preheated to 650°C with a series of heat exchanger at the convection section. The naphtha is then vaporized with superheated steam and is passed into long, narrow tubes, which are made of chromium nickel alloys (ren et al., 2006). Recycle ethane and propane streams are mixed in the gas feed header while recycle C4 (hydrocarbon with four carbon atoms) are mixed preferentially with the fresh naphtha in the liquid feed header. Any excess of C4 will go to the gas feed header.

The cracking reactions take place mainly in the radiant section of the furnace, where the naphtha is cracked into smaller molecules via a free radical mechanism in the absence of catalyst. The free radicals lead to the formation of light olefins in gaseous state. The tubes in the radiant section are externally heated to 750-900°C (up to 1100°C) by fuel oil or gas fired burners (Ren et al., 2006). Dilution steam is added to reduce the hydrocarbon partial pressure to promote the production of olefins and minimize the rate of coke deposition. Periodic decoking is required to remove coke which accumulates gradually in the radiant coils and quench exchangers. The furnaces will be steam or air decoked when the tube metal temperature approaches its design limit.

Depending on the severity, naphtha is cracked into smaller molecules via a free radical mechanism in the absence of catalyst. Thus, the olefins are in the gaseous state. After

leaving the furnace, the hot gas mixture is subsequently quenched in the transfer line exchangers (TLE) to 550 – 650°C or lower to 400°C (Ren et al., 2006). Super high pressure (SHP) steam is generated (500 °c and 105 kg/cm<sup>2</sup>g) and is used in the turbine driver for the cracked gas compressor. Rapid cooling is necessary to avoid secondary reactions which convert valuable products to heavier materials that tend to cause fouling in the exchangers. The steam generation pressure is set so that the tube wall temperature is high enough to prevent condensation of hydrocarbon in the TLE's.

### **2.3.2 PRIMARY FRACTIONATION, COMPRESSION AND QUENCH SYSTEM**

Primary fractionation applies to the liquid feedstock of naphtha and gas oil feed only. In the primary fractionation section, gasoline and fuel oil streams (rich in aromatics) are condensed and fractionated. While this liquid fraction is extracted, the gaseous fraction is desuperheated in the quench tower by a circulating oil or water stream. The gaseous fraction is then passed through four or five stages of gas compression with temperatures at approximately 15-100 °C, then cooling and finally cleanup to remove acid gases, carbon dioxide and water. Most of the dilution steam is condensed, recovered and recycled. Product of primary fractionation are fuel oil and BTX or aromatic gasoline which consists benzene, toluene, and xylene. The problem faced with compression is fouling with cracked gas compressors and after coolers. The build-up of polymers on the rotor and internal will leads to energy losses as well as mechanical problems. Wash oil and water used to reduce fouling (Ren et al., 2006).

Furnace effluent gas is cooled further by direct contact with circulating quench oil and fractionated in a quench oil tower to remove the heavy fraction. This quench oil material is stripped to control flash point and sent to storage as fuel oil product. The overhead from the quench oil tower will enter the quench water tower. Most of the dilution steam condenses in this tower, along with a portion of the gasoline fraction.

### **2.3.3 CAUSTIC WASHING & DRYING**

The caustic wash tower is installed to remove hydrogen sulphide, mercaptans, and carbon dioxide formed during the cracking process. These acid gases are removed from the cracked gas for the following purposes:

1. to meet product quality requirements on the ethylene and propylene products
2. to protect downstream catalytic operations, since some acid gas components are known to be catalyst poisons
3. to avoid corrosion
4. to avoid the possible formation of carbon dioxide ice within the cold process systems.

The caustic solution used in this process is caustic soda (sodium hydroxide). After four stages of compression, the acid gases of the cracked gas are removed by scrubbing the gas with circulating caustic solution in the caustic tower. The tower consists of three sections, only two of which provide the caustic scrubbing of the cracked gas. The middle and bottom sections are circulated with strong and weak caustic solutions, respectively. The top section is the water wash section, which washes the treated cracked gas to prevent caustic carryover into the downstream equipment.

Removal of acid gas at this point in the process allows all of the C4 and lighter hydrocarbons to be desulfurized together, eliminating the necessity to clean individual product streams. Overhead gas from the caustic tower is cooled with propylene refrigerant. The condensate is pumped forward to the high pressure (HP) depropanizer via the liquid dryer unit. Essentially, complete removal of water is necessary to prevent freeze-ups in subsequent low temperature equipment.

### **2.3.4 PRODUCT RECOVERY AND FRACTIONATION SECTION**

This is essentially a separation process through distillation, refrigeration, and extraction. Equipment includes chilling trains and fractionation towers, which include refrigeration, demethanizer, deethanizer and others which shown in Figure 4.

### **i. Depropanizer**

The dried gases are cooled and fed to the HP depropanizer, which separates the feed into an overhead vapor essentially free of C4 and heavier material and a bottoms product essentially free of C2 (hydrocarbon with two carbon atoms) and lighter material. Tower overhead vapor is compressed in the fifth stage of the cracked gas compressor. Net bottom flows to the low pressure (LP) depropanizer. The LP depropanizer produces a raw C3 (hydrocarbon with three carbon atoms) liquid distillate which is sent to C3 hydrogenation and a bottom stream which flows to the Debutanizer.

### **ii. Acetylene Removal**

Gas from the fifth stage of the cracked gas compressor is catalytically hydrogenated to remove acetylene. The reactor feed gas may either be cooled or heated, depending on the age and activity of the catalyst. Catalyst life is expected to be at least three years between regeneration. Three catalyst beds are used, with inter-cooling between beds to limit the temperature rise per bed. Essentially, all acetylene is converted to ethylene and ethane. Some of the methylacetylene and propadiene is converted to propylene. a spare reactor is not required because on-line regeneration is not required. Effluent from the reactor is cooled and dried in a secondary dryer to remove any trace quantities of water. Dried gas is cooled and partially condensed to provide reflux for the hp depropanizer.

### **iii. Demethanizer**

The effluent gas from the hydrogenation reactor is chilled by exchange with ethane recycle and successively colder levels of propylene and ethylene refrigeration. Liquids separated in the chilling train are fed to appropriate trays in the demethanizer prefractionator and demethanizer, according to composition. The prefractionator separates C3 and heavier material from C2 and lighter. The overhead vapor from the prefractionator, which contains essentially no C3 material, is sent to the demethanizer. The prefractionator bottom is sent to the deethanizer. The demethanizer makes a sharp separation between methane and ethylene.

#### **iv. Deethanizer & C2 splitter systems**

The deethanizer separates the feed into C2 and C3. The net overhead, consisting principally of ethylene and ethane, is taken as a liquid to a C2 splitter, while the net bottom is fed to C3 hydrogenation. The C2 splitter is a single tower operated at low pressure and temperature. Two feeds enter the tower; an ethylene rich vapor stream from the demethanizer and the overhead liquid product from the deethanizer.

The C2 splitter makes a sharp separation between ethylene and ethane. The ethylene product is pumped to high pressure, heated, and delivered to storage as a vapor product. If required, approximately 70% of the nameplate ethylene production can be subcooled and sent out entirely as a liquid product. Ethane bottom from the splitter is pumped and vaporized by exchange with demethanizer feed, and recycled to the cracking furnaces.

#### **v. C3 hydrogenation, C3 splitter, Debutanizers Systems**

Raw C3 from the deethanizer bottom and LP depropanizer overhead are catalytically hydrogenated to remove methylacetylene and propadiene. Methylacetylene and propadiene are converted to propylene.

Hydrogenated C3 are pumped to the C3 splitter which consists of two towers: a stripper and a rectifier. The overhead from the stripper is fed to the rectifier. Light ends, a result of the hydrogenation reaction, are removed in the pasteurizing section of the rectifier. Propylene is condensed and returned as reflux. Reflux for the stripper is obtained from the bottom of the rectifier. The rectifier overhead is condensed by cooling water. The polymer grade propylene product is taken off as a liquid side draw. A propane rich stream is removed as a vapor product from a location two trays above the bottom of the stripper to be recycle cracked in the furnaces. The net bottom liquid is recycled back to the LP depropanizer to remove any green oil produced in the C3 hydrogenation unit.

The debutanizer receives a liquid feed from the LP depropanizer bottom. A separation is made between C4 and C5 (hydrocarbon with five carbon atoms). The overhead is

condensed against cooling water. LP steam provides reboiler heat. The net overhead product is sent to the C4 hydrogenation unit and the bottom is combined with the distillate stripper bottom, cooled and sent to the pyrolysis gasoline hydrogenation unit.

**vi. C4 and Pyrolysis & Hydrogenation Unit**

The C4 hydrogenation unit selectively converts butadiene to butenes using high purity hydrogen. The unit consists of a single fixed-bed catalytic reaction system. The C4 product stream is recycle cracked in the cracking furnaces.

The pyrolysis gasoline hydrogenation unit is a one-stage catalytic reaction system to selectively hydrogenate diolefins and styrenic compounds. A stabilizer removes dissolved lights and a rerun tower removes gums from the gasoline product.

**vii. Olefin Cracking Process**

Based on UOP (2004), the Olefin Cracking process converts C<sub>4</sub> to C<sub>8</sub> olefins to propylene and ethylene at high propylene and ethylene ratio. See Figure 32, the Olefin Cracking Process features fixed bed reactors operating at temperatures between 500 and 600 °C and pressures between 1 to 5 bar gauge. The process utilizes a proprietary zeolitic catalyst and provides high yields of propylene. The catalyst minimizes the reactor size and operating costs by operating at high space velocities and high conversions and selectivities without requiring an inert diluent stream. A swing reactor system is used for catalyst regeneration. Separation facilities depend on how the unit is integrated into the processing system.

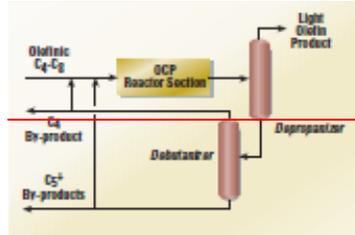
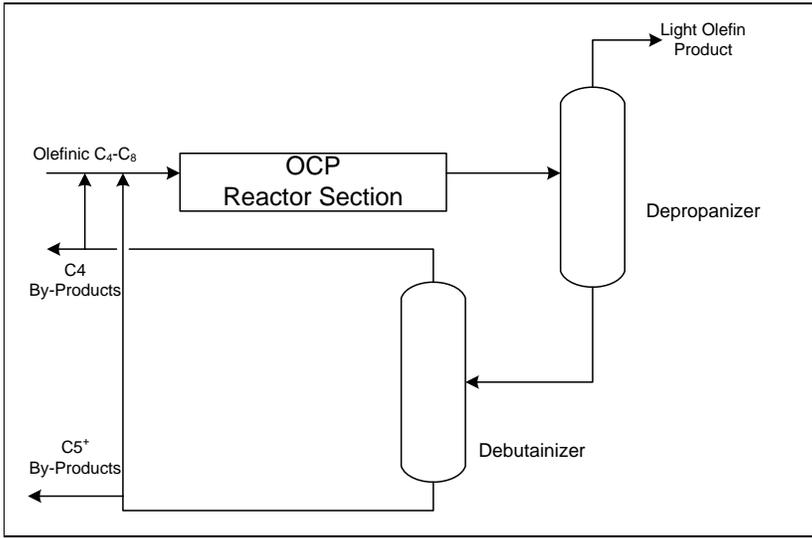


Figure 3-Figure 2 Description of Olefin Cracking Process

## 2.5 Overview of Process Description of Ethane Cracking

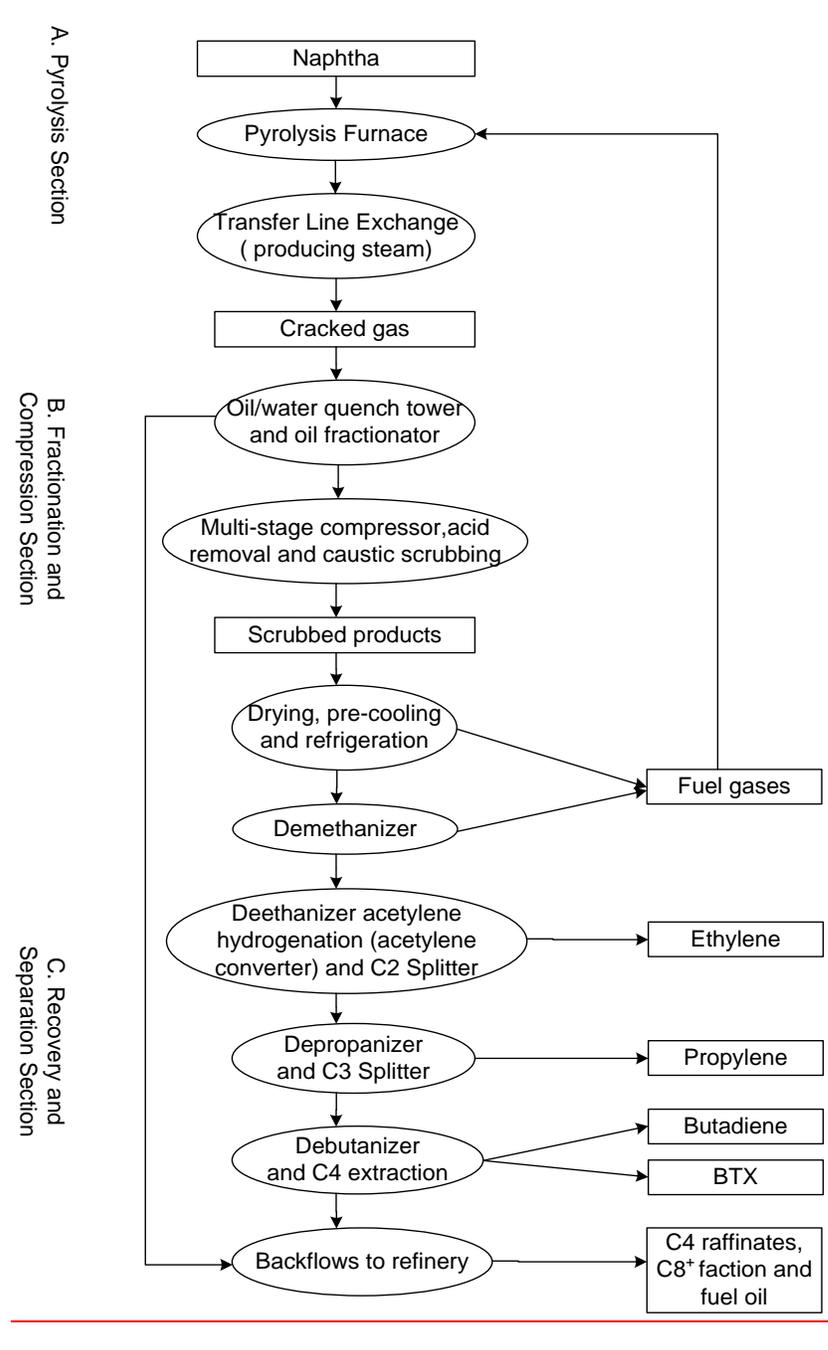
A typical ethane cracker has several identical pyrolysis furnaces in which fresh ethane feed and recycle ethane are cracked with steam as a diluent. The outlet temperature is usually in the 850 °C range. The furnace effluent is quenched in a heat exchanger and further cooled by direct contact in a water quench tower where the diluent steam is condensed. The water is recycled to the pyrolysis furnace. The cracked gas is compressed, acid constituents are removed, and the purified gas dried (Hatch and Matar, 1981).

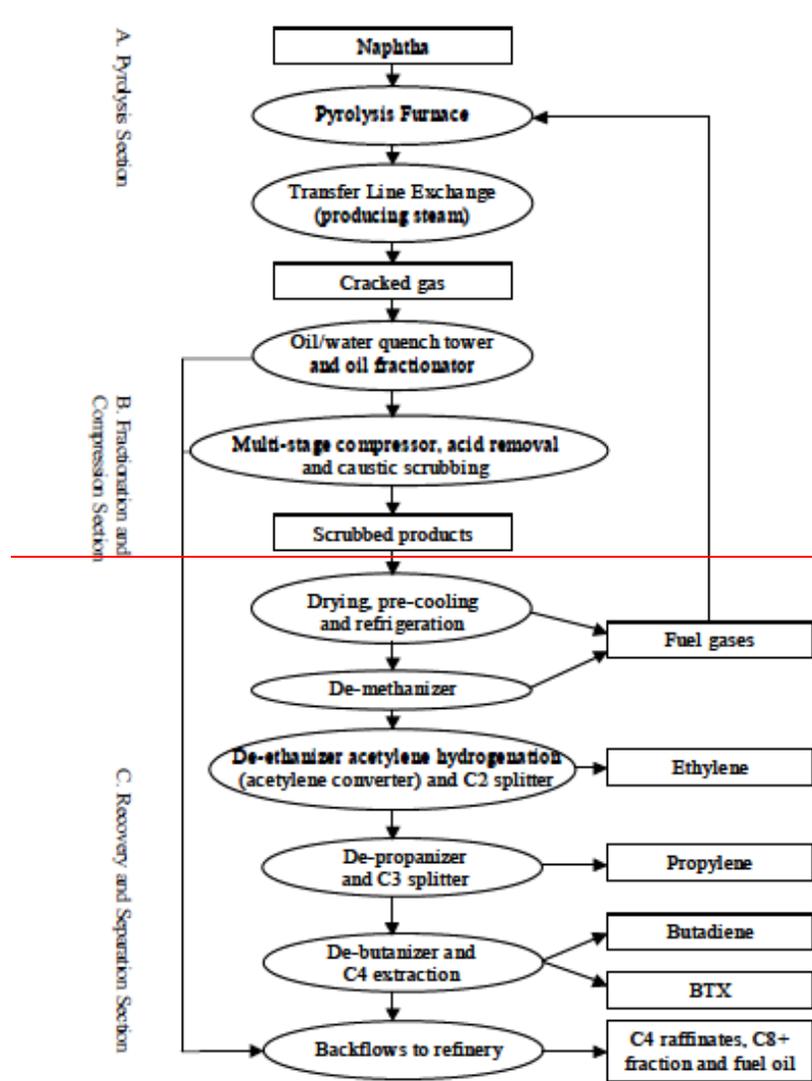
Hydrogen and methane are removed from the pyrolysis products in the demethanizer. The product stream is hydrogenated to remove acetylene, or the acetylene is separated as a product. Ethylene is separated in the ethylene tower from the unreacted ethane and higher boiling products. The ethane is recycled to extinction. The other products are separated and either sold, burned as fuel, or absorbed into a refinery operation (Hatch and Matar, 1981).

The liquid feedstocks are usually cracked with lower residence times and higher temperatures and with higher steam ratios than is used for gas feedstocks. The reaction section of the plants is essentially same as with the gas feedstocks but the design of the convection and quenching section are different (Hatch & Matar, 1981). An olefin plant which utilizes a liquid feedstock requires an additional pyrolysis furnace for cracking co product ethane and propane and an effluent quench exchanger. This is followed by an oil quench and a primary fractionator for fuel oil separation. In contrast, a gas craker requires a simple direct-contact water quench tower off the cracking unit. A liquid feed cracker also contains a propylene tower and a methylacetylene removal unit. A unit for first stage hydrotreating of pyrolysis gasoline may be included (Hatch & Matar, 1981).

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Figure 3 — A typical flow sheet of naphtha cracking plant (Ren, et al, 2006)

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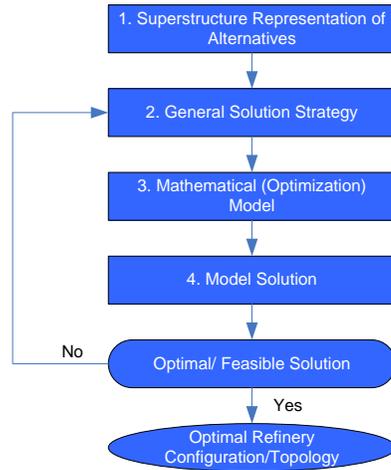
## CHAPTER 3

### Methodology

In general, the mathematical programming approach to process synthesis and design activities and problems consists of the following four major steps (Grossmann, 1990; Floudas, 1995, pp. 233.234; Novak et al., 1996):

1. Development of the superstructure to represent the space of topological alternatives of the naphtha flow to petrochemical plant configuration;
2. Establishment of the general solution strategy to determine the optimal topology from the superstructure representation of candidates;
  - If model is largely linear, simultaneous solution strategy is used.
  - If model is non-linear, sequential solution strategy is used (i.e. 1<sup>st</sup> stage, solve NLP (fix binary variables), 2<sup>nd</sup> stage, solve MILP using NLP solution).
3. Formulation or modeling of the postulated superstructure in a mathematical form that involves discrete and continuous variables for the selection of the configuration and operating levels, respectively; and
4. Solution of the corresponding mathematical form, i.e., the optimization model from which the optimal topology is determined.

The block diagram of the four major steps mentioned above is shown in Figure 54.



**Figure 5-Figure 4** Steps in mathematical programming approach to process synthesis and design problems (Grossman, 1990; Floudas, 1995; Novak et al., 1996)

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### 3.1 MILP Objective Function

In order to formulate a MILP program for this problem, it is important to devise an objective function which can be used to compare different alternatives. Thus, the objective function is to minimize the project cost, which is made up of capital expenses and operating expenses. This cost can be approximated by a function of the form of (1).

$$Cost = \sum_{k \in COL} CAPEX_k y_k + \sum_{k \in COL} OPEX_k F_k \quad (1)$$

Where **FC = Fixed cost associated with the column**

**V = Slope of line relating the column cost**

**F<sub>k</sub>** = stream flow rate associated with the column, *k* with process unit *i*

**CAPEX** = Capital Expenses

**OPEX** = Operating Expenses

**y<sub>k</sub>** = Binary variable denoting the existence or nonexistence of column *k*

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This objective function is subject to two types of constraints. Material balance constraints describe the permissible routes by which material may flow from one column in the superstructure to another. The second type of constraints which is integrality constraints, ensure consistency between the continuous variables and binary variables. The data of installed capital cost and operating cost are taken from Meyers (2005)( see Table 42).

**Table 221 Ethylene Production Cost Components<sup>a,b</sup>**

Location	N.E Asia/ W.Europe	Middle East	United States
Feedstock	Naphtha	Ethane	Ethane
Feedstock Cost (\$/t feed)	320 <sup>c</sup>	62 <sup>d</sup>	317 <sup>e</sup>
Net Feedstock Cost <sup>f</sup> (\$/t C <sub>2</sub> H <sub>4</sub> )	55	68	266
Energy Cost (\$/ t C <sub>2</sub> H <sub>4</sub> )	194	16	140
Fixed Cost <sup>g</sup> (\$/t C <sub>2</sub> H <sub>4</sub> )	66	56	51
Total Production Cost (\$/t C <sub>2</sub> H <sub>4</sub> )	315	140	457
Contract sales Price (\$/t C <sub>2</sub> H <sub>4</sub> )		650-700	

<sup>a</sup>Amortization costs for capital investment are excluded.

<sup>b</sup>Cost basis: first quarter 2004

<sup>c</sup>N.E.Asia/W.Europe naphtha cost = approx. \$37.5/bbl (130% crude price)

<sup>d</sup>Middle East ethane cost = \$1.25/MMBtu

<sup>e</sup>United States ethane cost = \$ 5.45/MMBtu natural gas + \$1.0/MMBtu extraction cost

<sup>f</sup>Net feedstock cost = feedstock cost – price of total nonethylene co-products

<sup>g</sup>Fixed cost include labour, supervision, maintenance, insurance , overhead.

### 3.2 Logical Constraints

The propose procedure to develop the logical relationships in the model is as below:

1. Associate Boolean Variables with every note in the model.

Boolean variables  $Y$  is used to represent the existence of all the units ( $U_n$ ) in the superstructure while  $Z$  is used to represents the splitters, mixer, sources and sinks.

- a. Mixer:

Mixes two or more streams, no other unit operation is involved

- b. Splitter:

Splits a stream into multiple streams, no other unit operation is involved.

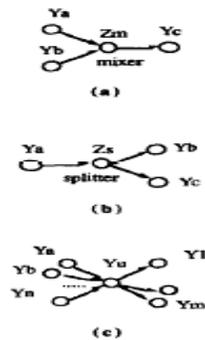
- c. Unit:

Including units that perform a change in compositions, pressure and temperature in the output streams, e.g. reactor, distillation columns.

- d. Sources and sinks:

Inlet and outlet of the process flowsheet.

2. Develop relationships between Boolean variables (Figure 65).



**Figure 5 Figure 6.** Nodes in the graph of a superstructure: (a) mixer; (b) splitter; and (c) Un component.

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a. Mixer:

$$Z_m \Rightarrow Y_a \vee Y_b$$

$$Z_m \Rightarrow Y_c$$

If  $Y_a \vee Y_b \Rightarrow Z_m$  and  $Y_c \Rightarrow Z_m$  are also valid, then the relations can be written as  $Y_a \vee Y_b \Leftrightarrow Z_m$  and  $Y_c \Leftrightarrow Z_m$ , respectively.

b. Splitter:

$$Z_s \Rightarrow Y_a$$

$$Z_s \Rightarrow Y_b \vee Y_c$$

If  $Y_a \Rightarrow Z_s$  and  $Y_b \vee Y_c \Rightarrow Z_s$  are also valid, the relations can be written as  $Z_s \Leftrightarrow Y_a$  and  $Z_s \Leftrightarrow Y_b \vee Y_c$  respectively.

c. Units  $u \in U_n$  :

$$Y_u \Rightarrow Y_a \wedge Y_b \dots \wedge Y_n$$

$$Y_u \Rightarrow Y_a \wedge Y_b \dots \wedge Y_m$$

### 3. User specification

User specifications limit on the unit selection and also take into account of the availability of the feed streams. The basic relation of Boolean Variable, Y with linear inequalities of binary variable, y is given in Table 23.

**Table 332** Constraint representation of logical relations as algebraic linear inequalities  
(Adapted from Raman and Grossmann (1991) and Williams (1999))

Logical operator	Logic proposition	Logical Boolean expression	Representation as algebraic integer linear inequality/equality constraint
Logical OR		$Y_1 \vee Y_2 \vee \dots \vee Y_r$	$y_1 + y_2 + \dots + y_r \geq 1$
Logical AND		$Y_1 \wedge Y_2 \wedge \dots \wedge Y_r$	$y_1 \geq 1$ $y_2 \geq 1$ $\dots$ $y_r \geq 1$
Implication	$Y_1 \Rightarrow Y_2$ is logically equivalent to $\neg Y_1 \vee Y_2$	$\neg Y_1 \vee Y_2$	$(1 - y_1) + y_2 \geq 1$ $y_1 - y_2 \leq 0$ $y_1 \leq y_2$
Equivalence	$Y_1$ if and only if $Y_2$ $(Y_1 \Rightarrow Y_2) \wedge (Y_2 \Rightarrow Y_1)$ which can also be written as: $Y_1 \Leftrightarrow Y_2$	$(\neg Y_1 \vee Y_2) \wedge (\neg Y_2 \vee Y_1)$	$y_1 = y_2$
Exclusive OR (EOR)	Exactly one of the variables is true	$Y_1 \oplus Y_2 \oplus \dots \oplus Y_r$	$y_1 + y_2 + \dots + y_r = 1$
Classification	$Q = \{Y_1, Y_2, \dots, Y_r\}$ $Q$ is true if any of the variables inside the brackets are true		$y_q = y_1 + y_2 + \dots + y_r$

The systematic procedure to convert a logical expression into its corresponding conjunctive normal consists of applying the following three steps to each logical proposition (Raman and Grossmann, 1991):

1. replace the implication by its equivalent disjunction:

$$Y_1 \Rightarrow Y_2 \Leftrightarrow \neg Y_1 \vee Y_2;$$

2. move the negation inward by applying DeMorgan's Theorem:

$$\neg(Y_1 \wedge Y_2) \Leftrightarrow \neg Y_1 \vee \neg Y_2;$$

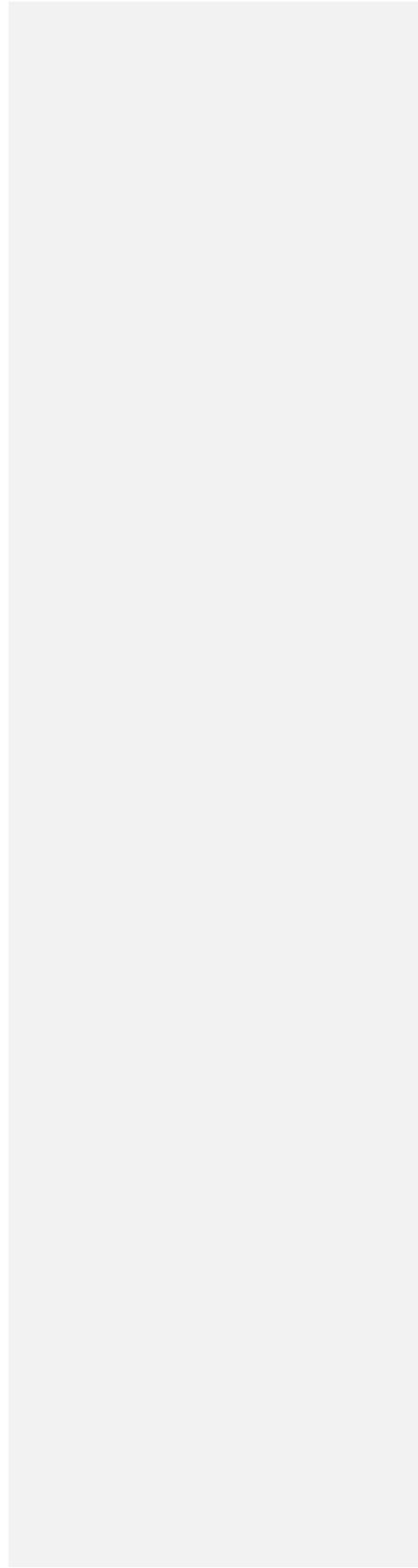
$$\neg(Y_1 \vee Y_2) \Leftrightarrow \neg Y_1 \wedge \neg Y_2;$$

3. recursively distribute the "OR" over the "AND" by using the following equivalence:

$$(Y_1 \wedge Y_2) \vee Y_3 \Leftrightarrow (Y_1 \vee Y_3) \wedge (Y_2 \vee Y_3)$$

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### 3.3 — Switching Constraints

To ensure that the non-existence of a process unit results in the corresponding input flowrates to the unit assuming the value of zero, we consider the formulation of big- $M$  logical constraints to impose the relations between the continuous variables, which in our case represent the flowrates of the streams, and the discrete binary 0–1 variables, which denote the existence of the streams and process units.

The general formulation of the big- $M$  logical constraints is given by:

$$F_k \leq M_k y_k \quad (2)$$

where  $F_k$  = total flowrate of an input stream for process unit  $k$  in kg/day,  
 $M_k$  = maximum capacity of process unit  $k$   
 $y_k$  = existence or non-existence of process unit  $k$ .

We could see that when  $y_k = 0$  (unit does not exist), then the constraint (2) becomes:

$$F_k \leq 0 \quad (3)$$

but flowrate variables are either zero or takes on positive values, so equation (3) becomes  $F_k = 0$ , which stipulates the condition of zero input flowrate into a non-existing unit. When  $y_k = 1$  (unit exists), then the constraint (2) becomes:

$$F_k \leq M_k \quad (4)$$

which means that the input flowrate is bounded from above by the value of the big- $M$  constant. Here, it is clear that a suitable value for the big- $M$  constant is the maximum capacity of the unit.

For example equation (5), if the maximum capacity of a distillation column is equals to  $100 \text{ m}^3$ , then the big- $M$  logical constraint for that unit becomes

$$F_k \leq (100 \text{ m}^3) y_k \quad (5)$$

This constraint (4) is usually written for the input flowrate because it can be related to the output flowrates through the material balances.

The big- $M$  logical constraints are also sometimes termed as switching constraints in the literature (Pardin, 1998, p. 558). As mentioned, the main function of the switching constraints is to enforce the condition that no output flow exists if the unit does not exist. By extension, these constraints can be written as  $r_i \leq M_i z_i$  to relate the stream flowrate to the binary variable  $z_i$ , denoting the existence of the stream itself (instead of the unit from where it is produced). In our proposed approach, this is written for each column with the big- $M$  constant, taken to be an arbitrarily large number, 1000, which it acts as an upper bound for the corresponding feed flow rate of the initial mixture.

### 3.4 — Linear Material Balances

According M.J.Andrecovich and A.W. Westerberg (1985), material balance constraints relate material flows into and out of columns in the superstructure. Each column separates its feed into two products streams whose amounts are related to the feed flow by equation (6)

$$\begin{aligned} D_k &= \xi_D F_k \\ B_k &= \xi_B F_k = (1 - \xi_D) F_k \end{aligned} \quad (6)$$

Where  $\xi_D$  is the split fraction of the feed to column,  $k$  which leaves in the distillate and  $\xi_B$  is the split fraction that leaves in the bottoms. The constraint is written for each product produced by columns in the structure must equal to the amount of that intermediate product fed to columns which further separate the product. That is

$$\sum_{k \in PS_m} \xi_k F_k - \sum_{k \in FS_m} F_k = 0 \quad m \in IP \quad (7)$$

Where  $PS_m$  is the set of all columns which produce a given intermediate product  $m$  as distillate or bottoms,  $FS_m$  is the set of all columns having intermediate product  $m$  as

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feed,  $F$  is the total flow rate to a column,  $IP$  is the set of all intermediate products, and  $\xi$  is the split fraction relating distillate or bottoms flows to feed flows. This constraint (7) is written for each intermediate product.

A similar expression is necessary for the feed to the distillation system:

$$\sum_{k \in FS_p} F_k = F_{TOT} \quad (8)$$

Refer to equation (8), the total feed to the system must equal the sum of the feeds to all columns which process some portion of the feed stream.

## CHAPTER 4

### OPTIMIZATION MODEL FORMULATION

Due to time constraint, the project scope is narrowed down to the separation subsystem of the superstructure. An alternative superstructure representation that is proposed by Caballero and Grossmann (1999), termed simply as the intermediate representation is employed to represent the separation subsystem. In this project, intermediate superstructure representation was used for the distillation sequencing for olefin production.

#### 4.1 Intermediate Superstructure Representation

Intermediate representation possesses the characteristics between the state–task network (STN) and the state–equipment network (SEN) superstructure representation.

For STN, the tasks and states are defined while the equipment assignment is generally unknown (See Figure 67). For SEN, tasks and equipment are defined while the assignment of tasks to equipment must be determined (Yeomans and Grossmann, 1999) (See Figure 87). In distillation sequencing problem, both SEN and STN are extreme cases because the number of columns is equal to the number of tasks for STN while the number of columns in SEN is the minimum necessary to perform the separation. Table 3-4 shows the comparison between STN and SEN.

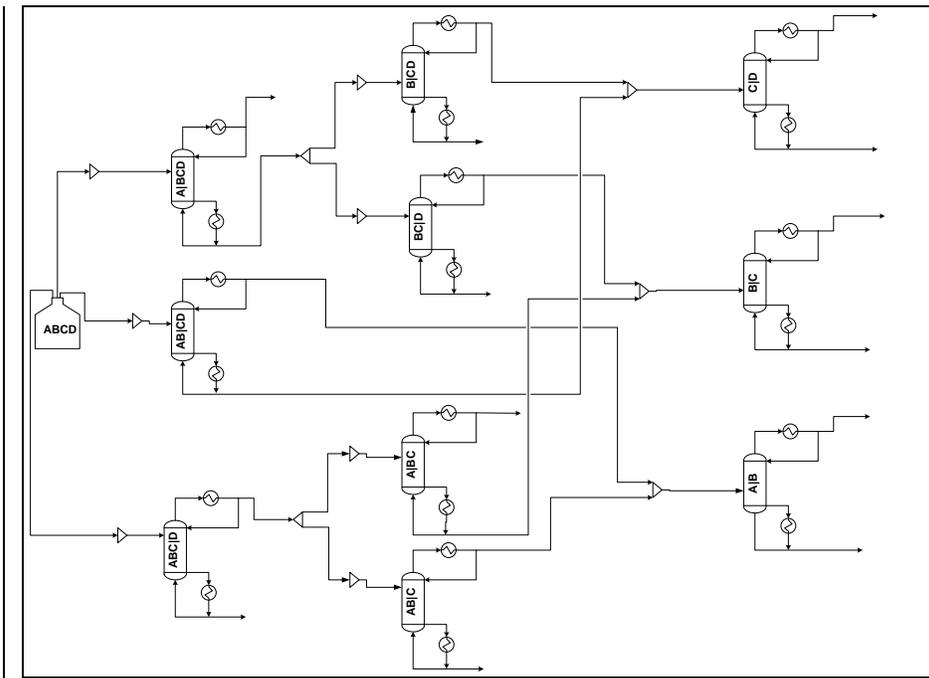
Referring to Figure 89, the number of columns in intermediate representation is in between these two extreme separations/cases (Caballero and Grossmann, 1999). Hence,

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intermediate representation superstructure will involve less number of equations compared to STN representation superstructure. Intermediate representation has shown

a good performance in reaching the global optimal solution (Caballero and Grossmann, 1999). Note also that for intermediate representation, both mixers and splitters are “single choice”, that is, only one input stream from the mixer or only one output stream from the splitter takes a non-zero value (i.e., a value different from zero). A contribution of this work pertaining to systematic superstructure generation is on how we demonstrate that the intermediate representation of Caballero and Grossmann (1999) can be readily and conveniently extended to include the representation of reactors (in this case, the catalytic hydrogenation reactor, the methyl acetylene and propadiene reactor (MAPD), the C<sub>4</sub> hydrogenation reactor, and the gasoline hydrogenation reactor (which is basically a hydrotreater)).



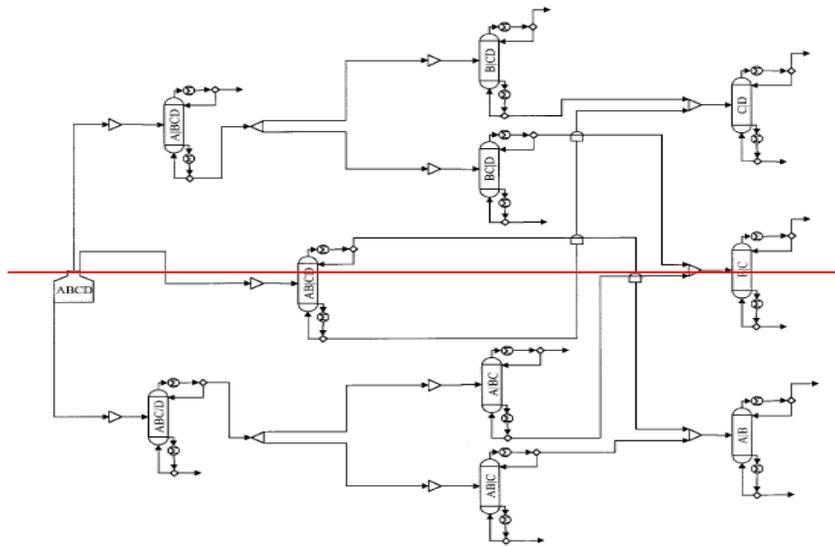


Figure 67 STN Representation for a mixture of four components (Caballero & Grossmann, 1999)

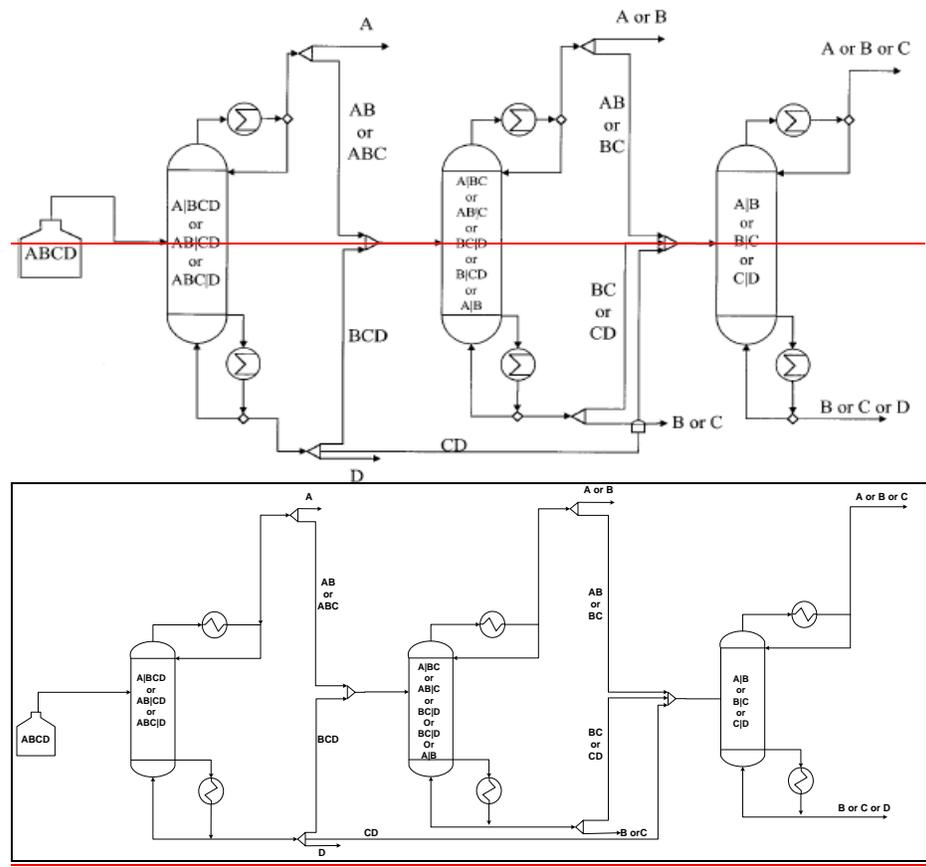


Figure 8-7 SEN Representation for a mixture of four components (Caballero & Grossmann, 1999)

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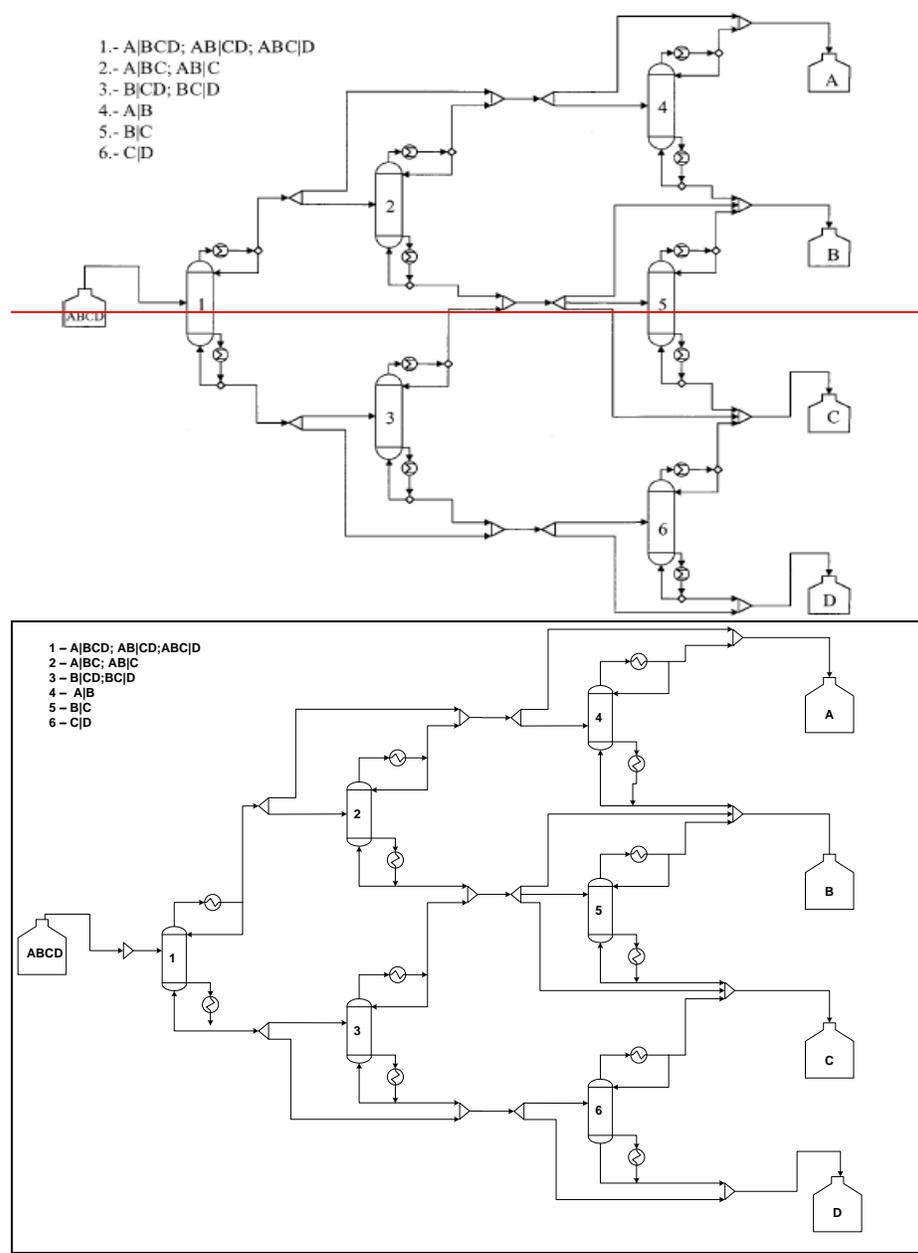


Figure 9-8 Intermediate Representation for a mixture of four components (Caballero & Grossmann, 1999)

**Table 443 Comparison between STN and SEN**

	STN	SEN
Characteristic	Concerned with the selection of tasks, leaving the equipment assignment (or selection) to a second stage	Concerned with the selection of equipment, leaving the selection (or assignment) of tasks to a second stage
Number of Columns	No. of columns = no. of tasks	No. of columns = minimum necessary to perform the separation (in the case that we are considering $(N - 1)$ columns))
Difference	One task one equipment (OTOE) Each task is assigned to a single equipment unit. If a task can be executed by two different equipments, the tasks will have to be redefined to distinguish one from the other.	Tradeoff between the smaller combinatorial problem for equipment selection and the increasing problem complexity in the state definition

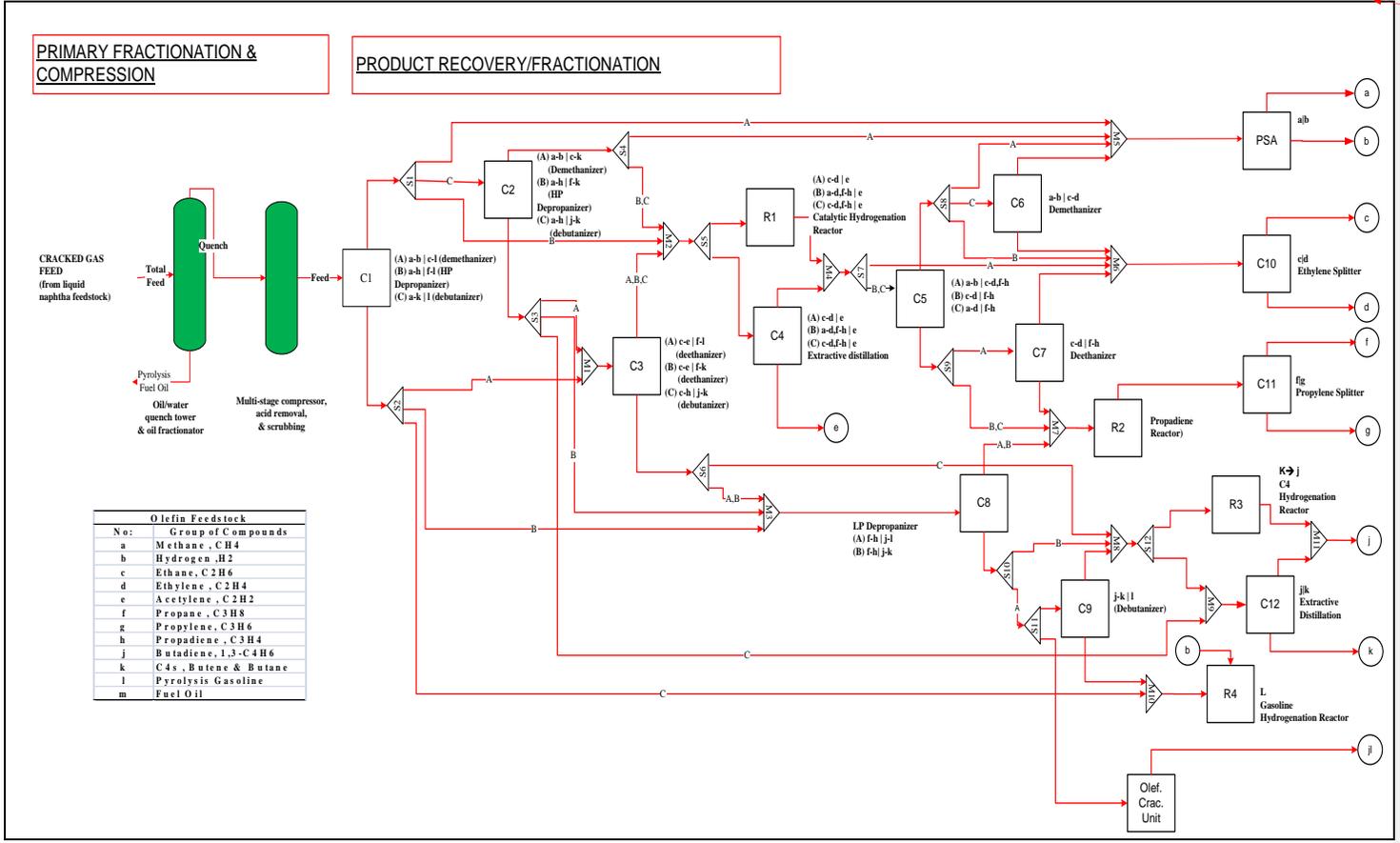


Figure 109 — Intermediate Representation of Distillation Sequencing for Olefin Production

Figure 9 shows the intermediate representation of distillation sequencing for olefin production. The project scope is narrowed down to the product recovery or fractionation section. There are a few alternatives involved in the superstructure.

1. The first unit C1 consider different cuts :

- Demethanizer – remove the light end first
- HP depropanizer – use when the propane and heavier are main cracked feed.
- Debutanizer – employs indirect sequence.

2. Different method to remove/separate acetylene from the stream:

- Extractive distillation (task C4)
- Catalytic hydrogenation reactor/ acetylene reactor ( task R1) – improve the quality of specific product, e.g. upgrade the chemical grade ethylene to polymer grade ethylene.

3. Different method to remove /separate butadiene from mixed C4s mixture

- Extractive distillation (task C12)
- Catalytic hydrogenation reactor (task R3) – convert the butane and butane into butadiene.

4. ATOFINA/UOP Olefin Cracking Process (UOP, 2004) can be used to convert the heavy end product C4 to C8 olefin to propylene and ethylene at high propylene to ethylene ratio.

- When integrated naphtha steam cracker the yield of propylene is increased dramatically for the same total naphtha flowrate.

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#### 4.34.2 Linear Material Balances

According to Andreacovich and Westerberg (1985), material balance constraints relate material flows into and out of columns in the superstructure. Each column separates its feed into two product streams whose amounts are related to the feed flow by equation (2)

$$\begin{aligned} D_k &= \xi_D F_k \\ B_k &= \xi_B F_k = (1 - \xi_D) F_k \end{aligned} \quad (2)$$

Where  $\xi_D$  is the split fraction of the feed to column,  $k$  which leaves in the distillate and  $\xi_B$  is the split fraction that leaves in the bottoms. The constraint is written for each product produced by columns in the structure must equal to the amount of that intermediate product fed to columns which further separate the product. That is

$$\sum_{k \in PS_m} \xi_k F_k - \sum_{k \in FS_m} F_k = 0 \quad m \in IP \quad (3)$$

Where  $PS_m$  is the set of all columns which produce a given intermediate product  $m$  as distillate or bottoms,  $FS_m$  is the set of all columns having intermediate product  $m$  as feed,  $F$  is the total flow rate to a column,  $IP$  is the set of all intermediate products, and  $\xi$  is the split fraction relating distillate or bottoms flows to feed flows. This constraint (3) is written for each intermediate product.

A similar expression is necessary for the feed to the distillation system:

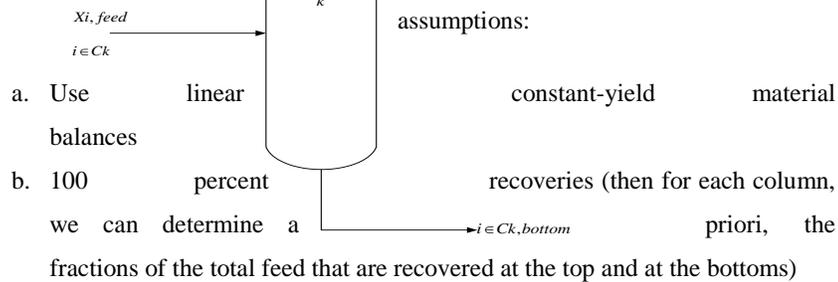
$$\sum_{k \in FS_F} F_k = F_{TOT} \quad (4)$$

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Refer to equation (4), the total feed to the system must equal the sum of the feeds to all columns which process some portion of the feed stream.

In order to reduce the size and production, there are a few

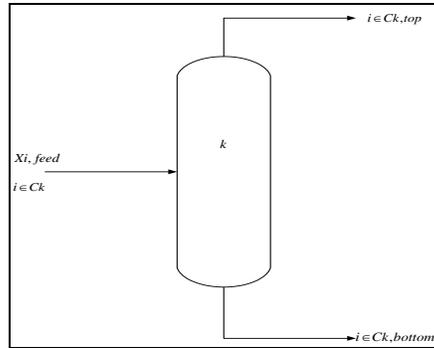


For each column, the calculation (95) procedure to obtain the split fractions is as follows (Figure 4-10):

$$\xi_{k,top} = \frac{\sum_{i \in Ck,top} Xi, feed}{\sum_{i \in Ck,} Xi}$$

$$\xi_{k,bottom} = \frac{\sum_{i \in Ck,bottom} Xi, feed}{\sum_{i \in Ck,} Xi} \quad (95)$$

Where  $Xi, feed$  = mole fraction of component  $i$  in the initial mixture,  
 $Ck$  = set of component in the feed  
 $Ck,top$  = set of components in the top or overhead,  
 $Ck,bottom$  = set of components in the bottom of column  $k$



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Figure 5544 Module for total flow with sharp split

As an example, consider the mass compositions from University of Manchester’s Centre for Process Integration (2005), the corresponding split fraction are shown in Table 45.

Table 5544 Split fraction based on mass composition from University Manchester’s Centre for Process Integration (2005)

Split fraction based on mass composition from University of Manchester’s Centre for Process Integration (2005)		
$\xi_{TotalFeed}^{a-l} = 0.9618$	$\xi_{C3a}^{c-e} = 0.4246$	$\xi_{C4a}^{c-d} = 0.9793$
$\xi_{TotalFeed}^m = 0.0382$	$\xi_{C3a}^{f-l} = 0.5754$	$\xi_{C4a}^e = 0.0207$
$\xi_{C1a}^{a-b} = 0.1682$	$\xi_{C3b}^{c-e} = 0.5768$	$\xi_{C4b}^{ad-fh} = 0.9893$
$\xi_{C1a}^{c-l} = 0.8318$	$\xi_{C3b}^{f-k} = 0.4232$	$\xi_{C4b}^e = 0.0107$
$\xi_{C1b}^{a-h} = 0.7387$	$\xi_{C3c}^{c-h} = 0.8413$	$\xi_{C4c}^{cd-fh} = 0.9858$
$\xi_{C1b}^{f-l} = 0.2613$	$\xi_{C3c}^{j-k} = 0.1587$	$\xi_{C4c}^e = 0.0142$
$\xi_{C1c}^{a-k} = 0.7806$	$\xi_{R1a}^{c-d} = 0.9793$	$\xi_{C5a}^{a-b} = 0.2488$
$\xi_{C1c}^l = 0.2194$	$\xi_{R1a}^e = 0.0207$	$\xi_{C5a}^{cd-fh} = 0.7512$
$\xi_{C2a}^{a-b} = 0.2155$	$\xi_{R1b}^{ad-fh} = 0.9893$	$\xi_{C5b}^{c-d} = 0.6811$
$\xi_{C2a}^{c-k} = 0.7845$	$\xi_{R1b}^e = 0.0107$	$\xi_{C5b}^{f-h} = 0.3189$

$\xi_{C2b}^{a-h} = 0.8632$	$\xi_{R1c}^{cd-fh} = 0.9858$	$\xi_{C5c}^{a-d} = 0.7604$
$\xi_{C2b}^{f-k} = 0.1368$	$\xi_{R1c}^e = 0.0142$	$\xi_{C5c}^{f-h} = 0.2396$
$\xi_{C2c}^{a-h} = 0.8755$	$\xi_{C6}^{a-b} = 0.3272$	$\xi_{C7}^{c-d} = 0.6811$
$\xi_{C2c}^{j-k} = 0.1245$	$\xi_{C6}^{c-d} = 0.6728$	$\xi_{C7}^{f-h} = 0.3189$
$\xi_{C8a}^{f-h} = 0.3384$	$\xi_{C8b}^{f-h} = 0.6250$	$\xi_{C9}^{j-k} = 0.3069$
$\xi_{C8a}^{j-l} = 0.6616$	$\xi_{C8b}^{j-k} = 0.3750$	$\xi_{C9}^{j-k} = 0.6931$

For initial node in the network we have Equation (406),

$$\xi_{\text{TotalFeed}}^{a-l} F_{\text{Quench}} + \xi_{\text{TotalFeed}}^m F_{\text{Oil}} = \text{TOTFEED} \quad (406)$$

$$\xi_{\text{TotalFeed}}^{a-l} F_{\text{Quench}} + \xi_{\text{TotalFeed}}^m F_{\text{Oil}} = \text{TOTFEED} \quad (40)$$

For the remaining nodes in the network, mass balances for each intermediate product are considered. Based on the split fractions of recoveries sections calculated given in Table 45, the mass balances for each intermediate product is as listed in follows (Table 56, as obtained from the following general constraint:-)

$$\sum_{k \in PS_m} \xi_k F_k - \sum_{k \in FS_m} F_k = 0 \quad m \in IP \quad (403)$$

where  $PS_m$  is the set of all columns that produce a given intermediate product  $m$  as distillate or bottoms,  $FS_m$  is the set of all columns having intermediate product  $m$  as feed, and  $IP$  is the set of all intermediate products.

Table 665 Mass balance for each intermediate product

Mass balances for each intermediate product

1. Intermediate (a-b) which is produced in C1a, C2a, C6 and C5a and directed to PSA.

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$$\xi_{C1a}^{a-b} F_{C1a} + \xi_{C2a}^{a-b} F_{C2a} + \xi_{C6}^{a-b} F_{C6} + \xi_{C5a}^{a-b} F_{C5a} - F_{PSA} = 0$$

2. Intermediate (c-l) which is produced in C1a and directed to C3a.

$$\xi_{C1a}^{c-l} F_{C1a} - F_{C3a} = 0$$

3. Intermediate (a-h) which is produced in C1b, C2b and C2c and directed to R1b and C4b.

$$\xi_{C1b}^{a-h} F_{C1b} + \xi_{C2b}^{a-h} F_{C2b} + \xi_{C2c}^{a-h} F_{C2c} - F_{R1b} - F_{C4b} = 0$$

4. Intermediate (f-l) which is produced in C1b and C3a and directed to C8a.

$$\xi_{C1b}^{f-l} F_{C1b} + \xi_{C3a}^{f-l} F_{C3a} - F_{C8a} = 0$$

5. Intermediate (a-k) which is produced in C1c and directed to C2a, C2b and C2c.

$$\xi_{C1c}^{a-k} F_{C1c} - F_{C2a} - F_{C2b} - F_{C2c} = 0$$

6. Intermediate (l) which is produced in C1c and C9 and directed to R4.

$$\xi_{C1c}^l F_{C1c} + \xi_{C9}^l F_{C9} - F_{R4} = 0$$

7. Intermediate (c-k) which is produced in C2a and directed to C3b and C3c

$$\xi_{C2a}^{c-k} F_{C2a} - F_{C3b} - F_{C3c} = 0$$

8. Intermediate (f-k) which is produced in C2b and C3b and directed to C8b

$$\xi_{C2b}^{f-k} F_{C2b} + \xi_{C3b}^{f-k} F_{C3b} - F_{C8b} = 0$$

9. Intermediate (j-k) which is produced in C2c, C3c, C8b, and C9 and directed to C12

$$\xi_{C2c}^{j-k} F_{C2c} + \xi_{C3c}^{j-k} F_{C3c} + \xi_{C8b}^{j-k} F_{C8b} + \xi_{C9}^{j-k} F_{C9} - F_{C12} = 0$$

10. Intermediate (c-e) which is produced in C3a and C3b and directed to R1a and C4a

$$\xi_{C3a}^{c-e} F_{C3a} + \xi_{C3b}^{c-e} F_{C3b} - F_{R1a} - F_{C4a} = 0$$

11. Intermediate (c-h) which is produced in C3c and directed to R1c and C4c

$$\xi_{C3c}^{c-h} F_{C3c} - F_{R1c} - F_{C4c} = 0$$

12. Intermediate (c-d) which is produced in R1a, C4a, C6, C7 and C5b and C3b and directed to C10

$$\xi_{R1a}^{c-d} F_{R1a} + \xi_{C4a}^{c-d} F_{C4a} + \xi_{C6}^{c-d} F_{C6} + \xi_{C7}^{c-d} F_{C7} + \xi_{C5b}^{c-d} F_{C5b} - F_{C10} = 0$$

13. Intermediate (ad-fh) which is produced in R1b and C4b and C3b and directed to C5a and C5c

$$\xi_{R1b}^{ad-fh} F_{R1b} + \xi_{C4b}^{ad-fh} F_{C4b} - F_{C5a} - F_{C5c} = 0$$

14. Intermediate (cd-fh) which is produced in R1c, C4c and C5a and directed to C7.

$$\xi_{R1c}^{cd-fh} F_{R1c} + \xi_{C4c}^{cd-fh} F_{C4c} + \xi_{C5a}^{cd-fh} F_{C5a} - F_{C7} = 0$$

15. Intermediate (a-d) which is produced in C5c and directed to C6

$$\xi_{C5c}^{a-d} F_{C5c} - F_{C6} = 0$$

16. Intermediate (f-h) which is produced in C5b, C5c, C7, C8a and C8b and directed to R2

$$\xi_{C5b}^{f-h} F_{C5b} + \xi_{C5c}^{f-h} F_{C5c} + \xi_{C7}^{f-h} F_{C7} + \xi_{C8a}^{f-h} F_{C8a} + \xi_{C8b}^{f-h} F_{C8b} - F_{R2} = 0$$

17. Intermediate (j-l) which is produced in C8a and directed to C9 and OCU
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$$\xi_{C8a}^{j-l} F_{C8a} - F_{C9} - F_{OCU} = 0$$

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#### 4.2.3 Logical Constraints on Design Specifications, Interconnectivity Relationships and Switching Constraints

Logical constraints are developed for the intermediate representation superstructure in Figure 4-9 for the following purposes:

- to relate the continuous variables with the binary 0–1 variables, specifically to ensure that the non-selection of a process unit results in corresponding zero flowrates of the input and output streams associated with the process unit;
- to stipulate design specifications based on engineering knowledge and past design experience; and
- to enforce interconnectivity relationships among the states and tasks nodes in the superstructure.

The logical constraints and switching constraints are also developed for the entire Intermediate superstructure representation and they are included in Table 6-7 and Table 78.

The following notations and definitions are used in constructing these constraints:

$Y_i$ : Boolean variable with value true denoting the existence of a process unit  $i$  (including mixers and splitters) and values false denoting its non-existence;

$y_i$ : binary variable associated with their corresponding Boolean variables with value equals to one (1) denoting the existence of a process unit  $i$  (including mixers and splitters) and value equals to zero (0) denoting its non-existence;

$F_j$ : flow rate variable of a state (or material stream)  $j$ ; and

$M_i$ : maximum capacity of a process unit  $i$  to represent the upper bound on its outlet flow rate in stream  $j$ .

Note that in this work, we have found it desirable to only consider the selection of the process units; thus, we have omitted the modeling of the stream selection in the logical

constraints. The same reason has been stressed in Raman and Grossmann (1993), which goes on to assert that this is indeed commonly the case in problems of similar nature.

Tables 6-7 and 78, present the logical constraints on design specifications and logical constraints on interconnectivity relationships (structural specifications) respectively for the feed and cracking subsystem. Logical constraints on design specifications are needed especially for distillation columns (and reactors) in which selection of a single task that takes place in the column needs to be made.

**Table 7.6** Logical constraints on design specifications (DS) for the separation subsystem using intermediate representation

	Logic proposition on design specification	Logical expression and clauses	Integer linear inequality
DS1	Select only one from among: <ul style="list-style-type: none"> <li>demethanizer (task C1a)</li> <li>HP depropanizer (task C1b)</li> <li>debutanizer (C1c)</li> </ul>	$Y_{a-b e-l}^{C1a} \oplus Y_{a-h f-l}^{C1b} \oplus Y_{a-k l}^{C1c}$	$y_{a-b e-l}^{C1a} + y_{a-h f-l}^{C1b} + y_{a-k l}^{C1c} = 1$
DS2	From among the demethanizer (C2a), HP depropanizer (C2b), and debutanizer (C2c), select none or only one (note: none of the task for C2 column can be selected because there is provision for it to be bypassed in the superstructure)	$Y_{a-b c-k}^{C2a} \vee Y_{a-i f-k}^{C2b} \vee Y_{a-i j-k}^{C2c}$	$y_{a-b c-k}^{C2a} + y_{a-i f-k}^{C2b} + y_{a-i j-k}^{C2c} \leq 1$
DS3	Select only one or none of the deethanizer (C3a, C3b) or debutanizer (C3c).	$Y_{c-e f-l}^{C3a} \vee Y_{c-e f-k}^{C3b} \vee Y_{c-i j-k}^{C3c}$	$y_{c-e f-l}^{C3a} + y_{c-e f-k}^{C3b} + y_{c-i j-k}^{C3c} \leq 1$
DS4	Catalytic hydrogenation reactor (R1) converts acetylene to ethane and ethylene. Components entering R1 depend on constraint DS1, i.e., whether HP depropanizer or debutanizer is selected upstream. (note that this might be a redundant constraint; this condition might have been enforced by other constraints)	$Y_{c-d e}^{R1a} \vee Y_{a-d,f-h e}^{R1b} \vee Y_{c-d,f-h e}^{R1c}$	$y_{c-d e}^{R1a} + y_{a-d,f-h e}^{R1b} + y_{c-d,f-h e}^{R1c} \leq 1$
DS5	Extractive distillation column (C4) separates acetylene from the other components. As in previous, components entering C4 depend on the unit selected upstream.	$Y_{c-d e}^{C4a} \vee Y_{a-d,f-h e}^{C4b} \vee Y_{c-d,f-h e}^{C4c}$	$y_{c-d e}^{C4a} + y_{a-d,f-h e}^{C4b} + y_{c-d,f-h e}^{C4c} \leq 1$
DS6	At most two of the tasks for similar categories of tasks involving the catalytic reactor R1 or column C4 can be selected		$y_{c-d e}^{R1a} + y_{c-d e}^{C4a} \leq 2$ $y_{a-d,f-h e}^{R1b} + y_{a-d,f-h e}^{C4b} \leq 2$ $y_{c-d,f-h e}^{R1c} + y_{c-d,f-h e}^{C4c} \leq 2$
DS7	Select at most one from among demethanizer (C5a), deethanizer (C5b), and depropanizer (C5c).		$y_{a-b e-d,f-h}^{C5a} + y_{c-d f-h}^{C5b} + y_{a-d f-h}^{C5c} \leq 1$
DS8	Select only one or none from among LP depropanizer (C8a) and C8b	$Y_{f-h j-l}^{C8a} \vee Y_{f-h j-k}^{C8b}$	$y_{f-h j-l}^{C8a} + y_{f-h j-k}^{C8b} \leq 1$
DS9	At most two tasks can be selected between C4 hydrogenation reactor R3 and extractive distillation column C12		$y_{jk}^{R3} + y_{jk}^{C12} \leq 2$

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The logical constraints on structural specifications ~~are categorized into~~ two groups or sections ~~are categorized into~~:

- (1) Logical constraints on structural specifications that involve the overhead and bottom products (Table 7a8a);
- (2) Logical constraints on structural specifications that involve the feed or inlet to the columns (Table 87b) , which is similar to the —constraints on sequence of task of columns as employed by (refer to Floudas and Paules (1988), p. 538)

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**Table 887(a) Logical constraints on structural specifications for interconnectivity relationships for the separation subsystem using intermediate representation which involve the overhead and bottom products**

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Logic proposition on structural specification	Algebraic constraint (integer linear)
Overhead products from the demethanizer (C1a) go to the pressure swing absorber (PSA); bottom products go to the deethanizer (C3a). $Y_{a-h c-l}^{C1a} \Rightarrow Y_{ab}^{PSA} \wedge Y_{c-e f-l}^{C3a}$ OR express the logical statement in the following way: From the demethanizer (C1a): <ul style="list-style-type: none"> <li>• the overhead products go to the pressure swing absorber (PSA);</li> <li>• the bottom products go to the deethanizer (C3a).</li> </ul> From the HP depropanizer (C1b): <ul style="list-style-type: none"> <li>• the overhead products go to either the catalytic hydrogenation reactor (R1b) or extractive distillation column (C4b)</li> </ul>	$y_{a b}^{PSA} - y_{a b}^{C1a} \geq 0$ $y_{c-e f-l}^{C3a} - y_{a b}^{C1a} \geq 0$  $y_{a-d,f-h e}^{R1b} + y_{a-d,f-h e}^{C4b} - y_{a-h f-l}^{C1b} \geq 0$ $y_{f-h j-l}^{C8a} - y_{a-h f-l}^{C1b} \geq 0$

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- the bottom products go to the LP depropanizer (C8a).

$$Y_{a-h|f-l}^{C1b} \Rightarrow \left( Y_{a-d,f-h|e}^{R1b} \vee Y_{a-d,f-h|e}^{C4b} \right) \wedge Y_{f-h|j-l}^{C8a}$$

$$\left( \neg Y_{a-h|f-l}^{C1b} \vee Y_{a-d,f-h|e}^{R1b} \vee Y_{a-d,f-h|e}^{C4b} \right) \wedge \left( \neg Y_{a-h|f-l}^{C1b} \vee Y_{f-h|j-l}^{C8a} \right)$$

Overhead products from debutanizer (C1c) go to demethanizer (C2a), depropanizer (C2b) or debutanizer (C2c). Bottom products go to gasoline hydrogenation reactor (R4).

$$Y_{a-k|l}^{C1c} \Rightarrow \left( Y_{a-b|c-k}^{C2a} \vee Y_{a-h|f-k}^{C2b} \vee Y_{a-i|j-k}^{C2c} \right) \wedge Y_l^{R4}$$

$$\left( \neg Y_{a-k|l}^{C1c} \vee Y_{a-b|c-k}^{C2a} \vee Y_{a-h|f-k}^{C2b} \vee Y_{a-i|j-k}^{C2c} \right) \wedge \left( \neg Y_{a-k|l}^{C1c} \vee Y_l^{R4} \right)$$

$$y_{a-b|c-k}^{C2a} + y_{a-h|f-k}^{C2b} + y_{1-9|10,11}^{C2c} - y_{a-i|j-k}^{C2c} \geq 0$$

$$y_l^{R4} - y_{a-k|l}^{C1c} \geq 0$$

Overhead products from demethanizer (C2a) go to pressure swing absorber (PSA). Bottom products go to deethanizer(C3b) or debutanizer (C3c).

$$Y_{a-b|c-k}^{C2a} \Rightarrow Y_{a|b}^{PSA} \wedge \left( Y_{c-e|f-k}^{C3b} \vee Y_{c-e|j-k}^{C3c} \right)$$

$$\left( \neg Y_{a-b|c-k}^{C2a} \vee Y_{a|b}^{PSA} \right) \wedge \left( \neg Y_{a-b|c-k}^{C2a} \vee Y_{c-e|f-k}^{C3b} \vee Y_{c-e|j-k}^{C3c} \right)$$

$$y_{a|b}^{PSA} - y_{a-b|c-k}^{C2a} \geq 0$$

$$y_{c-e|f-k}^{C3b} + y_{c-e|j-k}^{C3c} - y_{a-b|c-k}^{C2a} \geq 0$$

Overhead products from depropanizer (C2b) go to catalytic hydrogenation reactor (R1b) or extractive distillation column (C4b). Bottom products go to depropanizer (C8b).

$$Y_{a-h|f-k}^{C2b} \Rightarrow \left( Y_{a-d,f-h|e}^{R1b} \vee Y_{a-d,f-h|e}^{C4b} \right) \wedge Y_{f-h|j-k}^{C8b}$$

$$\left( \neg Y_{a-h|f-k}^{C2b} \vee Y_{a-d,f-h|e}^{R1b} \vee Y_{a-d,f-h|e}^{C4b} \right) \wedge \left( \neg Y_{1-9|6-11}^{C2b} \vee Y_{f-h|j-k}^{C8b} \right)$$

$$y_{a-d,f-h|e}^{R1b} + y_{a-d,f-h|e}^{C4b} - y_{a-h|f-k}^{C2b} \geq 0$$

$$y_{f-h|j-k}^{C8b} - y_{a-h|f-k}^{C2b} \geq 0$$

Overhead products from depropanizer (C2c) go to catalytic hydrogenation reactor (R1b) or extractive distillation column (C4b). Bottom products go to extractive distillation column (C12)

$$Y_{a-h|j-k}^{C2c} \Rightarrow \left( Y_{a-d,f-h|e}^{R1b} \vee Y_{a-d,f-h|e}^{C4b} \right) \wedge \left( Y_{j|k}^{C12} \right)$$

$$\left( \neg Y_{a-h|j-k}^{C2c} \vee Y_{a-d,f-h|e}^{R1b} \vee Y_{a-d,f-h|e}^{C4b} \right) \wedge \left( \neg Y_{a-h|j-k}^{C2c} \vee Y_{j|k}^{C12} \right)$$

$$y_{a-d,f-h|e}^{R1b} + y_{a-d,f-h|e}^{C4b} - y_{a-h|j-k}^{C2c} \geq 0$$

$$y_{j|k}^{C12} - y_{a-h|j-k}^{C2c} \geq 0$$

Overhead products from the deethanizer (C3a) go to the catalytic hydrogenation reactor (R1a) or extractive distillation column (C4a). Bottom products go to depropanizer (C8a).

$$Y_{c-e|f-l}^{C3a} \Rightarrow \left( Y_{c-d|e}^{R1a} \vee Y_{c-d|e}^{C4a} \right) \wedge Y_{f-h|j-l}^{C8a}$$

$$\left( \neg Y_{c-e|f-l}^{C3a} \vee Y_{c-d|e}^{R1a} \vee Y_{c-d|e}^{C4a} \right) \wedge \left( \neg Y_{c-e|f-l}^{C3a} \vee Y_{f-h|j-l}^{C8a} \right)$$

$$y_{c-d|e}^{R1a} + y_{c-d|e}^{C4a} - y_{c-e|f-l}^{C3a} \geq 0$$

$$y_{f-h|j-l}^{C8a} - y_{c-e|f-l}^{C3a} \geq 0$$

Overhead products from the deethanizer (C3b) go to the catalytic hydrogenation reactor (R1a) or extractive distillation column (C4a). Bottom products go to depropanizer (C8b).

$$Y_{c-e|f-k}^{C3b} \Rightarrow \left( Y_{c-d|e}^{R1a} \vee Y_{c-d|e}^{C4a} \right) \wedge Y_{f-h|j-k}^{C8b}$$

$$\left( \neg Y_{c-e|f-k}^{C3b} \vee Y_{c-d|e}^{R1a} \vee Y_{c-d|e}^{C4a} \right) \wedge \left( \neg Y_{c-e|f-k}^{C3b} \vee Y_{f-h|j-k}^{C8b} \right)$$

$$y_{c-d|e}^{R1a} + y_{c-d|e}^{C4a} - y_{c-e|f-k}^{C3b} \geq 0$$

$$y_{f-h|j-k}^{C8b} - y_{c-e|f-k}^{C3b} \geq 0$$

Overhead products from debutanizer (C3c) go to catalytic hydrogenation reactor (R1c) or extractive distillation column (C4c). Bottom products go to extractive distillation column (C12) or C4 hydrogenation reactor (R3).

$$Y_{c-h|j-k}^{C3c} \Rightarrow \left( Y_{c-d,f-h|e}^{R1c} \vee Y_{c-d,f-h|e}^{C4c} \right) \wedge \left( Y_{j|k}^{C12} \vee Y_{j|k}^{R3} \right)$$

$$\left( \neg Y_{c-h|j-k}^{C3c} \vee Y_{c-d,f-h|e}^{R1c} \vee Y_{c-d,f-h|e}^{C4c} \right) \wedge \left( \neg Y_{j|k}^{C12} \vee Y_{j|k}^{R3} \right)$$

$$y_{c-d,f-h|e}^{R1c} + y_{c-d,f-h|e}^{C4c} - y_{c-h|j-k}^{C3c} \geq 0$$

$$y_{j|k}^{C12} + y_{j|k}^{R3} - y_{c-h|j-k}^{C3c} \geq 0$$

Products from catalytic hydrogenation reactor (R1a) go to ethylene splitter (C10).

$$Y_{c-d|e}^{R1a} \Rightarrow Y_{c|d}^{C10}$$

$$\neg Y_{c-d|e}^{R1a} \vee Y_{c|d}^{C10}$$

$$y_{c|d}^{C10} - y_{c-d|e}^{R1a} \geq 0$$

Products from catalytic hydrogenation reactor (R1b) go to demethanizer (C5a) or depropanizer (C5c).

$$Y_{a-d,f-h|e}^{R1b} \Rightarrow Y_{a-b|c-d,f-h}^{C5a} \vee Y_{a-d|f-h}^{C5c}$$

$$\neg Y_{a-d,f-h|e}^{R1b} \vee Y_{a-b|c-d,f-h}^{C5a} \vee Y_{a-d|f-h}^{C5c}$$

$$y_{a-b|c-d,f-h}^{C5a} + y_{a-d|f-h}^{C5c} - y_{a-d,f-h|e}^{R1b} \geq 0$$

Products from catalytic hydrogenation reactor (R1c) go to demethanizer (C5b).

$$Y_{c-d,f-h|e}^{R1c} \Rightarrow Y_{c-d|f-h}^{C5b}$$

$$\neg Y_{c-d,f-h|e}^{R1c} \vee Y_{c-d|f-h}^{C5b}$$

$$y_{c-d|f-h}^{C5b} - y_{c-d,f-h|e}^{R1c} \geq 0$$

Overhead products of extractive distillation (C4a) go to ethylene splitter (C10).

$$Y_{c-d|e}^{C4a} \Rightarrow Y_{c|d}^{C10}$$

$$\neg Y_{c-d|e}^{C4a} \vee Y_{c|d}^{C10}$$

$$y_{c|d}^{C10} - y_{c-d|e}^{C4a} \geq 0$$

Overhead products from extractive distillation (C4b) go to demethanizer (C5a) or depropanizer (C5c).

$$y_{a-b|c-d,f-h}^{C5a} + y_{a-d|f-h}^{C5c} - y_{a-d,f-h|e}^{C4b} \geq 0$$

$$Y_{a-d,f-h|e}^{C4b} \Rightarrow Y_{a-b|c-d,f-h}^{C5a} \vee Y_{a-d|f-h}^{C5c}$$

$$\neg Y_{a-d,f-h|e}^{C4b} \vee \left( Y_{a-b|c-d,f-h}^{C5a} \vee Y_{a-d|f-h}^{C5c} \right)$$

(NOTE: Boolean variable for column C5b  $Y_{3,4|6-9}^{C5b}$  is not considered in the logic proposition because it does not involve components 1 and 2.)

Overhead products from extractive distillation (C4c) go to deethanizer (C5b)

$$Y_{c-d,f-h|e}^{C4c} \Rightarrow Y_{c-d|f-h}^{C5b}$$

$$\neg Y_{c-d,f-h|e}^{C4c} \vee Y_{c-d|f-h}^{C5b}$$

$$y_{c-d|f-h}^{C5b} - y_{c-d,f-h|e}^{C4c} \geq 0$$

Overhead products demethanizer (C5a) go to pressure swing absorber (PSA). Bottom products go to deethanizer (C7).

$$Y_{a-b|c-d,f-h}^{C5a} \Rightarrow Y_{a|b}^{PSA} \wedge Y_{c-d|f-h}^{C7}$$

$$\left( \neg Y_{a-b|c-d,f-h}^{C5a} \vee Y_{a|b}^{PSA} \right) \wedge \left( \neg Y_{a-b|c-d,f-h}^{C5a} \vee Y_{c-d|f-h}^{C7} \right)$$

$$y_{a|b}^{PSA} - y_{a-b|c-d,f-h}^{C5a} \geq 0$$

$$y_{c-d|f-h}^{C7} - y_{a-b|c-d,f-h}^{C5a} \geq 0$$

Overhead products demethanizer (C5b) go to ethylene splitter (C10). Bottom products go to methyl acetylene & propadiene reactor (R2).

$$Y_{c-d|f-h}^{C5b} \Rightarrow Y_{c|d}^{C10} \wedge Y_{f-h}^{R2}$$

$$\left( \neg Y_{c-d|f-h}^{C5b} \vee Y_{c|d}^{C10} \right) \wedge \left( \neg Y_{c-d|f-h}^{C5b} \vee Y_{f-h}^{R2} \right)$$

$$y_{c|d}^{C10} - y_{c-d|f-h}^{C5b} \geq 0$$

$$y_{f-h}^{R2} - y_{3,4|6-9}^{C5b} \geq 0$$

Overhead products depropanizer (C5c) go to demethanizer (C6). Bottom products go to methyl acetylene & propadiene reactor (R2).

$$Y_{a-d|c-d,f-h}^{C5c} \Rightarrow Y_{a-b|c-d}^{C6} \wedge Y_{f-h}^{R2}$$

$$\left( \neg Y_{a-d|c-d,f-h}^{C5c} \vee Y_{a-b|c-d}^{C6} \right) \wedge \left( \neg Y_{a-d|c-d,f-h}^{C5c} \vee Y_{f-h}^{R2} \right)$$

$$y_{a-b|c-d}^{C6} - y_{a-d|c-d,f-h}^{C5c} \geq 0$$

$$y_{f-h}^{R2} - y_{a-d|c-d,f-h}^{C5c} \geq 0$$

Overhead products of demethanizer (C6) go to pressure swing absorber (PSA) and the bottom product go to ethylene splitter (C10).

$$Y_{a-b|c-d}^{C6} \Rightarrow Y_{a|b}^{PSA} \wedge Y_{c|d}^{C10}$$

$$\left( \neg Y_{a-b|c-d}^{C6} \vee Y_{a|b}^{PSA} \right) \wedge \left( \neg Y_{a-b|c-d}^{C6} \vee Y_{c|d}^{C10} \right)$$

$$y_{a|b}^{PSA} - y_{a-b|c-d}^{C6} \geq 0$$

$$y_{c|d}^{C10} - y_{a-b|c-d}^{C6} \geq 0$$

Overhead product from deethanizer (C7) go to ethylene splitter (C10) and bottom product go to methyl acetylene & propadiene reactor (R2).

$$Y_{c-d|f-h}^{C7} \Rightarrow Y_{c|d}^{C10} \wedge Y_{f-h}^{R2}$$

$$\left( \neg Y_{c-d|f-h}^{C7} \vee Y_{c|d}^{C10} \right) \wedge \left( \neg Y_{c-d|f-h}^{C7} \vee Y_{f-h}^{R2} \right)$$

$$y_{c|d}^{C10} - y_{c-d|f-h}^{C7} \geq 0$$

$$y_{f-h}^{R2} - y_{c-d|f-h}^{C7} \geq 0$$

Overhead products from depropanizer (C8a) go to methyl acetylene & propadiene reactor (R2). Bottom products will either go to debutanizer (C9) or olefin cracking unit (OCU).

$$Y_{f-h|j-l}^{C8a} \Rightarrow Y_{f-h}^{R2} \wedge \left( Y_{j-k|l}^{C9} \vee Y_{j-l}^{OCU} \right)$$

$$\left( \neg Y_{f-h|j-l}^{C8a} \vee Y_{f-h}^{R2} \right) \wedge \left( \neg Y_{f-h|j-l}^{C8a} \vee Y_{j-k|l}^{C9} \vee Y_{j-l}^{OCU} \right)$$

$$y_{f-h}^{R2} - y_{f-h|j-l}^{C8a} \geq 0$$

$$y_{j-k|l}^{C9} + y_{j-l}^{OCU} - y_{f-h|j-l}^{C8a} \geq 0$$

Overhead products from depropanizer (C8b) go to methyl acetylene and propadiene reactor (R2). Bottom products will either go to C4 hydrogenation reactor (R3), extractive distillation (C12)

$$Y_{f-h|j-k}^{C8b} \Rightarrow Y_{f-h}^{R2} \wedge \left( Y_{j|k}^{R3} \vee Y_{j|k}^{C12} \right)$$

$$\left( \neg Y_{f-h|j-k}^{C8b} \vee Y_{f-h}^{R2} \right) \wedge \left( \neg Y_{f-h|j-k}^{C8b} \vee Y_{j|k}^{R3} \vee Y_{j|k}^{C12} \right)$$

$$y_{f-h}^{R2} - y_{f-h|j-k}^{C8b} \geq 0$$

$$y_{j|k}^{R3} + y_{j|k}^{C12} - y_{f-h|j-k}^{C8b} \geq 0$$

Products from methyl acetylene and propadiene reactor (R2) go to propylene splitter (C11) (*note*: equivalence relation is used in the logical statement because involving single choice decision)

$$Y_{f-h}^{R2} \Leftrightarrow Y_{f|g}^{C11}$$

$$\left( \neg Y_{f-h}^{R2} \vee Y_{f|g}^{C11} \right) \wedge \left( Y_{f-h}^{R2} \vee \neg Y_{f|g}^{C11} \right)$$

$$y_{f|g}^{C11} - y_{f-h}^{R2} \geq 0$$

$$y_{f-h}^{R2} - y_{f|g}^{C11} \geq 0$$

Overhead products from debutanizer (C9) will either go to C4 hydrogenation reactor (R3) or extractive distillation (C12). Bottom products go to gasoline hydrogenation reactor (R4).

$$Y_{j-k|l}^{C9} \Rightarrow \left( Y_{j|k}^{R3} \vee Y_{j|k}^{C12} \right) \wedge Y_l^{R4}$$

$$\left( \neg Y_{j-k|l}^{C9} \vee Y_{j|k}^{R3} \vee Y_{j|k}^{C12} \right) \wedge \left( \neg Y_{j-k|l}^{C9} \vee Y_l^{R4} \right)$$

$$y_{j|k}^{R3} + y_{j|k}^{C12} - y_{j-k|l}^{C9} \geq 0$$

$$y_l^{R4} - y_{j-k|l}^{C9} \geq 0$$

**Table 78(b) Logical constraints on structural specifications that involve inlet/feed to columns**

Logic proposition on structural specification	Algebraic constraint (integer linear)
<p>The inlet of demethanizer (C2a), depropanizer (C2b), and debutanizer (C2c) is the overhead product of debutanizer (C1c).</p> $Y_{a-b c-k}^{C2a} \vee Y_{a-h f-k}^{C2b} \vee Y_{a-h j-k}^{C2c} \Rightarrow Y_{a-k l}^{C1c}$ $\left( \neg Y_{a-b c-k}^{C2a} \vee Y_{a-k l}^{C1c} \right) \wedge \left( \neg Y_{a-h f-k}^{C2b} \vee Y_{a-k l}^{C1c} \right) \wedge \left( \neg Y_{a-h j-k}^{C2c} \vee Y_{a-k l}^{C1c} \right)$	$y_{a-k l}^{C1c} - y_{a-b c-k}^{C2a} \geq 0$ $y_{a-k l}^{C1c} - y_{a-h f-k}^{C2b} \geq 0$ $y_{a-k l}^{C1c} - y_{a-h j-k}^{C2c} \geq 0$
<p>The inlet of deethanizer (C3a) is the bottom product of demethanizer (C1a).</p> $Y_{c-e f-l}^{C3a} \Rightarrow Y_{a-b c-l}^{C1a}$ $\neg Y_{c-e f-l}^{C3a} \vee Y_{a-b c-l}^{C1a}$	$y_{a-b c-l}^{C1a} - y_{c-e f-l}^{C3a} \geq 0$
<p>The inlet of deethanizer (C3b) or debutanizer (C3c) is the bottom product of demethanizer (C2a).</p> $Y_{c-e f-k}^{C3b} \vee Y_{c-h j-k}^{C3c} \Rightarrow Y_{a-b c-k}^{C2a}$ $\neg \left( Y_{c-e f-k}^{C3b} \vee Y_{c-h j-k}^{C3c} \right) \vee Y_{a-b c-k}^{C2a}$ $\left( \neg Y_{c-e f-k}^{C3b} \wedge \neg Y_{c-h j-k}^{C3c} \right) \vee Y_{a-b c-k}^{C2a}$ $\left( \neg Y_{c-e f-k}^{C3b} \vee Y_{a-b c-k}^{C2a} \right) \wedge \left( \neg Y_{c-h j-k}^{C3c} \vee Y_{a-b c-k}^{C2a} \right)$	$y_{a-b c-k}^{C2a} - y_{c-e f-k}^{C3b} \geq 0$ $y_{a-b c-k}^{C2a} - y_{c-h j-k}^{C3c} \geq 0$
<p>The inlet of catalytic hydrogenation reactor (R1a) is either from demethanizer (C3a) or demethanizer (C3b).</p> $Y_{c-d e}^{R1a} \Rightarrow Y_{c-e f-l}^{C3a} \vee Y_{c-e f-l}^{C3b}$ $\neg Y_{c-d e}^{R1a} \vee Y_{c-e f-l}^{C3a} \vee Y_{c-e f-l}^{C3b}$	$y_{c-e f-l}^{C3a} + y_{c-e f-l}^{C3b} - y_{c-d e}^{R1a} \geq 0$
<p>The inlet of catalytic hydrogenation reactor (R1b) is either from depropanizer (C2b), debutanizer (C2c) or HP depropanizer (C1b).</p> $Y_{a-d,f-h e}^{R1b} \Rightarrow Y_{a-h f-k}^{C2b} \vee Y_{a-h j-k}^{C2c} \vee Y_{a-h f-l}^{C1b}$ $\neg Y_{a-d,f-h e}^{R1b} \vee Y_{a-h f-k}^{C2b} \vee Y_{a-h j-k}^{C2c} \vee Y_{a-h f-l}^{C1b}$	$y_{a-h f-k}^{C2b} + y_{a-h j-k}^{C2c} + y_{a-h f-l}^{C1b} - y_{a-d,f-h e}^{R1b} \geq 0$
<p>The inlet of catalytic hydrogenation reactor (R1c) is from debutanizer (C3c).</p>	$y_{c-h j-k}^{C3c} - y_{c-d,f-h e}^{R1c} \geq 0$

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$$Y_{c-d,f-h|e}^{R1c} \Rightarrow Y_{c-h|j-k}^{C3c}$$

$$\neg Y_{c-d,f-h|e}^{R1c} \vee Y_{c-h|j-k}^{C3c}$$

The inlet of extractive distillation (C4a) is either from deethanizer (C3a) or deethanizer (C3b).

$$Y_{c-d|e}^{C4a} \Rightarrow Y_{c-e|f-l}^{C3a} \vee Y_{c-e|f-k}^{C3b}$$

$$\neg Y_{c-d|e}^{C4a} \vee Y_{c-e|f-l}^{C3a} \vee Y_{c-e|f-k}^{C3b}$$

$$y_{c-e|f-l}^{C3a} + y_{c-e|f-k}^{C3b} - y_{c-d|e}^{C4a} \geq 0$$

The inlet of extractive distillation (C4b) is either from depropanizer (C2b), debutanizer (C2c) or HP depropanizer (C1b).

$$Y_{a-d,f-h|e}^{C4b} \Rightarrow Y_{a-h|f-k}^{C2b} \vee Y_{a-h|j-k}^{C2c} \vee Y_{a-k|l}^{C1b}$$

$$\neg Y_{a-d,f-h|e}^{C4b} \vee Y_{a-h|f-k}^{C2b} \vee Y_{a-h|j-k}^{C2c} \vee Y_{a-k|l}^{C1b}$$

$$y_{a-h|f-k}^{C2b} + y_{a-h|j-k}^{C2c} + y_{a-k|l}^{C1b} - y_{a-d,f-h|e}^{C4b} \geq 0$$

The inlet of extractive distillation (C4c) is from debutanizer (C3c).

$$Y_{c-d,f-h|e}^{C4c} \Rightarrow Y_{c-h|j-k}^{C3c}$$

$$\neg Y_{c-d,f-h|e}^{C4c} \vee Y_{c-h|j-k}^{C3c}$$

$$y_{c-h|j-k}^{C3c} - y_{c-d,f-h|e}^{C4c} \geq 0$$

The inlet of demethanizer (C5a) or depropanizer (C5c) is either from catalytic hydrogenation reactor (R1b) or extractive distillation (C4b).

$$Y_{a-b|c-d,f-h}^{C5a} \vee Y_{a-d|f-h}^{C5c} \Rightarrow Y_{a-d,f-h|e}^{R1b} \vee Y_{a-d,f-h|e}^{C4b}$$

$$(\neg Y_{a-b|c-d,f-h}^{C5a} \wedge \neg Y_{a-d|f-h}^{C5c}) \vee (Y_{a-d,f-h|e}^{R1b} \vee Y_{a-d,f-h|e}^{C4b})$$

$$y_{a-d,f-h|e}^{R1b} + y_{a-d,f-h|e}^{C4b} - y_{a-b|c-d,f-h}^{C5a} \geq 0$$

$$y_{a-d,f-h|e}^{R1b} + y_{a-d,f-h|e}^{C4b} - y_{a-d|f-h}^{C5c} \geq 0$$

The inlet of deethanizer (C5b) is either from catalytic hydrogenation reactor (R1c) or extractive distillation (C4c).

$$Y_{c-d|f-h}^{C5b} \Rightarrow Y_{c-d,f-h|e}^{R1c} \vee Y_{c-d,f-h|e}^{C4c}$$

$$\neg Y_{c-d|f-h}^{C5b} \vee Y_{c-d,f-h|e}^{R1c} \vee Y_{c-d,f-h|e}^{C4c}$$

$$y_{c-d,f-h|e}^{R1c} + y_{c-d,f-h|e}^{C4c} - y_{c-d|f-h}^{C5b} \geq 0$$

The inlet of demethanizer (C6) is from depropanizer (C5c).

$$Y_{a-b|c-d}^{C6} \Rightarrow Y_{a-d|f-h}^{C5c}$$

$$\neg Y_{a-b|c-d}^{C6} \vee Y_{a-d|f-h}^{C5c}$$

$$y_{a-d|f-h}^{C5c} - y_{a-b|c-d}^{C6} \geq 0$$

The inlet of deethanizer (C7) is from demethanizer (C5a).

$$y_{a-b|c-d,f-h}^{C5a} - y_{c-d|f-h}^{C7} \geq 0$$

$$Y_{c-d|f-h}^{C7} \Rightarrow Y_{a-b|c-d,f-h}^{C5a}$$

$$\neg Y_{c-d|f-h}^{C7} \vee Y_{a-b|c-d,f-h}^{C5a}$$

The inlet to depropanizer (C8a) is either from deethanizer (C3a) or HP depropanizer (C1b).

$$Y_{f-h|j-l}^{C8a} \Rightarrow Y_{c-e|f-l}^{C3a} \vee Y_{a-h|f-l}^{C1b}$$

$$\neg Y_{f-h|j-l}^{C8a} \vee Y_{c-e|f-l}^{C3a} \vee Y_{a-h|f-l}^{C1b}$$

$$y_{c-e|f-l}^{C3a} + y_{a-h|f-l}^{C1b} - y_{f-h|j-l}^{C8a} \geq 0$$

The inlet to depropanizer (C8b) is either from deethanizer (C3b) or HP depropanizer (C2b).

$$Y_{f-h|j-k}^{C8b} \Rightarrow Y_{c-e|f-k}^{C3b} \vee Y_{a-h|f-k}^{C2b}$$

$$\neg Y_{f-h|j-k}^{C8b} \vee Y_{c-e|f-k}^{C3b} \vee Y_{a-h|f-k}^{C2b}$$

$$y_{c-e|f-k}^{C3b} + y_{a-h|f-k}^{C2b} - y_{f-h|j-k}^{C8b} \geq 0$$

The inlet of olefin cracking unit (OCU) is either from depropanizer (C8a) or depropanizer (C8b).

$$Y_{j-l}^{OCU} \Rightarrow Y_{f-h|j-l}^{C8a} \vee Y_{f-h|j-k}^{C8b}$$

$$\neg Y_{j-l}^{OCU} \vee Y_{f-h|j-l}^{C8a} \vee Y_{f-h|j-k}^{C8b}$$

$$y_{f-h|j-l}^{C8a} + y_{f-h|j-k}^{C8b} - y_{j-l}^{OCU} \geq 0$$

The inlet of MAPD(R2) is from either from C7, C5b, C5c, C8a or C8b.

$$Y_{f-h}^{R2} \Rightarrow Y_{c-d|f-h}^{C7} \vee Y_{c-d|f-h}^{C5b} \vee Y_{a-d|f-h}^{C5c} \vee Y_{f-h|j-l}^{C8a} \vee Y_{f-h|j-k}^{C8b}$$

$$\neg Y_{f-h}^{R2} \vee Y_{c-d|f-h}^{C7} \vee Y_{c-d|f-h}^{C5b} \vee Y_{a-d|f-h}^{C5c} \vee Y_{f-h|j-l}^{C8a} \vee Y_{f-h|j-k}^{C8b}$$

$$y_{c-d|f-h}^{C7} + y_{c-d|f-h}^{C5b} + y_{a-d|f-h}^{C5c} + y_{f-h|j-l}^{C8a} + y_{f-h|j-k}^{C8b} - y_{f-h}^{R2} \geq 0$$

The inlet to pressure swing absorber (PSA) is either from demethanizer (C1a), demethanizer (C2a), demethanizer (C5a) or demethanizer (C6).

$$Y_{a|b}^{PSA} \Rightarrow Y_{a-b|c-l}^{C1a} \vee Y_{a-b|c-k}^{C2a} \vee Y_{a-b|c-d,f-h}^{C5a} \vee Y_{a-b|c-d}^{C6}$$

$$\neg Y_{a|b}^{PSA} \vee Y_{a-b|c-l}^{C1a} \vee Y_{a-b|c-k}^{C2a} \vee Y_{a-b|c-d,f-h}^{C5a} \vee Y_{a-b|c-d}^{C6}$$

$$y_{a-b|c-l}^{C1a} + y_{a-b|c-k}^{C2a} + y_{a-b|c-d,f-h}^{C5a} + y_{a-b|c-d}^{C6} - y_{a|b}^{PSA} \geq 0$$

The inlet of debutanizer (C9) is from depropanizer (C8a).

$$Y_{j-k|l}^{C9} \Rightarrow Y_{f-h|j-l}^{C8a}$$

$$\neg Y_{j-k|l}^{C9} \vee Y_{f-h|j-l}^{C8a}$$

$$y_{f-h|j-l}^{C8a} - y_{j-k|l}^{C9} \geq 0$$

The inlet to ethylene splitter (C10) is either from catalytic hydrogenation reator (R1a), extractive distillation (C4a), depropanizer (C5) or demethanizer (C6) or deethanizer (C7).

$$y_{c-d|e}^{R1a} + y_{c-d|e}^{C4a} + y_{c-d|f-h}^{C5b} + y_{a-b|c-d}^{C6} + y_{c-d|f-h}^{C7} - y_{c|d}^{C10} \geq 0$$

$$Y_{c|d}^{C10} \Rightarrow Y_{c-d|e}^{R1a} \vee Y_{c-d|e}^{C4a} \vee Y_{c-d|f-h}^{C5b} \vee Y_{a-b|c-d}^{C6} \vee Y_{c-d|f-h}^{C7}$$

$$\neg Y_{c|d}^{C10} \vee Y_{c-d|e}^{R1a} \vee Y_{c-d|e}^{C4a} \vee Y_{c-d|f-h}^{C5b} \vee Y_{a-b|c-d}^{C6} \vee Y_{c-d|f-h}^{C7}$$

The inlet of C11 is from MAPD (R2)

$$Y_{f|g}^{C11} \Rightarrow Y_{f-h}^{R2}$$

$$\neg Y_{f|g}^{C11} \vee Y_{f-h}^{R2}$$

$$y_{f-h}^{R2} - y_{f|g}^{C11} \geq 0$$

The inlet to C4 hydrogenation reactor (R3) is either from debutanizer (C9), depropanizer (C8b), debutanizer (C3c) .

$$Y_{j|k}^{R3} \Rightarrow Y_{j-k|l}^{C9} \vee Y_{f-h|j-k}^{C8b} \vee Y_{c-h|j-k}^{C3c}$$

$$\neg Y_{j|k}^{R3} \vee \left( Y_{j-k|l}^{C9} \vee Y_{f-h|j-k}^{C8b} \vee Y_{c-h|j-k}^{C3c} \right)$$

$$y_{j-k|l}^{C9} + y_{f-h|j-k}^{C8b} + y_{c-h|j-k}^{C3c} - y_{j|k}^{R3} \geq 0$$

The inlet to extractive distillation (C12) is either from debutanizer (C9), depropanizer (C8b), debutanizer (C3c) or debutanizer (C2c).

$$Y_{j|k}^{C12} \Rightarrow Y_{j-k|l}^{C9} \vee Y_{f-h|j-k}^{C8b} \vee Y_{c-h|j-k}^{C3c} \vee Y_{a-h|j-k}^{C2c}$$

$$\neg Y_{j|k}^{C12} \vee Y_{j-k|l}^{C9} \vee Y_{f-h|j-k}^{C8b} \vee Y_{c-h|j-k}^{C3c} \vee Y_{a-h|j-k}^{C2c}$$

$$y_{j-k|l}^{C9} + y_{f-h|j-k}^{C8b} + y_{c-h|j-k}^{C3c} + y_{a-h|j-k}^{C2c} - y_{j|k}^{C12} \geq 0$$

The inlet of gasoline dehydrogenation reactor (R4) is either from debutanizer (C9) or debutanizer (C1c).

$$Y_l^{R4} \Rightarrow Y_{j-k|l}^{C9} \vee Y_{a-k|l}^{C1c}$$

$$\neg Y_l^{R4} \vee Y_{j-k|l}^{C9} \vee Y_{a-k|l}^{C1c}$$

$$y_{j-k|l}^{C9} + y_{a-k|l}^{C1c} - y_l^{R4} \geq 0$$

#### 4.4 Switching Constraints

To ensure that the non-existence of a process unit results in the corresponding input flowrates to the unit assuming the value of zero, we consider the formulation of big- $M$  logical constraints to impose the relations between the continuous variables, which in our case represent the flowrates of the streams, and the discrete binary 0–1 variables, which denote the existence of the streams and process units.

The general formulation of the big- $M$  logical constraints is given by:

$$\underline{F_k \leq M_k y_k} \quad (7)$$

where  $F_k$   $\equiv$  total flowrate of an input stream for process unit  $k$  in kg/day,

$M_k$   $\equiv$  maximum capacity of process unit  $k$

$y_k$   $\equiv$  existence or non existence of process unit  $k$ .

We could see that when  $y_k = 0$  (unit does not exist), then the constraint (7) becomes:

$$\underline{F_k \leq 0} \quad (8)$$

but flowrate variables are either zero or takes on positive values, so equation (8) becomes  $F_k = 0$ , which stipulates the condition of zero input flowrate into a non-existing unit. When  $y_k = 1$  (unit exists), then the constraint (7) becomes:

$$\underline{F_k \leq M_k} \quad (9)$$

which means that the input flowrate is bounded from above by the value of the big- $M$  constant. Here, it is clear that a suitable value for the big- $M$  constant is the maximum capacity of the unit.

For example equation (7), if the maximum capacity of a distillation column is equals to  $100 \text{ m}^3$ , then the big- $M$  logical constraint for that unit becomes

$$\underline{F_k \leq (100 \text{ m}^3) y_k} \quad (8)$$

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This constraint (7) is usually written for the input flowrate because it can be related to the output flowrates through the material balances.

The big- $M$  logical constraints are also sometimes termed as switching constraints in the literature (Rardin, 1998, p. 558). As mentioned, the main function of the switching constraints is to enforce the condition that no output flow exists if the unit does not exist. By extension, these constraints can be written as  $f_i \leq M_i z_i$  to relate the stream flowrate to the binary variable  $z_i$  denoting the existence of the stream itself (instead of the unit from where it is produced). In our proposed approach, this is written for each column with the big- $M$  constant, taken to be an arbitrarily large number, 1000, which it acts as an upper bound for the corresponding feed flow rate of the initial mixture.

**Table 998** Switching constraints for the separation subsystem using intermediate representation

Task/Process Unit	Switching Constraint
<b>C1</b>	$F^{C1a} \leq M_{C1a} y^{C1a}$ $F^{C1b} \leq M_{C1b} y^{C1b}$ $F^{C1c} \leq M_{C1c} y^{C1c}$
<b>C2</b>	$F^{C2a} \leq M_{C2a} y^{C2a}$ $F^{C2b} \leq M_{C2b} y^{C2b}$ $F^{C2c} \leq M_{C2c} y^{C2c}$
<b>C3</b>	$F^{C3a} \leq M_{C3a} y^{C3a}$ $F^{C3b} \leq M_{C3b} y^{C3b}$ $F^{C3c} \leq M_{C3c} y^{C3c}$
<b>R1</b>	$F^{R1a} \leq M_{R1a} y^{R1a}$ $F^{R1b} \leq M_{R1b} y^{R1b}$ $F^{R1c} \leq M_{R1b} y^{R1c}$
<b>C4</b>	$F^{C4a} \leq M_{C4a} y^{C4a}$ $F^{C4b} \leq M_{C4b} y^{C4b}$ $F^{C4c} \leq M_{C4c} y^{C4c}$

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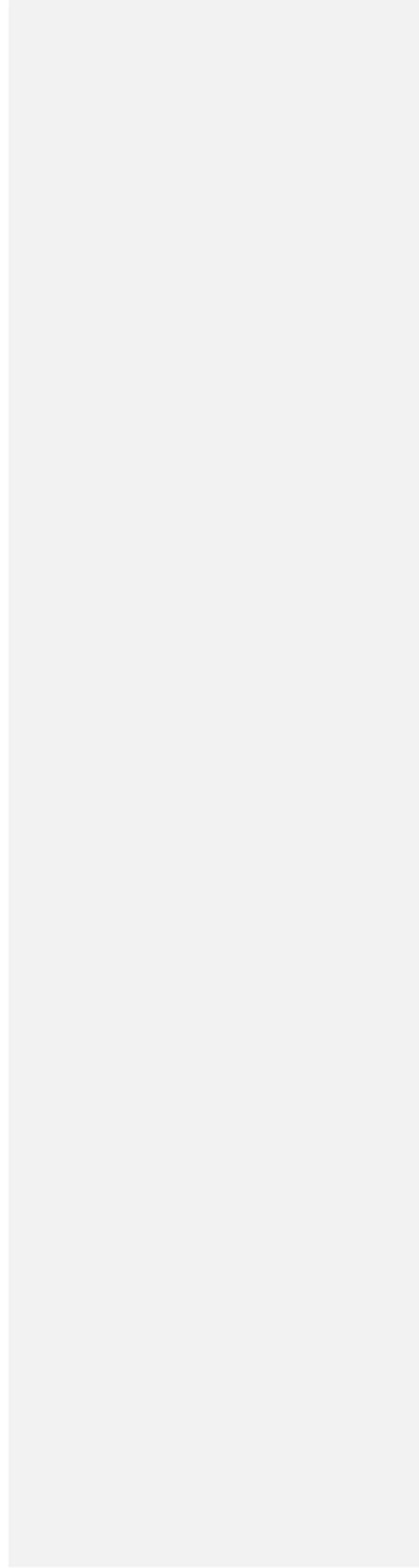
<b>C5</b>	$F^{C5a} \leq M_{C5a} y^{C5a}$ $F^{C5b} \leq M_{C5b} y^{C5b}$ $F^{C5c} \leq M_{C5c} y^{C5c}$
<b>C6</b>	$F^{C6} \leq M_{C6} y^{C6}$
<b>C7</b>	$F^{C7} \leq M_{C7} y^{C7}$
<b>C8</b>	$F^{C8a} \leq M_{C8a} y^{C8a}$ $F^{C8b} \leq M_{C8b} y^{C8b}$
<b>R2</b>	$F^{R2} \leq M_{R2} y^{R2}$
<b>C9</b>	$F^{C9} \leq M_{C9} y^{C9}$
<b>C10</b>	$F^{C10} \leq M_{C10} y^{C10}$
<b>C11</b>	$F_{8,9 \rightarrow 6,7}^{R2} \leq M_{C11} y_{67}^{C11}$
<b>R3</b>	$F^{R3} \leq M_{R3} y^{R3}$
<b>C12</b>	$F^{C12} \leq M_{C12} y^{C12}$
<b>Pressure Swing Absorber (PSA)</b>	$F^{PSA} \leq M_{PSA} y^{PSA}$
<b>Olefin Cracking Unit (OCU)</b>	$F_{OCU} \leq M_{OCU} y^{OCU}$
<b>R4</b>	$F^{R4} \leq M_{R4} y^{R4}$

The complete formulation of the optimization model for the distillation sequences for olefin production is [summarized as follows](#)~~presented as below~~:

$$\begin{aligned}
\min \quad & Z = \sum_{k \in COL} CAPEX_k y_k + \sum_{k \in COL} OPEX_k F_k \\
\text{s.t} \quad & \sum_{k \in FS_F} F_k = F_{TOT} \\
& \sum_{k \in PS_m} \xi_k F_k - \sum_{k \in FS_m} F_k = 0 \quad m \in IP \quad (\text{material balances for each intermediate product}) \\
& F_k \leq M_k y_k \quad \forall k \in COL \quad (\text{big-}M \text{ logical constraints}) \\
& \sum_{k \in FS_F} y_k = 1 \quad (\text{logical constraints on leading columns}) \\
& \sum_{k \in m} y_k \leq 1 \quad (\text{logical constraints on intermediate columns}) \\
& \sum_{k \in PS_m} y_k - \sum_{k \in FS_m} y_k \geq 0 \quad (\text{logical constraints on structural specifications}) \\
& y_k = 0 \text{ or } 1 \quad \forall k \in COL
\end{aligned}$$

The decision variables in this formulation are the binary variable,  $y_k$  and the flowrates to each column,  $F_k$ .

|



## CHAPTER 5

### COMPUTATIONAL EXPERIMENTS AND DISCUSSIONS ON NUMERICAL RESULTS

To demonstrate the implementation of the proposed model formulation for determining the optimal separation sequence, we consider different olefin feedstock [as the feed compositions](#) and by utilizing the method of integer cuts constraints.

#### 5.1 Comparison of distillation sequencing using different olefin feedstocks

Three cases of different olefin feedstock are evaluated using our proposed model formulation.

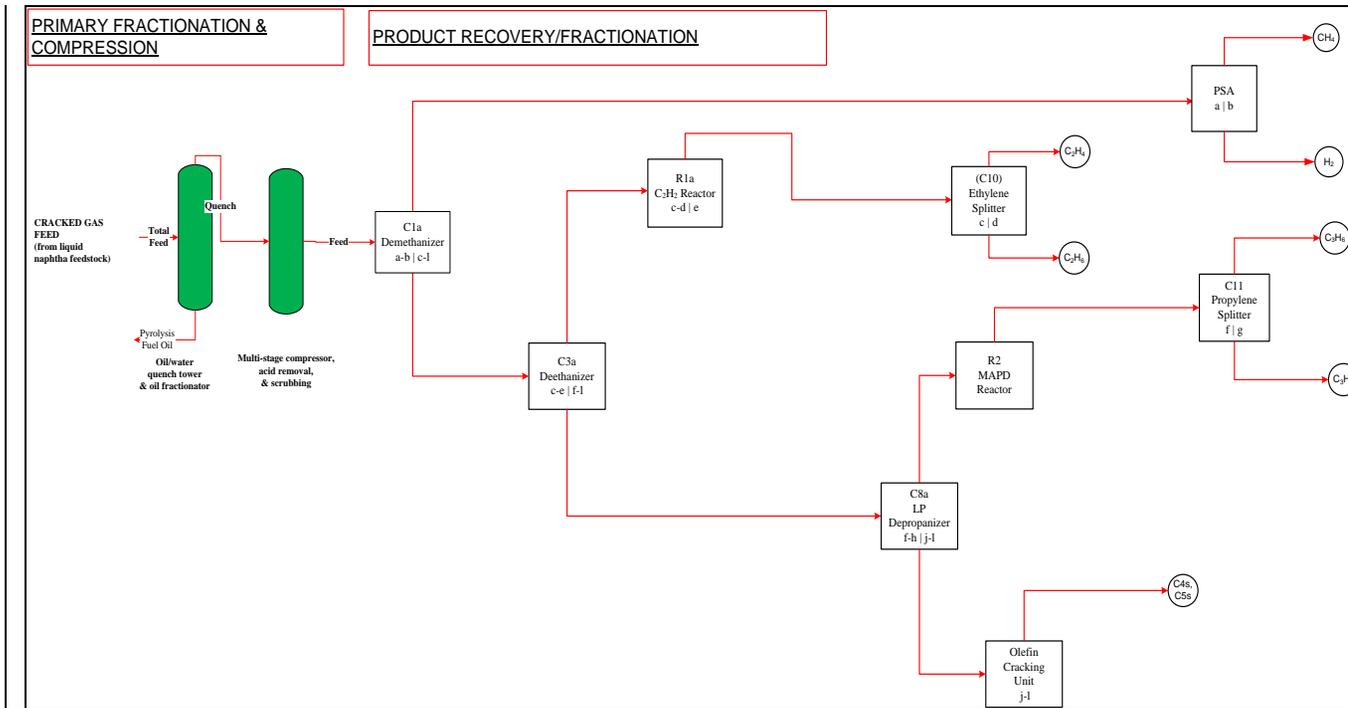
##### 5.1.1 Case 1: Ethane feedstock from Ethylene Polyethylene (M) Sdn. Bhd (EPEMSB)

Table ~~10109~~ Typical yields of ethane feedstock from EPEMSB

Feed Composition of Ethane Yield		
No:	Group of Compounds	Typical Yields (wt %)
a	Methane , CH <sub>4</sub>	24.56
b	Hydrogen ,H <sub>2</sub>	0.65
c	Ethane, C <sub>2</sub> H <sub>6</sub>	27.91
d	Ethylene , C <sub>2</sub> H <sub>4</sub>	41.83
e	Acetylene , C <sub>2</sub> H <sub>2</sub>	0.32
f	Propane , C <sub>3</sub> H <sub>8</sub>	0.22
g	Propylene, C <sub>3</sub> H <sub>6</sub>	1.12
h	Propadiene/ Methylacetyl , C <sub>3</sub> H <sub>4</sub>	0.02
j	Butadiene, 1,3-C <sub>4</sub> H <sub>6</sub>	1.23
k	C <sub>4</sub> s , Butene & Butane	0.35
l	Pyrolysis Gasoline	1.67
m	Fuel Oil	0.12

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This feed composition of ethane yield from EPMSB as shown in Table [9-10](#) is tested in our optimization model. The optimum distillation sequence from the result is shown in Figure [1211](#).



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Figure 12-6 Optimal flowsheet distillation sequence for Ethane Feedstock from EPMSB

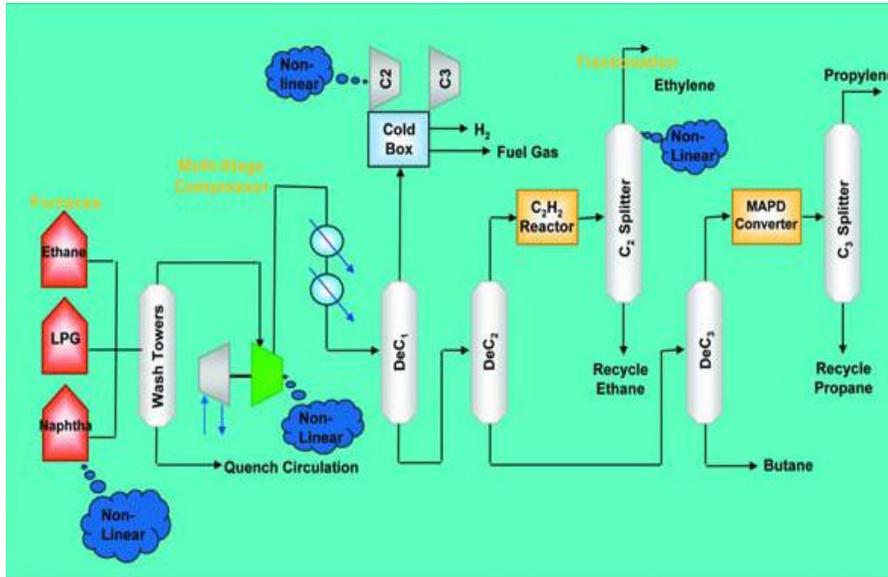


Figure 13 Flowsheet configuration for Ethylene Polyethylene (M) Sdn. Bhd., which uses ethane as the feedstock

Compared to the distillation column sequence of the existing configuration of the ethylene plant of Ethylene Polyethylene (M) Sdn. Bhd (Figure 13), which uses ethane as its feedstock, the optimal distillation sequence obtained from our computational experiments differs only in that the Pressure Swing Absorption (PSA) is also selected.

The optimal solution is in agreement with the following three common heuristic guidelines for distillation sequencing in accordance with Douglas et al. (1985):

- Heuristic 1. Remove the lightest component first and;
- Heuristic 2. Remove the most plentiful component first; and
- Heuristic 3: perform difficult separation last.

The optimal solution follows hHeuristic 1 as the first column is the demethanizer, which removes the lightest components of hydrogen and methane first. This is known as the direct sequence, which requires less energy as the light material (hydrogen and

methane) is vaporized once in the direct sequence. In another way, it requires less minimum vapor flow rate for reboiler duty and condenser duty.

~~The optimal solution also follows the Heuristic 2 as the bottom of demethanizer goes to deethanizer in order to remove the most plentiful components first, which is C2s at the top and C3s above at the bottom of the task Depropanizer (C3a).~~ Besides that, the optimal solution also performs the difficult separation last which is consistent with the Heuristic 3: e.g. propylene fractionator and ethylene fractionator.

### 5.1.2 Case 2: Naphtha Composition from University of Manchester's Centre for Process Integration (CPI) (2005)

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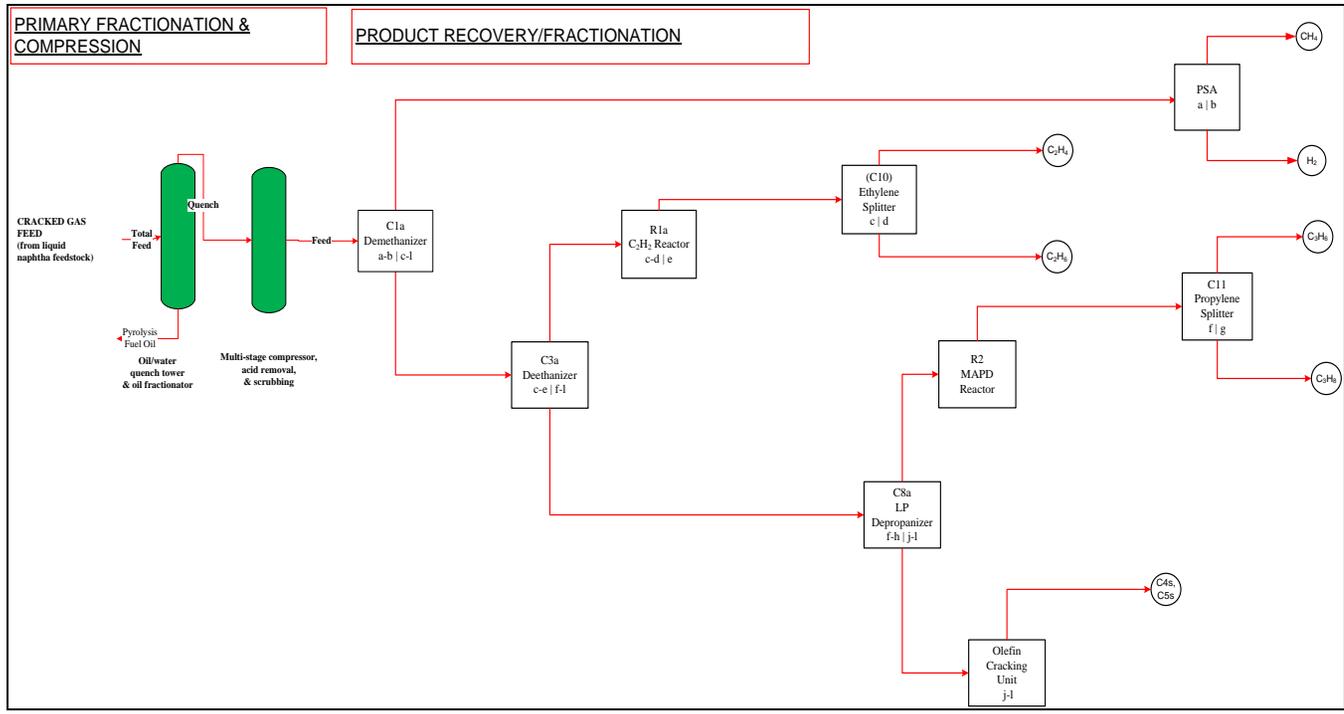
Table ~~11110~~ Typical yields of naphtha feedstock taken from ~~University of Manchester's Centre for Process Integration-CPI~~ (2005)

Feed Composition of Naphtha Cracking Yield from UMIST		
No:	Group of Compounds	Typical Yields (wt %)
a	Methane , CH <sub>4</sub>	15.3
b	Hydrogen ,H <sub>2</sub>	0.8
c	Ethane, C <sub>2</sub> H <sub>6</sub>	3.8
d	Ethylene , C <sub>2</sub> H <sub>4</sub>	29.3
e	Acetylene , C <sub>2</sub> H <sub>2</sub>	0.7
f	Propane , C <sub>3</sub> H <sub>8</sub>	0.3
g	Propylene, C <sub>3</sub> H <sub>6</sub>	14.1
h	Propadiene , C <sub>3</sub> H <sub>4</sub>	1.1
j	Butadiene, 1,3-C <sub>4</sub> H <sub>6</sub>	4.8
k	C <sub>4</sub> s , Butene & Butane	4.5
l	Pyrolysis Gasoline	21
m	Fuel Oil	3.8

The ~~is~~ feed composition of ~~typical~~ naphtha ~~typical~~ yield ~~as reported by~~ ~~from~~ ~~University of Manchester's Centre for Process Integration or University of Manchester's Centre for Process Integration-CPI, for short, (2005)~~ ~~is~~ ~~which~~ shown in Table ~~10-11~~ and ~~is~~ tested in our optimization model. The optimum distillation sequencing using ~~this~~ naphtha feedstock ~~from University of Manchester's Centre for Process Integration (2005)~~ produces ~~from~~ the ~~optimal flowsheet~~ result ~~is~~ shown in Figure ~~1412~~.

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**Figure 7**—Optimal flowsheet for distillation sequencing using naphtha composition from University of Manchester’s Centre for Process Integration (2005)

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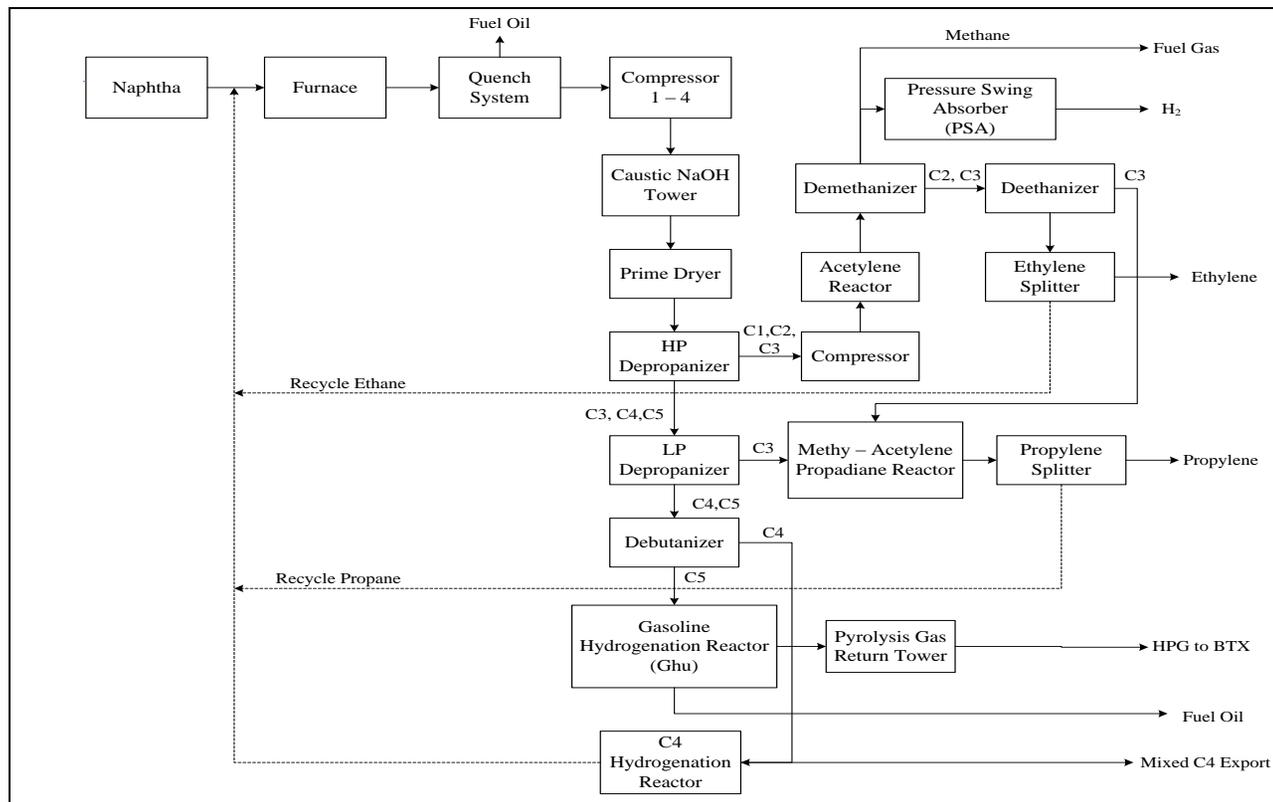
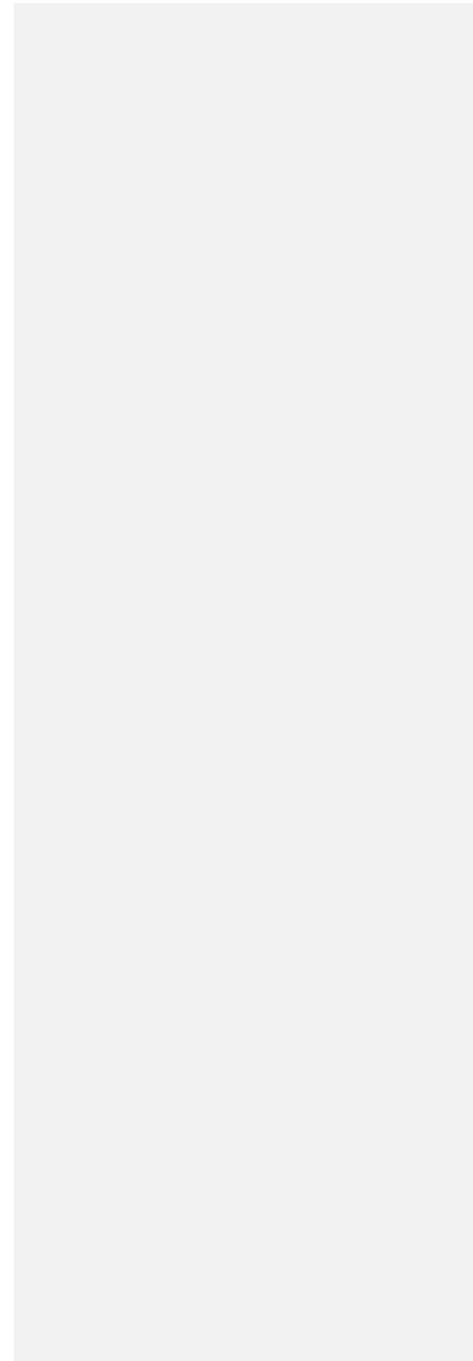
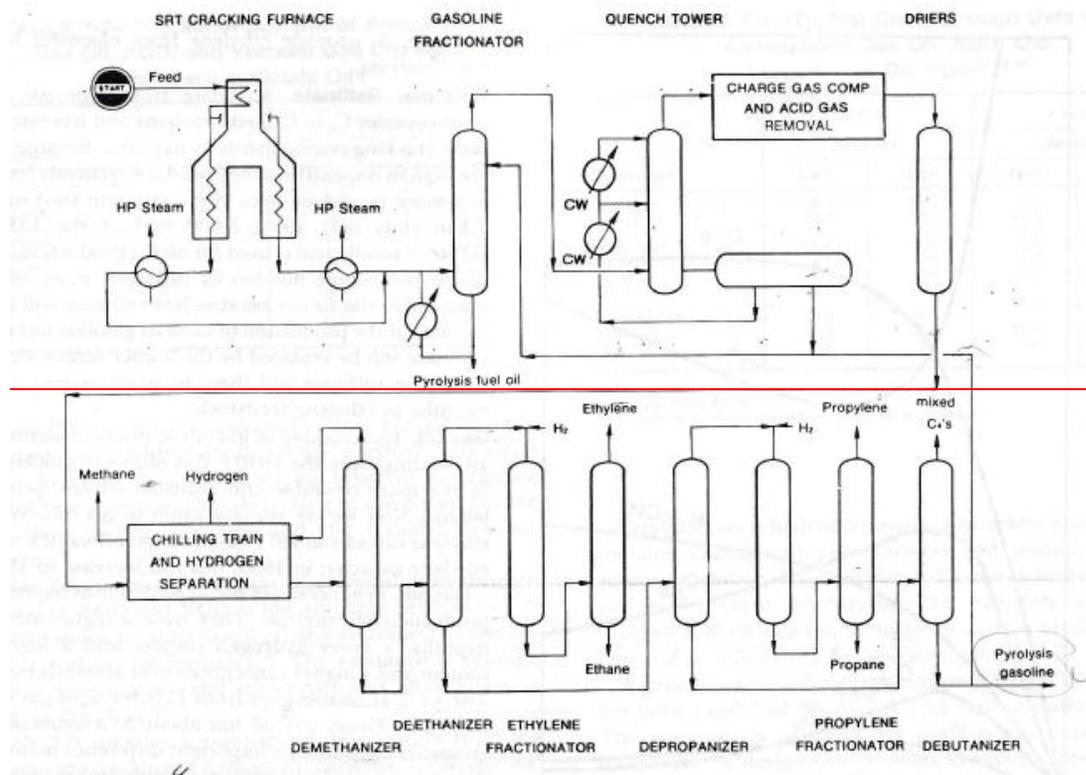


Figure 15.8 Flowsheet Configuration from Titan Petrochemicals (M) Sdn. Bhd

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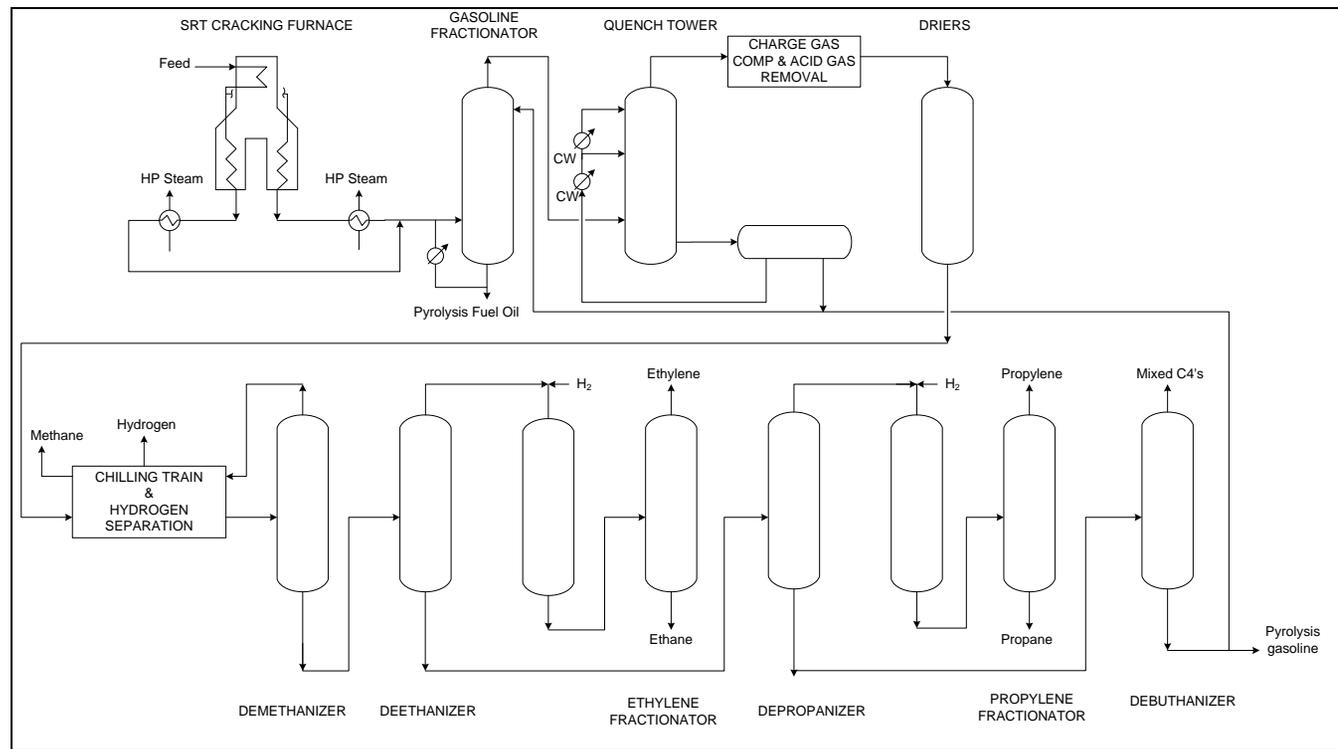


Figure 16-9 The C-E Lummus process for the cracking of naphtha or gas oil for the production of ethylene (Hydrocarbon Processing & Matar, 1975)

~~The optimal distillation sequence obtained from our computational experiments using naphtha composition from University of Manchester's Process Integration (2005) is different from Titan Petrochemical (M) Sdn. Bhd. However, the optimal distillation sequence obtained from our model formulation using naphtha composition from University of Manchester's Process Integration (2005) has the same demethanizer at the up front as the C-E Lummus process for the cracking of naphtha for the production of ethylene. The difference for C-E Lummus from optimal distillation sequencing solution are without the unit of PSA and debutanizer (Figure 16).~~

~~The optimal distillation sequence obtained from our computational experiments using the CPI naphtha composition is compared against the configuration of Titan Petrochemical (M) Sdn. Bhd, which uses a similar feedstock of liquid naphtha. The major difference is that Titan's configuration uses a high pressure (HP) depropanizer at the front-end. According to Meyer (2005, p. 6.60), a front-end depropanizer is used when propane and heavier materials are the primary cracked feed.~~

~~On the other hand, our optimal configuration based on CPI's naphtha composition as the feed has demethanizer at the front-end, similar to the C-E Lummus naphtha cracking process configuration for ethylene production. However, compared to our configuration, the C-E Lummus topology does not include ~~an acetylene reactor, a PSA, and an MAPD reactor.~~~~

~~For the Titan Petrochemicals (M) Sdn.Bhd (Figure 15), the distillation configuration is different by using depropanizer at the front end. According to Meyer (2005), front end depropanizer is used when propane and heavier material is the primary cracked feed.~~

~~From the~~It is seen from our computational results that both forms of feed composition of typical gaseous ethane feedstock (such as that of EPMSB) and typical ~~using~~ feedstock of ethane from EPMSB and feedstock of liquid naphtha feedstock (such as that of CPI (2005)) from University of Manchester's Process Integration (2005) ~~generates~~yield the same optimal configuration or topology of distillation sequencing.

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## 5.2. Optimal and Suboptimal Distillation Sequences using Integer Cuts

By incorporating ~~using~~ integer cuts, we can obtain the second best, ~~and the~~ third best, and subsequent “suboptimally best” ~~distillation configurations~~ solutions from the MILP ~~an integer program~~. According to Floudas and Paules (~~1988~~), it is important to consider the restriction of the branch and bound enumeration tree for the solution of an integer program is important in the solution of mathematical formulation. From, the integer cuts, we can thus compare the solutions in terms of the annualized cost and the total mass flow-rate. Integer cut is a

type of weak integer cut that could be derived are the ones that will ensure that those previously considered integer combinations cannot be encountered again. For the case when the integer combination is an element of some unit hypercube (i.e., binary variables), the following well-known integer cut will perform the above tasks.

Lemma (Duran and Grossmann, 1986), Given any integer combination with index sets  $B^i$ , s.t.  $|B^i| + |NB^i| = m$ , the integer constraint will be violated only by  $y_i$  and no other  $y_j, j \neq i$ . Note that  $|B^i|$  is the number of terms in the first summation.

### 5.2.1 Case 1: Ethane feedstock from Ethylene Polyethylene (M) Sdn. Bhd (EPMSB)

Table ~~12.12.1~~ Integer Cut for Ethane Gas Feedstock from EPMSB

Ethane Gas Feedstock						
	Best Solution	Flowrate (-ton/hr)	2 <sup>nd</sup> Best Solution	Flowrate (-ton/hr)	3 <sup>rd</sup> Best Solution	Flowrate (-ton/hr)
Distillation Sequence	C1a	998.9	C1a	998.8	C1a	998.80
	C3a	746.803	C3a	746.803	C3a	746.803
	PSA	251.997	PSA	251.997	PSA	251.997
	R1a	700.576	C4a	700.576	R1a	700.576
	C8a	46.227	C8a	46.227	C8a	46.227
	R2	13.679	R2	13.679	R2	13.679

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	C11	13.679	C11	13.679	<u>C11C12</u>	<u>13.679+5.845</u>
	C10	697.423	C10	697.423	<u>C10R4</u>	<u>697.423+6.704</u>
	OCU	32.548	OCU	32.548	<u>C9C11</u>	<u>32.548+3.679</u>
					<u>C12C10</u>	<u>15.845+697.423</u>
					<u>R4C9</u>	<u>16.704+32.548</u>
<u>Total Mass Flowrate (ton/hr)</u>		<u>3501.832</u>	<u>Total Mass Flow (ton/hr)</u>	<u>3501.832</u>		<u>3534.281</u>
		<u>3501.832</u>		<u>3501.832</u>		<u>3534.281</u>

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Table 11-12 lists shows the optimal and suboptimal distillation sequences integer cuts for the feed composition of ethane gas feedstock from EPMSB. The optimal solution and second<sup>nd</sup> best solution involves show lower the least total mass flow-rate (3501.831 ton/hr) compared to the third-3<sup>rd</sup> best solution, which is consistent with the heuristic of selecting the sequence with minimum total mass flow-rate.

By incorporating reducing appropriate integer cuts as constraints in the model formulation, task R1a (acetylene catalytic hydrogenation reactor) is selected in the optimal solution while the task C4a (extractive distillation) is selected in the second best solution. According to John McKetta and William Aaron (1984) in the authoritative McKetta's Encyclopedia of Chemical Processing and Design, if economically attractive, the acetylene may be recovered by extractive distillation. In most cases, it is simply hydrogenated to ethylene and ethane, which involves less equipment and a higher production of ethylene.

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5.2.2 Case 2: Naphtha Composition ~~off from University of Manchester's~~  
 Centre for Process Integration CPI (2005)

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Table ~~13-12~~ Integer cuts for naphtha liquid feedstock from University of Manchester's Centre for Process Integration (2005)

Naphtha Liquid Feedstock						
	Best Solution	Flow (ton/hr)	2 <sup>nd</sup> Best Solution	Flow (ton/hr)	3 <sup>rd</sup> Best Solution	Flow (ton/hr)
Distillation Sequence	C1a	961.80	C1a	961.80	C1a	961.80
	C3a	800.025	C3a	800.025	C3a	800.025
	PSA	161.775	PSA	161.775	PSA	161.775
	R1a	339.709	R1a	339.709	R1a	339.709
	C8a	460.316	C8a	460.316	C8a	460.316
	R2	155.785	R2	155.785	R2	155.785
	C11	155.785	R4	211.061	<del>R4</del> <sup>R3</sup>	<del>211.061</del> <sup>193.470</sup>
	C10	322.674	C12	93.470	<del>R3</del> <sup>R4</sup>	<del>93.470</del> <sup>11.061</sup>
	OCU	304.531	C11	155.785	C11	155.785
			C10	332.674	C10	332.674
		C9	304.531	C9	304.531	
Total Mass Flowrate (ton/hr)	3662.4		3976.931		3976.931	

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Table ~~12-13~~ lists the optimal and suboptimal distillation sequences for the feed composition of ~~shows the integer cuts for~~ naphtha liquid feedstock from ~~University of Manchester's Centre for Process Integration CPI~~ (2005). ~~The optimal sequence for the naphtha has the least total mass flow compared to the~~ ~~than 2<sup>nd</sup> second~~ best and ~~third~~<sup>3<sup>rd</sup></sup> best solutions, ~~although the two best suboptimal solutions share the same mass flowrate.~~ However, note that the process design textbook by Biegler, Grossmann, and Westerberg (1997) has reported an example in which

~~Referring to Andrevoich and Westerburg (1985) who developed the superstructure which has network of four components, also shown that the~~ ~~3<sup>rd</sup> third~~ best solution has a

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lower total mass flow-rate (~~2250 kmol/hr~~) than the second 2<sup>nd</sup>-best solution (~~en~~) (~~2400 kmol/hr~~).

·  
-

### 5.3 Computational Experiments

[Table 134](#) summarizes the problem size and statistics on the performance of computational experiments conducted in this work.

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Table ~~141413~~ Model size and Computational statistics of problem size performance

Type of model	Mixed-integer linear programming (MILP)
Solver for MILP	CPLEX
No. of continuous variables	35
No. of binary variables	79
No. of constraints	142
No. of iterations	24

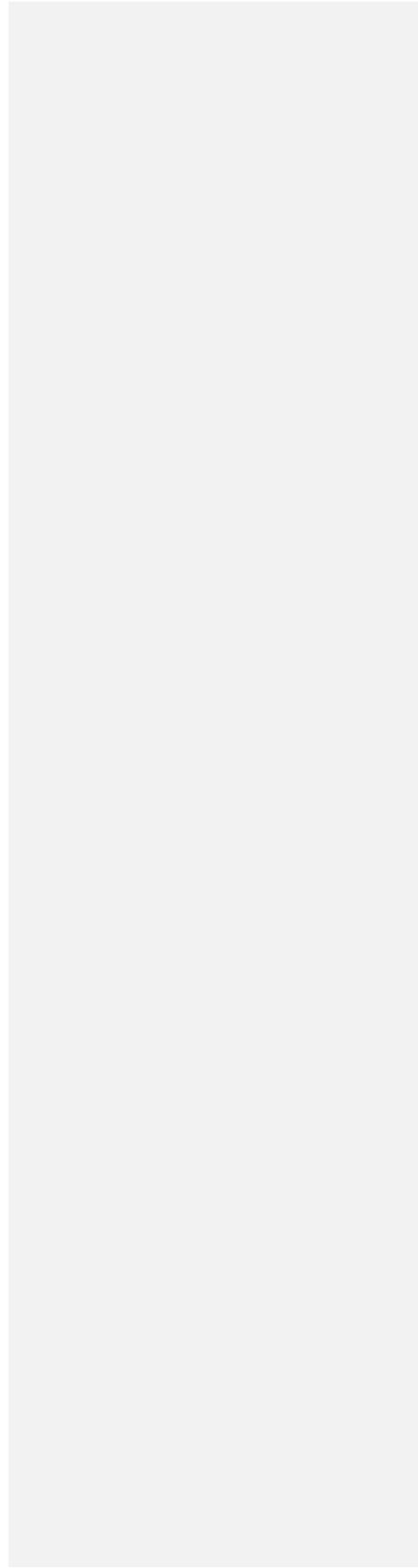
#### REMARKS ON COMPUTATIONAL EXPERIMENTS

☐ Solution of the MILP model using GAMS/CPLEX that does not account for the split flows between selections of parallel tasks will select task R1c in its optimal sequence.

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☐ Also, Assumption on 100% recovery is not accurate and impacts on the computational results.

|



## CHAPTER 5

### **CONCLUDING REMARKS & RECOMMENDATIONS FOR FUTURE WORK**

Comment [sufen1]:

#### **5.1. CONCLUDING REMARKS**

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~~The In conclusion,~~ intermediate representation superstructure ~~has been employed~~ used to represent the optimization approaches and strategies for distillation separation for olefin production. According to Caballero and Grossman (~~1999~~), the intermediate representation superstructure has shown ~~a~~ good performance in reaching the global optimal solution. Furthermore, ~~intermediate representation~~ this -superstructure form will involve s less number of equations compared to STN representation superstructure.

A MILP model has been developed by representing the discrete and continuous variables for distillation sequencing for olefin production. By using different feedstocks, the computational results yield the same optimal sequencing. The optimal solution obtained is further validate by the most common heuristic which is the selection of column sequencing with least total mass flow rate.

#### **5.2. RECOMMENDATIONS FOR FUTURE WORK**

An immediate future work is to conduct more rigorous computational experiments in order to investigate the governing parameter, i.e., the most important parameter ~~(s)~~ that determines the selection of the optimal distillation sequence. Feed composition does not appear to be the governing parameter. The logical constraints could be a probable

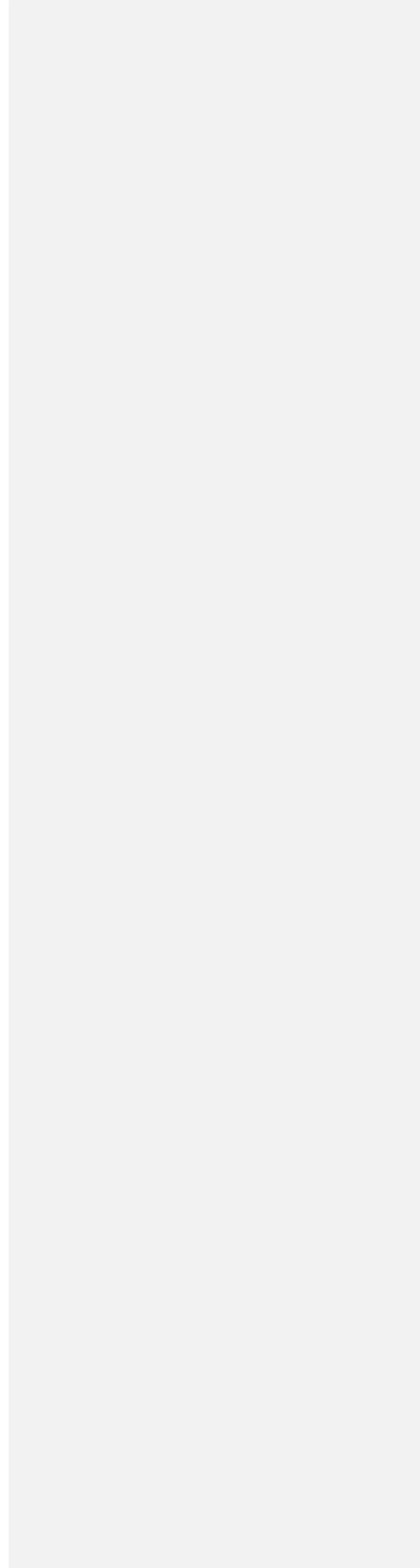
governing constraint that is too restrictive in its formulation, although more work is required to validate this preliminary hypothesis.

A more representative model could be developed by incorporating thermodynamic limitations on the operating process conditions such as temperature and pressure and the inclusion of important physical parameters such as relative volatility in distillation column separation. [As well, there are merits in considering the real-life features of ethylene plants such as the operations involving drying and chilling train at the front-end.](#)

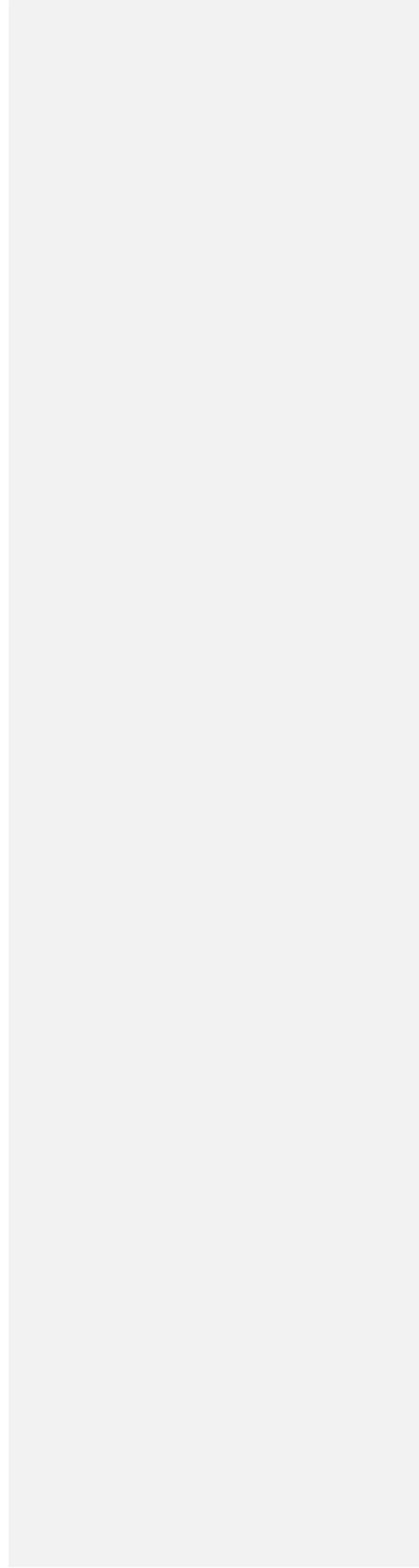
A more rigorous of objective function by considering the raw material cost, capital investment, production cost and profitability for the olefin production process in order to justify the feasibility of the olefin production.

Consideration of demand ~~and supply~~ constraints should be taken into account in the future work in order to integrate with the production planning and scheduling.

|



|



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## APPENDICES I

### GAMS CODE (Ethane/~~Naphtha~~)

;

GAMS Rev 146 x86/MS Windows 06/03/06 22:29:18 Page 1  
: Naphtha Separation  
C o m p i l a t i o n

```
 3  
 4  
 5  
*=====  
=  
=  
=====  
 6 *Declaration of Sets  
 7  
*=====  
=  
=  
=====  
 8 SETS  
 9 *the set of all tasks in superstructure  
10  
11 T Set of Task  
12 /  
13 OIL Fractionator  
14 QUENCH Fractionator  
15 FEED  
16 C1a,C1b,C1c  
17 C2a,C2b,C2c  
18 C3a,C3b,C3c  
19 PSA  
20 R1a,R1b,R1c  
21 C4a,C4b,C4c  
22 C8a,C8b  
23 R2,R3,R4  
24 C12,C11,C10,C9,C7,C6  
25 OCU  
26 C5a,C5b,C5c  
27  
28 /  
29  
30 U Set of Unit-Equipment-Column associated with different task  
31 /
```

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32 C1,C2,C3,C4,R1,R2,R3,R4,C8,C12,PSA,C10  
33  
34 /  
35  
36  
37 S Set of intermediate products (or streams or components)  
38 /  
39 al,m,ab,cl,ah,fl,ak,l,ck,fk,jk,ce,ch,cd,ad\_fh,cd\_fh,ad,fh,il  
40 /  
41  
42  
43 pm(T,S) ! maps tasks to "Intermediate Product" s  
streams( column produced)  
44 /  
45 (C1a,C2a,C6,C5a).ab  
46 (C1b,C2b,C2c).ah  
47 C1a.cl  
48 (C1b,C3a).fl  
49 C1c.ak  
50 (C1c,C9).l  
51 C2a.ck  
52 (C2b,C3b).fk  
53 (C2c,C3c,C8b,C9).jk  
54 (C3a,C3b).ce  
55 C3c.ch  
56 (R1a,C4a,C6,C7,C5b).cd  
57 (R1b,C4b).ad\_fh  
58 (R1c,C4c,C5a).cd\_fh  
59 C5c.ad  
60 (C5b,C5c,C7,C8a,C8b).fh  
61 C8a.il  
62  
63  
64 /  
65  
66  
67 fm(T,S) !Set maps Unit to "Intermediate Product Feed" Str  
reams- COlumn Directed  
68 /  
69 PSA.ab  
70 (R1b,C4b).ah  
71 C3a.cl  
72 C8a.fl  
73 (C2a,C2b,C2c).ak  
74 R4.l  
75 (C3b,C3c).ck  
76 C8b.fk  
77 (C12,R3).jk  
78 (R1a,C4a).ce  
79 (R1c,C4c).ch

80 C10.cd  
81 (C5a,C5c).ad fh  
82 (C7,C5b).cd fh  
83 C6.ad  
84 R2.fh  
85 (C9,OCU).jl  
86  
87  
88 /  
89  
90  
91 task\_producing\_IP(T,S) !Set for Logical Constraints for Structural task  
producing intermediate products  
92 /  
93 (C1a,C2a,C6,C5a).ab  
94 C1c.ak  
95 C1a.cl  
96 C2a.ck  
97 (C3a,C3b).ce  
98 (C1b,C2b,C2c).ad fh  
99 C3c.cd fh  
100 C5c.cd  
101 R2.fh  
102 (C3a,C1b).fl  
103 C8a.jl  
104 (R1a,C4a,C7,C6,C5b).cd  
105 (C9,C1c).l  
106  
107  
108 /  
109  
110  
111 IP\_feed\_to\_task(T,S) !Set for Logical Constraints for Structural Spec-F  
eed Source(From)  
112 /  
113 PSA.ab  
114 C2a.ak  
115 C2b.ak  
116 C2c.ak  
117 C3a.cl  
118 C3b.ck  
119 C3c.ck  
120 (C4a,R1a).ce  
121 (C4b,R1b).ad fh  
122 (C4c,R1c).cd fh  
123 C6.cd  
124 C11.fh  
125 C8a.fl  
126  
127 (C9,OCU).jl

128 C10.cd  
129 R4.l  
130  
131 /  
132  
133  
134 outlet column(T,S)  
135 /  
136 PSA.ab.C3a.cl  
137 (R1b,C4b).ah,C8a.fl  
138 (C2a,C2b,C2c).ak,R4.l  
139 (C3b,C3c).ck  
140 C8b.fk  
141 C12.jk  
142 (R1a,C4a).ce  
143 (R1c,C4c).ch,(R3).jk  
144 C10.cd,(C5a,C5c).ad fh,C5b.cd fh  
145 R2.fh,C6.ad  
146 (OCU,C9).jl  
147  
148  
149  
150 /  
151  
152 column(T,S)  
153 /  
154 C1a.(ab,cl)  
155 C1b.(ah,fl)  
156 C1c.(ak,l)  
157 C2a.(ab,ck)  
158 C2b.(ah,fk)  
159 C2c.(ah,ik)  
160 C3a.(ce,fl)  
161 C3b.(ce,fk)  
162 C3c.(ch,ik)  
163 (C4a,R1a).(cd)  
164 (C4b,R1b).(ad fh)  
165 (C4c,R1c).(cd fh)  
166 C5a.(ab)  
167 C5b.(cd,fh)  
168 C5c.(ad,fh)  
169 C6.(ab,cd)  
170 C7.(cd,fh)  
171 C8a.(fh,il)  
172 C8b.(fh,ik)  
173 C9.(ik,l)  
174  
175  
176 /  
177

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```

178
179
180 ;
181
182
183
184 ALIAS (S,S1);
185 ALIAS (T,T1);
186
=====
≡
=====
187 *Declaration of Parameters for rest of model
188
=====
≡
=====
189 PARAMETER
190
191 M(T) Big M Constant-1000 is the upper bound as it corresponds to the fee
d flow rate of the initial mixture;
192
193 M(T)=1000;
194
195 PARAMETER
196
197 spltfrc(T,S) Split Fraction maps to unit to Intermediate Product str
eams
198 /
199 QUENCH_FRACTIONATOR.al 0.9988,
200 OIL_FRACTIONATOR.m 0.0012,
201 C1a.ab 0.2523,
202 C1a.cl 0.7477,
203 C1b.ah 0.9798,
204 C1b.fl 0.0202,
205 C1c.ak 0.9833,
206 C1c.l 0.0167,
207 C2a.ab 0.2566,
208 C2a.ck 0.7434,
209 C2b.ah 0.9883,
210 C2b.fk 0.0117,
211 C2c.ah 0.9839,
212 C2c.jk 0.0161,
213 C3a.ce 0.9381,
214 C3a.fl 0.0619,
215 C3b.ce 0.9596,
216 C3b.fk 0.0404,
217 C3c.ch 0.9783,
218 C3c.jk 0.0217,
219 C4a.cd 0.9955,

```

```

220 C4b.ad fh 0.9967,
221 C4c.cd fh 0.9955,
222 C5a.ab 0.2617,
223 C5a.cd fh 0.7383,
224 C5b.cd 0.9808,
225 C5b.fh 0.0192,
226 C5c.ad 0.9858,
227 C5c.fh 0.0142,
228 R1a.cd 0.9955,
229 R1b.ad fh 0.9967,
230 R1c.cd fh 0.9955,
231 C8a.fh 0.2959,
232 C8a.il 0.7041,
233 C8b.fh 0.4633,
234 C8b.jk 0.5367,
235 C6.ab 0.2655,
236 C6.cd 0.7345,
237 C9.jk 0.4868,
238 C9.l 0.5132,
239 C7.cd 0.9808,
240 C7.fh 0.0192
241
242
243 /
244
245 *Ethylene Production = 450 kT/year
246 Fixed_Cost(T) Fixed Cost per year (for ethane: 56 $ per ton C2H4 in
Middle East)
247 Operating_Cost(T) Operating Cost or total production cost(140 $ per ton
C2H4 in Middle East)
248 ;
249
250 Fixed_Cost(T) = 56000; #(in unit of $/year)
251 Operating_Cost(T) = 140000;
252 ;
253
254
255
256
=====
≡
=====
257 *Define scalar quantities for rest of model
258
=====
≡
=====
259
260 SCALARS
261

```

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```

262 TOTFEED total feed flow rate(feedstock in tonnage) to superstructure /1
    000/;
263 *646
264
265
*=====
≡
=====
266 *Declaration of variables
267
*=====
≡
=====
268 VARIABLE
269 Z Objective function
270
271 ;
272
273 BINARY VARIABLES
274 Y(T) Columns selection in superstruture associated with T Tasks(exist
    ance Or Non-existence)
275 ;
276
277 POSITIVE VARIABLES
278 F(T) Flow Rate of selected T task associated with S streams
279 Fraction(T)
280 ;
281
282
*=====
≡
=====
283 *Declaration of Equations
284
*=====
≡
=====
285 *for material balances around unit, mixers, splitters
286 *for logical constraints on design specifications, structural specificatio
    ns.
287 *for switching constraints
288
289 EQUATIONS
290 OBJECTIVE Objective function
291 TotalFeed, Oil, Feed Column
292 Initial FEED Initial Column Feed to superstructure
293
294 MB Unit Material Balances for Unit
295 MB C11
296

```

297  
298  
299 \*SPLIT1,SPLIT2,SPLIT3,SPLIT4,SPLIT5,SPLIT6,SPLIT7,SPLIT8  
300  
301 DS1  
302 DS2  
303 DS3  
304 DS4  
305 DS5  
306 DS6a,DS6b,DS6c  
307 DS7  
308 DS9  
309 DS8  
310  
311  
312  
313 Inlet(T,S) \_\_\_\_\_ Inlet Condition  
314 InletC5a,InletC5b,InletC5c,InletC7,InletR2,InletC8b  
315  
316 STRUCTURAL SPEC LC(T,S) Overhead & Bottom  
317 SP\_C5a  
318 BigM \_\_\_\_\_ Big M Logical Constraints-Switching Constraints with T ta  
\_\_\_\_\_  
sks  
319 \*INTEGER CUT 1  
320 \*\$ontext  
321 \*CUTS 2nd Optimum  
322 \*CUTS 3rd Optimum  
323 \*\$offtext  
324 ;  
325  
326 \*\*\*\*\*Objective Function\*\*\*\*\*  
\*\*\*\*\*  
327 \*OBJECTIVE.. Z=E= SUM(T, Capital\_Cost(T)\*SUM(T,F(T));  
328 OBJECTIVE.. Z=E= SUM(T,Fixed\_Cost(T)\*Y(T)) + SUM(T,Operating\_Cost(T)\*  
F(T));  
329  
330  
331  
332 \*Initial Feed to Superstructure  
333  
334 TotalFeed.. TOTFEED =E= spltfrc('QUENCH\_FRACTIONATOR','al')\*F('QUENCH  
FRACTIONATOR') + spltfrc('OIL\_FRACTIONATOR','m')\*F('OIL\_FRACTIONATOR');  
335  
336  
337 Oil.. F('OIL\_FRACTIONATOR')=E= (TOTFEED-F('FEED'))/ spltfrc('OI  
L\_FRACTIONATOR','m');  
338 \*Cannot find the flow rate of Oil Fractionaor  
339  
340 Feed\_Column.. spltfrc('QUENCH\_FRACTIONATOR','al')\*F('QUENCH\_FRACTIONATO  
R')-F('FEED')=E=0;

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341  
 342 Initial FEED..  $F(\text{FEED}) = E = F(\text{C1a}) + F(\text{C1b}) + F(\text{C1c});$   
 343  
 344  
 345 \*Unit/Task  
 346 MB\_Unit(S)..  $\text{SUM}(T\$pm(T,S), \text{spltfrc}(T,S)*F(T)) = E = \text{SUM}(T \$ fm(T,S), F(T)$   
 347  $);$   
 348 MB\_C11..  $F(\text{R2}) = E = F(\text{C11});$   
 349  
 350  
 SPLIT1..  $F(\text{R1c}) = E = \text{Fraction}(\text{R1c}) * \text{spltfrc}(\text{C3c}, \text{ch}) * F(\text{C3c});$   
 SPLIT2..  $F(\text{C4c}) = E = \text{Fraction}(\text{C4c}) * \text{spltfrc}(\text{C3c}, \text{ch}) * F(\text{C3c});$   
 SPLIT3..  $F(\text{R1b}) = E = \text{Fraction}(\text{R1b}) * (\text{spltfrc}(\text{C1b}, \text{ah}) * F(\text{C1b}) + \text{spltfrc}(\text{C2b}, \text{ah}) * F(\text{C2b}) + \text{spltfrc}(\text{C2c}, \text{ah}) * F(\text{C2c}));$   
 SPLIT4..  $F(\text{C4b}) = E = \text{Fraction}(\text{C4b}) * (\text{spltfrc}(\text{C1b}, \text{ah}) * F(\text{C1b}) + \text{spltfrc}(\text{C2b}, \text{ah}) * F(\text{C2b}) + \text{spltfrc}(\text{C2c}, \text{ah}) * F(\text{C2c}));$   
 SPLIT5..  $F(\text{R1a}) = E = \text{Fraction}(\text{R1a}) * (\text{spltfrc}(\text{C3a}, \text{ce}) * F(\text{C3a}) + \text{spltfrc}(\text{C3b}, \text{ce}) * F(\text{C3b}));$   
 SPLIT6..  $F(\text{C4a}) = E = \text{Fraction}(\text{C4a}) * (\text{spltfrc}(\text{C3a}, \text{ce}) * F(\text{C3a}) + \text{spltfrc}(\text{C3b}, \text{ce}) * F(\text{C3b}));$   
 SPLIT7..  $F(\text{R3}) = E = \text{Fraction}(\text{R3}) * (\text{spltfrc}(\text{C2c}, \text{jk}) * F(\text{C2c}) + \text{spltfrc}(\text{C3c}, \text{jk}) * F(\text{C3c}) + \text{spltfrc}(\text{C8b}, \text{jk}) * F(\text{C8b}) + \text{spltfrc}(\text{C9}, \text{jk}) * F(\text{C9}));$   
 SPLIT8..  $F(\text{C12}) = E = \text{Fraction}(\text{C12}) * (\text{spltfrc}(\text{C2c}, \text{jk}) * F(\text{C2c}) + \text{spltfrc}(\text{C3c}, \text{jk}) * F(\text{C3c}) + \text{spltfrc}(\text{C8b}, \text{jk}) * F(\text{C8b}) + \text{spltfrc}(\text{C9}, \text{jk}) * F(\text{C9}));$   
 368  
 369  
 370 \*Only One Task is selected for Every unit  
 371 DS1..  $Y(\text{C1a}) + Y(\text{C1b}) + Y(\text{C1c}) = E = 1;$   
 372  
 373 \*No more than 1 process allowed( none or 1 process selected)  
 374 DS2..  $Y(\text{C2a}) + Y(\text{C2b}) + Y(\text{C2c}) = L = 1;$   
 375 DS3..  $Y(\text{C3a}) + Y(\text{C3b}) + Y(\text{C3c}) = L = 1;$   
 376 DS4..  $Y(\text{R1a}) + Y(\text{R1b}) + Y(\text{R1c}) = L = 1;$   
 377 DS5..  $Y(\text{C4a}) + Y(\text{C4b}) + Y(\text{C4c}) = L = 1;$   
 378  
 379 \*More than 1 process allowed( None, 1 or 2 process selected)  
 380  
 381 DS6a..  $Y(\text{R1a}) + Y(\text{C4a}) = L = 2;$   
 382 DS6b..  $Y(\text{R1b}) + Y(\text{C4b}) = L = 2;$   
 383 DS6c..  $Y(\text{R1c}) + Y(\text{C4c}) = L = 2;$

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384  
385 \*No more than 1 process allowed( none or 1 process selected)  
386 DS7.. Y('C5a')+ Y('C5b')+ Y('C5c')=L=1;  
387 DS8.. Y('C8a')+ Y('C8b')=L=1;  
388  
389 \*More than 1 process allowed( None, 1 or 2 process selected)  
390  
391 DS9.. Y('R3')+ Y('C12')=L=2;  
392  
393  
394 \*Big-M Logical Constraints  
395 BigM(T).. F(T)=L=M(T)\*Y(T);  
396  
397 \*Limit Choice of Overhead & Bottom  
398 STRUCTURAL SPEC LC(T,S)\$column(T,S).. SUM(T1 \$ outlet\_column(T1,S), Y(T1  
) - Y(T) =G= 0;  
399  
400 SP C5a.. Y('C7')-Y('C5a') =G=0;  
401  
402  
403 \*Inlet Condition  
404 Inlet(T,S) \$ IP\_feed to task(T,S).. SUM( T1 \$ task\_producing\_IP(T1,S),  
Y(T1) ) - Y(T) =G= 0;  
405  
406 InletC5a.. Y('C4b')+Y('R1b')-Y('C5a')=G=0;  
407 InletC5b.. Y('C4c')+ Y('R1c') -Y('C5b')=G=0;  
408 InletC5c.. Y('C4b')+Y('R1b')-Y('C5c')=G=0;  
409  
410 InletC7.. Y('C5a')-Y('C7')=G=0;  
411 InletR2.. Y('C5b')+Y('C5c')+Y('C7')+Y('C8a')  
+Y('C8b')-Y('R2')=G=0;  
412  
413 InletC8b.. Y('C3b')+Y('C2b')-Y('C8b')=G=0;  
414  
415 \*Integer Cuts to obtain second best solution  
416 \*CUTS 2nd Optimum.. Y('OIL Fractionator') + Y('QUENCH  
Fractionator')+ Y('FEED')+Y('C1a') + Y('C3a')+Y('PSA')+Y('R1a')+Y('C8a')+Y  
('R2')+Y('C11')+Y('C10')+Y('OCU')=L= 11 ;  
417  
418 \*Integer Cuts to obtain 3rd best solution  
419 \*CUTS 3rd Optimum.. Y('OIL Fractionator') + Y('QUENCH  
Fractionator')+ Y('FEED')+Y('C1a')+ Y('C3a')+ Y('PSA')+Y('C4A')+Y('C8a')+Y  
('R2')+Y('C11')+Y('C10')+Y('OCU')=L=11 ;  
420  
421  
422 \*Integer Cuts to obtain second best solution  
423 \*Cuts(k).. sum(T, sign(ycolk(T,k)-0.5)\*Y(T)) =| sum(T,ycol  
k(T,k) ) - 1;  
424  
425

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426 \*sum(i,sign(ycolk(i,k)-0.5)\*ycol(i)) =L= sum(i,ycolk(i,k)) - 1;  
427 \*INTEGER CUT 1.. Y('OIL Fractionator') + Y('QUENCH Fractionator') + Y('FEED') + Y('C1c') + Y('C2a') + Y('C3c') + Y('C5b') + Y('PSA') + Y('R1c')  
+ Y('C4c') + Y('R2') + Y('R3') + Y('R4') + Y('C10') + Y('C11') + Y('C12')  
+ Y('C13') =L= 15;

428

429

Y('C13')-Y('R4')=G=0;      directed    SP  
Y('R4')-Y('C13')=G=0;      inlet of C13

Y('C14')-Y('C13')=G=0;      bottom    SP  
Y('C13')-Y('C14')=G=0;      inlet of C14

Y('C15')-Y('C14')=G=0;      bottom    SP  
Y('C14')-Y('C15')=G=0;      inlet of C15

Y('C16')-Y('C15')=G=0;      bottom    SP  
Y('C15')-Y('C16')=G=0;      inlet of C16

Y('R5')-Y('C16')=G=0;      top        SP  
Y('C16')-Y('R5')=G=0;      inlet of R5

Y('C17')-Y('R5')=G=0;      directed    SP  
Y('R5')-Y('C17')=G=0;      inlet of C17

Y('C18')-Y('C17')=G=0;      bottom    SP  
Y('C17')-Y('C18')=G=0;      inlet of C18

Y('C18')-Y('C19')=G=0;      inlet C19  
Y('C20')-Y('C19')=G=0;      SP

Y('C19')-Y('C18')=G=0;    overhead    SP  
Y('C20')-Y('C18')=G=0;    bottom      SP

Y('C18')+Y('C19') -Y('C20')=G=0;    inlet of C20

Y('C21')-Y('C20')=G=0;      directed    SP  
Y('C20')-Y('C21')=G=0;      inlet of C21

465

466 ;

467

468

469

470 MODEL NAPHTHA

471 /

472 ALL

473

474 /;

```
475
476 *Initial values and bound are given to avoid getting stuck at an infeasible
point wen the NLP solver starts up
477
478
479 F.up(T)=TOTFEED;
480 Y.up(T)=1;
481
482
483 Fraction.LO(T) = 0.00;
484 Fraction.UP(T) = 1.00;
485
486
487 *OPTION
488 OPTION
489 *MINLP = BARON
490 MIP = CPLEX
491 *MINLP = SBB
492 *MINLP = DICOPT # DICOPT returns infeasible solution to this problem
493 LIMROW = 0
494 LIMCOL = 0
495 ;
496
497
498
499
500
501 SOLVE NAPHTHA USING MIP MINIMIZING Z
502 ;
503
504 DISPLAY Z,L, Y,L, F,L;

COMPILATION TIME = 0.010 SECONDS 3 Mb WIN223-146 Nov 21, 2006
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GAMS Rev 146 x86/MS Windows 06/03/06 22:29:18 Page 2  
: Naphtha Separation  
Model Statistics SOLVE NAPHTHA Using MIP From line 501

MODEL STATISTICS

BLOCKS OF EQUATIONS	28	SINGLE EQUATIONS	134
BLOCKS OF VARIABLES	3	SINGLE VARIABLES	69
NON ZERO ELEMENTS	419	DISCRETE VARIABLES	34

GENERATION TIME = 0.010 SECONDS 4 Mb WIN223-146 Nov 21, 2006

EXECUTION TIME = 0.020 SECONDS 4 Mb WIN223-146 Nov 21, 2006

SOLVE SUMMARY

MODEL NAPHTHA      OBJECTIVE Z  
TYPE MIP            DIRECTION MINIMIZE  
SOLVER CPLEX        FROM LINE 501

\*\*\*\* SOLVER STATUS 1 NORMAL COMPLETION  
 \*\*\*\* MODEL STATUS 8 INTEGER SOLUTION  
 \*\*\*\* OBJECTIVE VALUE 910746413.5937

RESOURCE USAGE, LIMIT 0.240 1000.000  
ITERATION COUNT, LIMIT 24 10000

GAMS/Cplex Nov 27, 2006 WIN.CP.CP 22.3 032.035.041.VIS For Cplex 10.1  
 Cplex 10.1.0, GAMS Link 32

Solution satisfies tolerances.

MIP Solution: 910746413.593735 (24 iterations, 0 nodes)  
Final Solve: 910746413.593724 (0 iterations)

Best possible: 910682452.747934  
Absolute gap: 63960.845801  
Relative gap: 0.000070

LOWER LEVEL UPPER MARGINAL

---- EQU OBJECTIVE . . . . . 1.000  
 ---- EQU TotalFeed -1000.000 -1000.000 -1000.000 -1.160E+8  
 ---- EQU Oil 8.3333E+5 8.3333E+5 8.3333E+5 756.998  
 ---- EQU Feed Colu~ . . . . .  
 ---- EQU Initial F~ . . . . . -4.908E+5

OBJECTIVE Objective function  
Initial FEED Initial Column Feed to superstructure

---- EQU MB\_Unit Material Balances for Unit

LOWER LEVEL UPPER MARGINAL

ab . . . . . -1.400E+5  
 cl . . . . . -4.220E+5  
 ah . . . . .  
 fl . . . . . -3.214E+5

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```

ak . . . . .
l . . . . .
ck . . . . .
fk . . . . .
jk . . . . .
ce . . . . . -2.794E+5
ch . . . . .
cd . . . . . -1.400E+5
ad fh . . . . .
cd fh . . . . .
ad . . . . .
fh . . . . . -2.800E+5
jl . . . . . -1.400E+5

```

LOWER LEVEL UPPER MARGINAL

```

---- EQU MB C11 . . . . . -1.400E+5
---- EQU DS1 1.000 1.000 1.000 .
---- EQU DS2 -INF . 1.000 .
---- EQU DS3 -INF 1.000 1.000 .
---- EQU DS4 -INF 1.000 1.000 .
---- EQU DS5 -INF . 1.000 .
---- EQU DS6a -INF 1.000 2.000 .
---- EQU DS6b -INF . 2.000 .
---- EQU DS6c -INF . 2.000 .
---- EQU DS7 -INF . 1.000 .
---- EQU DS9 -INF . 2.000 .
---- EQU DS8 -INF 1.000 1.000 .

```

---- EQU Inlet Inlet Condition

LOWER LEVEL UPPER MARGINAL

```

C2a.ak . . . . . +INF .
C2b.ak . . . . . +INF .
C2c.ak . . . . . +INF .
C3a.cl . . . . . +INF .
C3b.ck . . . . . +INF .
C3c.ck . . . . . +INF .
PSA.ab . . . . . +INF .
R1a.ce . . . . . +INF .
R1b.ad fh . . . . . +INF .
R1c.cd fh . . . . . +INF .
C4a.ce . . . . . 1.000 +INF .
C4b.ad fh . . . . . +INF .
C4c.cd fh . . . . . +INF .
C8a.fl . . . . . +INF .
R4 .l . . . . . +INF .
C11.fh . . . . . +INF .
C10.cd . . . . . +INF .

```

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C9 .jl	1.000	+INF
C6 .cd	1.000	+INF
OCU.jl		+INF

LOWER LEVEL UPPER MARGINAL

---- EQU InletC5a		+INF
---- EQU InletC5b		+INF
---- EQU InletC5c		+INF
---- EQU InletC7		+INF
---- EQU InletR2		+INF
---- EQU InletC8b		+INF

---- EQU STRUCTURAL SPEC LC Overhead & Bottom

LOWER LEVEL UPPER MARGINAL

C1a.ab		+INF
C1a.cl		+INF
C1b.ah		+INF
C1b.fl	1.000	+INF
C1c.ak		+INF
C1c.l		+INF
C2a.ab	1.000	+INF
C2a.ck		+INF
C2b.ah		+INF
C2b.fk		+INF
C2c.ah		+INF
C2c.jk		+INF
C3a.fl		+INF
C3a.ce		+INF
C3b.fk		+INF
C3b.ce	1.000	+INF
C3c.jk		+INF
C3c.ch		+INF
R1a.cd		+INF
R1b.ad fh		+INF
R1c.cd fh		+INF
C4a.cd	1.000	+INF
C4b.ad fh		+INF
C4c.cd fh		+INF
C8a.fh		+INF
C8a.jl		+INF
C8b.jk		+INF
C8b.fh	1.000	+INF
C9 .l		+INF
C9 .jk		+INF
C7 .cd	1.000	+INF
C7 .fh	1.000	+INF
C6 .ab	1.000	+INF

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C6.cd	1.000	+INF
C5a.ab	1.000	+INF
C5b.cd	1.000	+INF
C5b.fh	1.000	+INF
C5c.ad		+INF
C5c.fh	1.000	+INF

LOWER	LEVEL	UPPER	MARGINAL
-------	-------	-------	----------

---- EQU SP\_C5a . . . . +INF .

---- EQU BigM\_Big M Logical Constraints-Switching Constraints with T tasks

LOWER	LEVEL	UPPER	MARGINAL
-------	-------	-------	----------

OIL Fractionator	-INF	
QUENCH Fractionator	-INF	
FEED	-INF	-1.200
C1a	-INF	-1.200
C1b	-INF	-3.443E+5
C1c	-INF	-3.508E+5
C2a	-INF	
C2b	-INF	
C2c	-INF	
C3a	-INF	-253.197
C3b	-INF	
C3c	-INF	
PSA	-INF	-748.003
R1a	-INF	-299.424
R1b	-INF	
R1c	-INF	
C4a	-INF	
C4b	-INF	
C4c	-INF	
C8a	-INF	-953.773
C8b	-INF	
R2	-INF	-986.321
R3	-INF	
R4	-INF	
C12	-INF	
C11	-INF	-986.321
C10	-INF	-302.577
C9	-INF	
C7	-INF	
C6	-INF	
OCU	-INF	-967.452
C5a	-INF	
C5b	-INF	
C5c	-INF	

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LOWER LEVEL UPPER MARGINAL  
 ---- VAR Z        -INF 9.1075E+8    +INF        .

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Z Objective function

---- VAR Y Columns selection in superstruture associated with T Tasks(existance  
 Or Non-existance)

LOWER LEVEL UPPER MARGINAL  
 OIL Fractionator        .        1.000    1.000 56000.000  
 QUENCH Fractionator    .        1.000    1.000 56000.000  
 FEED                    .        1.000    1.000 56000.000  
 C1a                     .        1.000    1.000 56000.000  
 C1b                     .        .        1.000 -3.443E+8  
 C1c                     .        .        1.000 -3.508E+8  
 C2a                     .        .        1.000 56000.000  
 C2b                     .        .        1.000 56000.000  
 C2c                     .        .        1.000 56000.000  
 C3a                     .        1.000    1.000 56000.000  
 C3b                     .        .        1.000 56000.000  
 C3c                     .        .        1.000 56000.000  
 PSA                     .        1.000    1.000 56000.000  
 R1a                     .        1.000    1.000 56000.000  
 R1b                     .        .        1.000 56000.000  
 R1c                     .        .        1.000 56000.000  
 C4a                     .        .        1.000 56000.000  
 C4b                     .        .        1.000 56000.000  
 C4c                     .        .        1.000 56000.000  
 C8a                     .        1.000    1.000 56000.000  
 C8b                     .        .        1.000 56000.000  
 R2                      .        1.000    1.000 56000.000  
 R3                      .        .        1.000 56000.000  
 R4                      .        .        1.000 56000.000  
 C12                     .        .        1.000 56000.000  
 C11                     .        1.000    1.000 56000.000  
 C10                     .        1.000    1.000 56000.000  
 C9                      .        .        1.000 56000.000  
 C7                      .        .        1.000 56000.000  
 C6                      .        .        1.000 56000.000  
 OCU                     .        1.000    1.000 56000.000  
 C5a                     .        .        1.000 56000.000  
 C5b                     .        .        1.000 56000.000  
 C5c                     .        .        1.000 56000.000

---- VAR F Flow Rate of selected T task associated with S streams

LOWER LEVEL UPPER MARGINAL

OIL Fractionator	.	1000.000	1000.000	.
QUENCH Fractionator	.	1000.000	1000.000	-1.158E+8
FEED	.	998.800	1000.000	.
C1a	.	998.800	1000.000	.
C1b	.	.	1000.000	.
C1c	.	.	1000.000	.
C2a	.	.	1000.000	1.7592E+5
C2b	.	.	1000.000	1.4000E+5
C2c	.	.	1000.000	1.4000E+5
C3a	.	746.803	1000.000	.
C3b	.	.	1000.000	4.0808E+5
C3c	.	.	1000.000	1.4000E+5
PSA	.	251.997	1000.000	.
R1a	.	700.576	1000.000	.
R1b	.	.	1000.000	1.4000E+5
R1c	.	.	1000.000	1.4000E+5
C4a	.	.	1000.000	7.219E-12
C4b	.	.	1000.000	1.4000E+5
C4c	.	.	1000.000	1.4000E+5
C8a	.	46.227	1000.000	.
C8b	.	.	1000.000	2.6972E+5
R2	.	13.679	1000.000	.
R3	.	.	1000.000	1.4000E+5
R4	.	.	1000.000	1.4000E+5
C12	.	.	1000.000	1.4000E+5
C11	.	13.679	1000.000	.
C10	.	697.423	1000.000	.
C9	.	.	1000.000	EPS
C7	.	.	1000.000	2.8269E+5
C6	.	.	1000.000	2.8000E+5
OCU	.	32.548	1000.000	.
C5a	.	.	1000.000	1.7664E+5
C5b	.	.	1000.000	2.8269E+5
C5c	.	.	1000.000	1.4398E+5

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\*\*\*\* REPORT SUMMARY : 0 NONOPT  
 0 INFEASIBLE  
 0 UNBOUNDED

GAMS Rev 146 x86/MS Windows 06/03/06 22:29:18 Page 4  
; Naphtha Separation  
Execution

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---- 504 VARIABLE Z.L = 9.107464E+8 Objective function

---- 504 VARIABLE Y.L Columns selection in superstruture associated with T T  
asks(existance Or Non-existance)

OIL Fractionator	1.000,	QUENCH Fractionator	1.000
FEED	1.000, C1a		1.000
C3a	1.000, PSA		1.000
R1a	1.000, C8a		1.000
R2	1.000, C11		1.000
C10	1.000, OCU		1.000

---- 504 VARIABLE F.L Flow Rate of selected T task associated with S streams

OIL Fractionator	1000.000,	QUENCH Fractionator	1000.000
FEED	998.800, C1a		998.800
C3a	746.803, PSA		251.997
R1a	700.576, C8a		46.227
R2	13.679, C11		13.679
C10	697.423, OCU		32.548

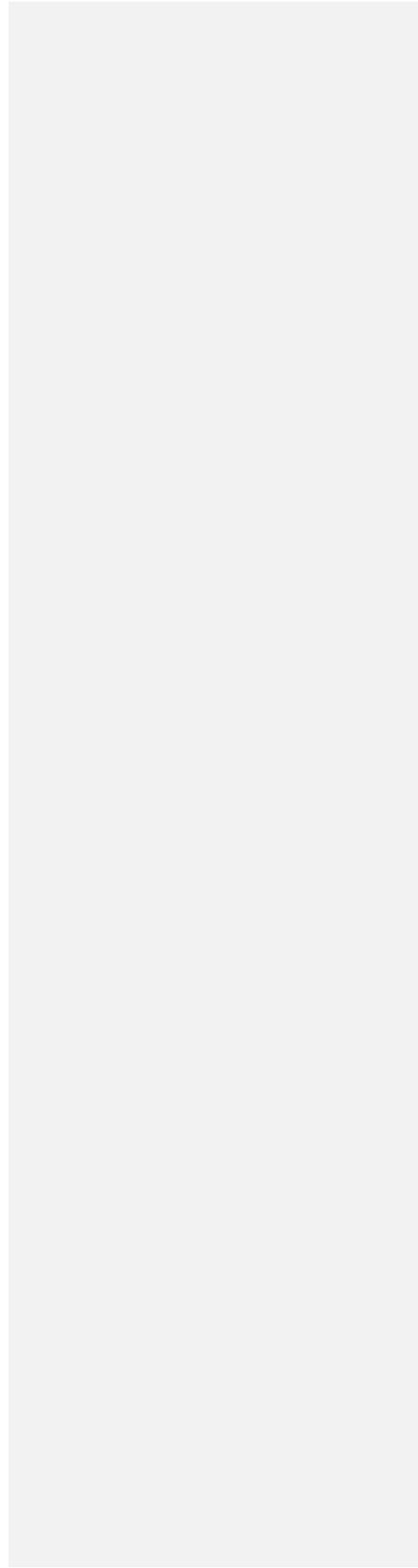
EXECUTION TIME = 0.010 SECONDS 3 Mb WIN223-146 Nov 21, 2006

USER: course license S060628:0842AL-WIN  
Phd course about mathematical programming DC5953  
License for teaching and research at degree granting institutions

\*\*\*\* FILE SUMMARY

Input C:\Documents and Settings\leesufen\Desktop\May\_FYP\Ethane\_EPMS\_24May.  
gms  
Output C:\Documents and Settings\leesufen\My Documents\gamsdir\projdir\Ethan  
e\_EPMS\_24May.lst

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APPENDICES II

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